MILLS AND MILLWORK

PART I.
TREATISE
ON
MILLS AND MILLWORK

PART I.
ON THE PRINCIPLES OF MECHANISM
AND ON
PRIME MOVERS

COMPRISSING THE ACCUMULATION AND ESTIMATION OF WATER POWER;
THE CONSTRUCTION OF WATER WHEELS AND TURBINES; THE PROPERTIES OF STEAM;
THE VARIETIES OF STEAM ENGINES AND BOILERS, AND WINDMILLS

BY

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THIRD EDITION.

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1871.
PREFACE

to

THE THIRD EDITION.

Although the work of the millwright, or the art of constructing the machinery of transmission in mills—considered separately from the machines employed in the manufacture—does not in the present stage of progress admit of much improvement, it has nevertheless undergone very considerable changes both in form and character. It is no longer of that heavy ponderous character which existed sixty years ago. The velocities of both shafts and wheels have been trebled, and in most cases quadrupled, and from this a saving of two-thirds in weight, and a proportionate saving of power, have been effected. All these facts are carefully recorded in the present volumes; and, taking into account the improvements in water-wheels, the investigation of steam as a motive power, and other practical instructions for the guidance of the millwright, I have no hesitation in recommending their careful perusal to the professional and the general reader.

Manchester: April 27, 1871.
PREFACE

to

THE SECOND EDITION.

The early demand for a Second Edition of my Treatise on Mills and Millwork, has enabled me to correct errors and supply omissions, which are almost sure to escape notice when the Author's time is occupied in professional pursuits.

The history of Mills is a subject which might be greatly extended; but the main object I have in view is to lay before the reader the results of a successful practice as a Millwright and Engineer during a period of more than half a century—a period which has contributed more than any previous one to the development and perfection of the manufacturing industry of the world.

Manchester: June 26, 1864.
PREFACE

to

THE FIRST EDITION.

There is probably no department of practical science so generally useful, or so little studied of late years, as the machinery of transmission. The term 'millwork,' as applied to this class of machinery, is of modern origin, but 'millwright' has long been a household word, and at no distant period conveyed the idea of a man marked by everything that was ingenious and skilful.

The millwright of former days was to a great extent the sole representative of mechanical art, and was looked upon as the authority in all the applications of wind and water, under whatever conditions they were to be used, as a motive power for the purposes of manufacture. He was the engineer of the district in which he lived, a kind of jack-of-all-trades, who could with equal facility work at the lathe, the anvil, or the carpenter's bench. In country districts, far removed from towns, he had to exercise all these professions, and he thus gained the character of an ingenious, roving, rollicking blade, able to turn his hand to anything, and, like other wandering tribes in days of old, went about the country from mill to mill, with the old song of 'kettles to mend' reapplied to the more important fractures of machinery.

Thus the millwright of the last century was an itinerant engineer and mechanic of high reputation. He could handle the axe, the hammer, and the plane with equal skill and precision;
he could turn, bore, or forge with the ease and despatch of one brought up to these trades, and he could set out and cut in the furrows of a millstone with an accuracy equal or superior to that of the miller himself. These various duties he was called upon to exercise, and seldom in vain, as in the practice of his profession he had mainly to depend upon his own resources. Generally, he was a fair arithmetician, knew something of geometry, levelling, and mensuration, and in some cases possessed a very competent knowledge of practical mathematics. He could calculate the velocities, strength, and power of machines: could draw in plan and section, and could construct buildings, conduits, or watercourses, in all the forms and under all the conditions required in his professional practice; he could build bridges, cut canals, and perform a variety of work now done by civil engineers. Such was the character and condition of the men who designed and carried out most of the mechanical work of this country, up to the middle and end of the last century. Living in a more primitive state of society than ourselves, there probably never existed a more useful and independent class of men than the country millwrights. The whole mechanical knowledge of the country was centred amongst them, and, wherever sobriety was maintained and self-improvement aimed at, they were generally looked upon as men of superior attainments and of considerable intellectual power. It, however, too frequently happened that early training, constant change of scene, and the temptation of jovial companions, led the young millwright into excesses which almost paralysed his good qualifications. His attainments as a mechanic, and his standing in the useful arts, were apt to make him vain; and with a rude independence he would repudiate the idea of working with an inferior craftsman, or even with another as skilful as himself, unless he was born and bred a millwright.* I

* This had reference to the young practitioner being the oldest son of a millwright, which circumstance in itself was, until of late years, considered a sufficient guarantee for skill and industry, whether he possessed them or not.
remember an old millwright who, in palliation of an offence with which his employer charged him, urged that he was the most useful man in his employ, and that he ought not to forget that he had even condescended to work with carpenters to please him.

The introduction of the steam engine, and the rapidity with which it created new trades, proved a heavy blow to the distinctive position of the millwright, by bringing into the field a new class of competitors in the shape of turners, fitters, machinists, and mechanical engineers; and, notwithstanding the immense extension of the demand for millwork and the great stimulus which it afforded to the manufactures of the country, it nevertheless lowered the profession of the millwright, and levelled it in a great degree with that of the ordinary mechanic. He, however, retains his distinctive appellation, and I hope he will long continue the representative of a higher class of mechanical artisans, to whom the public are deeply indebted for many of our first and greatest improvements in practical science.

Serious, and perhaps not altogether unfounded, charges have been brought against millwrights as a class, but on examination I do not think that they are borne out to the extent some persons would wish us to believe. On the contrary, I am persuaded there is no class of mechanics so intelligent or who work harder than the millwright, or who exercise a sounder judgment in the performance of their varied duties in the perfect execution of their work. It is true that, in former times, they too frequently gave way to habits of dissipation, and neglected their work; but in this respect they were not alone, as the changes which have lowered their standing have proved of use in reforming their habits, and produced in the millwrights of the present day a highly moral and intellectual class of workmen. Taking them as a body, I believe there is not a more trustworthy or a more respectable class of men in existence. I make this statement from experience, and have great pleasure in doing so.
It used to be a custom, before the days of Mechanics' Institutes, for the millwrights to form one for themselves in every shop. Their meetings were generally held at a public house on Saturday evenings; and many were the times when long discussions on practical science and the principles of construction were carried on between rival disputants with a fiery eagerness which not unfrequently ended in a quarrel, or effected a settlement by the less rational but more convincing argument of blows. It was a rough way of imparting knowledge, but it was not worse than that practised in the schools and seminaries of the day, where the application of the rod was the general remedy for dull apprehensions and indolent minds. This was beginning at the wrong end, endeavouring to impart knowledge through the sensitive parts of the body, instead of appealing to the higher organs of the intellect. The principal difference between the Millwrights' Institute and such schools was, probably, that the former was the more ferocious of the two, as the rival disputants hit harder under the influence of potations than would now, fortunately, be tolerated. On more peaceful occasions, however, it was curious to trace the influence of these discussions on the young aspirants around, and the interest excited by the illustrations and chalk diagrams by which each side supported their arguments, covering the tables and floors of the room in which they were assembled. The great objection to these gatherings was, however, the angry feeling too frequently aroused, and the injurious influence of the place of meeting, which gave rise to prolonged debates under the encouragement of the landlord, who on most occasions was appealed to as referee in all matters in dispute.

The above is no overdrawn statement of the condition of the millwrights some fifty years ago. Their education and habits were those of the times in which they lived. There were then no schools for the working classes but those of the parish, nor any libraries or mechanics' institutes; and after the usual course of reading, writing, and accounts, the millwright was thrown
upon his own resources in the attainment of the knowledge which might aid him in his profession. Hence his value and worth were most exhibited when away from home, and isolated from all assistance, where he was left to the construction and erection of work. In such a position his energies were frequently called into action, and on many occasions he displayed powers calculated to advance the interests of his employers, and to complete his task with accuracy and skill. Thus the genuine millwright became, to a fault, tenacious of his own views and position, and jealous of any interference or assistance from others. He would reconnoitre and survey the premises on which he was to work, rule and line in hand, and would stand for hours (much to the annoyance of his employers) before he could make up his mind as to what was best to be done. These preliminaries being settled, his decision was final, and he would fix his levels, stretch his lines, and in the course of a day or two commence work with an energy which generally led to the best and most satisfactory results.

Another feature of this class, which should not be lost sight of, was the kindly feeling and generous sympathy which generally belonged to them, and that exhibited especially towards those in declining years or in distress. It is in acts of charity and good will to those in want that the millwright of all times has shown his native goodness. He may frequently be reckless and dissipated, but he seldom fails in generosity, and I know of no other trade where a more hearty feeling of liberality and kindness exists.

Yet the millwrights, with all these good qualities, have been and are still subject to faults injurious to themselves, and annoying to the public. Such are their frequent contests with their employers, either for an advance of wages or for some fancied privilege which they seek to maintain or establish. They are united in benefit societies for the relief of the old and indigent, and those who from sickness or other causes may be unable to work. Unfortunately these are connected with trade
societies established for the purposes of maintaining what they consider their rights—rights often of a very imaginary character, and ill calculated to advance their position or promote their individual interests. It is not my wish to enter here into the questions which these contests suggest. I am willing to forget bygone days and to look forward with sanguine hope to better times, when truer principles of freedom and social economy shall be acted upon, without destroying the independence and originality which have always been characteristic of an intelligent body of men for whom I entertain individually and collectively the highest veneration and respect.

I have deemed it necessary to give this brief account of the habits and character of a body of men whose skill and spirit of perseverance has done so much for the advancement of applied science, and whose labours have still a large influence on the industrial progress of the country. I am, perhaps, better qualified for this task than most others, from having been associated with them from early life, so that an experience of some fifty years must be my excuse for having imposed this narrative upon the reader.

For many years I have had it in contemplation to give an account of my own practical experience in millwright construction, but a multiplicity of engagements has combined with other causes to delay the work, and to modify considerably the original plan. This first volume, I hope, may contain reliable data and true principles for the successful guidance of the millwright in his professional duties.

The present portion of the work treats of the first principles of mechanism generally, and proceeds to the discussion of the various constructions of prime movers. I hope shortly to complete the work by a treatise on the new system of transmissive machinery, and on the arrangements necessary for imparting motion to the various descriptions of mills.

The accumulation, storage, and measurement of water has received attention; as well as the construction of prime movers
THE FIRST EDITION.

depending upon this motive power, including the best forms of water-wheels, according to my own practice, and the more recently introduced varieties of turbines. In discussing the principles of the steam engine I have inserted a short treatise on the properties of steam, derived in part from researches carried on under my own superintendence, bearing on the density of saturated steam and the law of expansion of superheated steam. To this has been added a chapter on engines and boilers, their strength, powers, and principles of construction.

It is evident that, in the present improved state of mill machinery, steam and water are the chief agents on which we depend for motive power. In former times the wind was also looked to as a source of power, but it is now very little employed, except in Holland and the fenny districts of this country, where it is still used for pumping and other operations where constant uniformity of action is not required. Notwithstanding the changes effected by steam, as windmills are not yet obsolete, I have given a short chapter on their mode of construction.

In the prosecution of this work I have been ably assisted by my friend Mr. Thomas Tate, to whom I owe the chapter on the elementary principles of mechanism: as also to my assistant and secretary, Mr. William C. Unwin, to whose assiduous attention and love of science I am greatly indebted.
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ON
MILLS AND MILL-WORK.

SECTION I.
INTRODUCTION.
CHAPTER I.
EARLY HISTORY OF MILLS.

We may search in vain for dates from which to calculate the earliest period at which the principles of accumulating power, and transmitting it for employment in mills, were first introduced, and it is equally impossible to trace consecutively the progressive developments that have taken place from the days of antiquity to the present improved state of the arts. Perhaps the earliest introduction of machinery was in the processes for the preparation of food, as we read of the Egyptians and Babylonians, and other nations in Europe and Asia, having mills for grinding corn from the earliest period of historical records. Hesiod and Pliny both describe the most primitive method of the preparation of corn, a method still further illustrated among the pictorial remains of the Egyptians, viz. pounding in a mortar.

CORN MILLS.—When millstones were introduced is uncertain, although they boast of a high antiquity. Agatharcides (B.C. 113) mentions grinding stones employed in the reduction of gold ore in the mines on the Red Sea, and of the same kind,
no doubt, were the early flour mills. Two round stones, with concave and convex fitting surfaces, roughened or notched like the pestle in Pliny's description, is probably the best form for the distribution of the grain introduced through a hole in the upper stone, and to throw off the flour at the edges. A pivot in either stone, fitting a recess in the other, would be necessary to guide the upper or running stone, which would be moved by simple manual labour. Millstones of this kind, or querns, as they are commonly called, are found not unfrequently amongst the foundations of Roman villas, and along the lines of Roman encampments. Fig. 1 is a representation of the nether stone of such a mill found at Gayton, near Northampton, and figured in the 'Archaeologia,' vol. xxx. The stone of which these mills were composed was a sort of pudding stone or rough lava, which from its varying hardness tended to retain a biting surface. Some of the querns retain traces of the notches or 'work;' they vary from ten inches to twenty inches in diameter. Usually, as at the present time in some countries, these handmills were turned by women, but amongst the Romans male slaves were employed for this purpose, or it was reserved as a penal exercise for convicts.

The essential defects of this mode of grinding, the want of power, and the tediousness of the operation, led gradually to the employment of cattle mills, and these are sometimes mentioned by classical authors, although little was known of their construction until recently. In disentombing the baker's house at Pompeii, several of these large mills were found, in excellent preservation. Fig. 2 is a representation of one of them, and may be described as follows: The base a is a cylindrical stone, about five feet in diameter, and two feet high. Upon this, forming part of the same block, or else firmly fixed into it, is a conical projection, about two feet high, the sides slightly curving inwards; upon this rests another block c, externally resembling a dice-box, internally an hour-glass, being shaped into two hollow cones with their vertices towards each other,
CORN MILLS.

the lower one fitting the conical surface on which it rests, but not with any degree of accuracy. To diminish friction, however, a strong iron pivot was inserted in the top of the solid cone, and a corresponding socket let into the narrow part of the hour-glass shaped stone c. Four holes were cut through the stone parallel to this pivot, the narrow part was hooped on the outside with iron, into which wooden bars d d were inserted, by means of which the upper stone was turned on its pivot by the

Fig. 2.

Pompeian Corn Mill.

labour of men or asses. The upper hollow stone served as a hopper as well as a grinder, and was filled with corn, which fell by degrees through the four holes upon the solid cone, and was reduced to powder by friction between the two rough surfaces; of course it worked its way to the bottom by degrees, and fell out on the cylindrical base, round which a channel was cut to facilitate the collection. These machines are about six feet high in the whole, made of rough grey volcanic stone full of large crystals of leucite.*

Imperfect and tedious as the operation of grinding must still

have been, cattle mills seem long to have held their ground against further innovation, and even down almost to our own day in old works on machinery various contrivances for employing the labour of cattle in corn mills are described. However, before the Christian era a new power was beginning to be applied to corn mills, that of flowing or falling water. Probably the immense quantities of water required in Egypt and Assyria for the irrigation of the land first led to contrivances for turning to account the current of rivers as a motive power. Vitruvius describes water wheels employed both for raising water and for grinding corn,* the motion in the latter case being made available by a rude kind of gearing, in which we may trace the rudiments of our present transmissive machinery. Whittaker, in his 'History of Manchester,' describes a water mill ascribed to the Romans, of which traces were found in Manchester some years since. This mill served equally the purposes of the town and garrison, but was not alone sufficient, as the use of handmills remained very common in both, many having been found on the site of the station at Campfield. The Roman water mill at Manchester was placed upon the River Medlock, immediately below Campfield, and a little above an ancient ford. The sluice and conduit which actually regulated and conveyed the water to the mill was accidentally discovered about the middle of the last century. It was found at a place called Dyer's-croft, where a flood in the river swept away a dam with a large oak beam upon the edge of it, and disclosed a tunnel in the rock below. This, when excavated, was found to be about three feet wide and three feet deep, gradually narrowing at the bottom, and upon the sides the marks of the tool were everywhere to be found. This ancient tunnel was bared to the extent of twenty-five yards, but it evidently had been continued in a direct line up to the commencement of a wide weir in the river above. From these discoveries it will appear that mills for grinding corn by power were of ancient date even in this country.

In our attempts to trace the progress of the mechanical arts, we are compelled to leave a wide blank for the period of intestine war which succeeded the decline of the Roman Empire.

* Vitruvius, Architecture, book x. c. 10.
The conquest of Rome by Alaric and the spread of a race of barbarians over the whole of Europe, had the effect, for many centuries, of obliterating almost every vestige of the arts, which in the turmoil and tumult of war were either entirely lost or utterly neglected. Thus, for a long succession of years, during the middle ages and at the period of the Crusades, the industrial arts languished and retrograded, and it was not until the time of Michael Angelo and Galileo that mathematics, architecture, engineering and mechanics received the least encouragement or attention. The mathematician and natural philosopher had before then been looked upon with suspicion and carefully watched as persons dangerous to society. During the rise of painting, sculpture, and architecture, the arts which rendered the republics of Italy so illustrious, mechanicism began to attract notice, and to that age we may trace the introduction of water mills in many parts of Italy. Little or no progress, however, was made down to the close of the seventeenth century.

The Dutch, owing to the natural difficulties of their location, were urged, in their own defence, to take the lead in the field of mechanical appliance; and the vast embankments of that enterprising people, with their canals and docks, fully justify the remark that they were amongst the first to benefit mankind by the introduction of mills for grinding corn, which was chiefly imported, and of machines for draining the lands which their patient industry had reclaimed from the sea. As a prime mover the Dutch had no water power except what was obtained by impounding the tidal water and working it off during its reflux. At best this was an expensive and uncertain power, which caused wind to come into more general use; and during the greater part of the seventeenth century we were chiefly indebted to the Dutch and Belgians for our improved knowledge of mills and the extension of our manufacturing industry.

Mills for the Manufacture of Textile Fabrics.—Woollen, cotton, and linen cloth was manufactured in this country from an early period, and the manufacture of silk was practised in Italy in the twelfth century. It was subsequently introduced into France and other parts of Europe, and we learn that James I. encouraged the manufacture, and made an attempt to grow the
mulberry and produce silk in this country, which, however, as might have been expected, totally failed. During the reign of Charles I., the Commonwealth, and the reign of Charles II., the manufacture of silk goods made great progress, and it is stated that in 1661 as many as 40,000 persons were employed in that branch of industry. In 1685, on the revocation of the Edict of Nantes, a large colony of skilful French weavers settled at Spitalfields, and from that time to the present have carried on the manufacture in that locality. The winding, throwing, and weaving were chiefly done by hand, and it was only from the construction of the large throwing mill at Derby, in 1719, that we date the introduction of mill-machinery, technically so called, for the production of these fabrics.

Woollen mills have a much greater antiquity than either silk or cotton mills. Spinning and weaving processes were known in the time of Moses, and are illustrated in ancient Egyptian monuments. Pliny attributes the discovery of the art of fulling cloth to Nicias of Megara (B.C. 1131). The origin of the woollen manufacture is evidently beyond the reach of tradition, though the process of felting was probably known before the art of spinning and weaving. Among the Romans the woollen manufacture attained considerable perfection, and several of their writers describe the different qualities of cloth as used for the tunic and common stuff garments.

From the time of the Romans until the Norman Conquest we have no record of the manufacture of woollens, and it is certain that amongst the Saxons, and, indeed, for several centuries after the Conquest, the costume of the peasantry was of leather, and there is reason to believe that the 'buff- jerkin' retained its place as the ordinary dress of the labouring people of England until the time of the Commonwealth.

It is generally supposed that the woollen manufacture was introduced into this country in the reign of Edward III., but there is every reason to believe that it existed long before that time. Mr. McCulloch states that it was practised above a hundred years before that prince introduced improvements in the manufacture. What these improvements were is not known; probably they were neither more nor less than protective laws, which, by giving an increased monopoly to guilds and corpora-
tions, seriously injured the freedom and restricted the extension of trade.

The whole of the woollen mills, from a very early period to the commencement of the present century, were driven by water, and this will account for the locations on the streams of the west of England and Yorkshire, where the woollen manufacture was carried on. The introduction of improved machinery for the manufacture of cotton gave to the woollen trade an entirely new character; and from that circumstance we may safely date the vastly increased production and the great extension that have taken place in that important branch of manufacture.

The next article of importance in an historical point of view is cotton; and to this production we may to a great extent trace the advancement, prosperity, and power of the British Empire. The cotton manufacture had its origin in India, where the plant is indigenous, and where the climate renders a light absorbent fabric the most suitable clothing for the inhabitants. The manufacture of cotton in India may be dated from a period antecedent to the Romans; and the implements used in the different processes of the manufacture, from the cleaning of the wool to its conversion into muslin, are of a most simple kind, and may be purchased for a few shillings.

The cotton manufacture of China is of the same character as that of India; and although of immense extent, the articles produced are chiefly employed for home consumption. The arts in that country, as far as we know from the accounts of the missionaries and the more recent expedition of Lord Elgin, are stationary; and the tools, implements, &c., are of the same primitive kind as those used in India. The chief description of cotton goods exported when the Chinese became famous for their manufacture were nankeens; but these have long since given way to the cheaper productions of Great Britain, and for years past we have supplied the Chinese with large quantities of cotton yarn and cloth.

The first introduction of cotton into Europe and its manufacture were first attempted by the commercial states of Italy; and as early as 1560 cottons were exported from Venice to the different markets of Europe in the West. It was not, however, until the beginning of the seventeenth century that cotton was
manufactured in this country; but we have records that the manufacturers of Manchester bought cotton wool in London which came from Cyprus and Smyrna, and worked it into fustians, vermillos, and ditories. These goods were woven chiefly at Bolton, and finished by the Manchester dealers.

It is curious to trace the progressive increase of any description of manufacture, particularly that of cotton, which has attained to such colossal dimensions. In early times the weaver provided his own warp, which was of linen yarn, and cotton for his weft; buying these where he could best supply himself. In this way, every cottage formed an independent factory; the cotton was carded and spun by the female part of the family, and the cloth woven by the father and his sons.

Such was the state of the cotton manufacture before the introduction of power machinery, and the division of labour and the separation of the different processes into distinct employments. At this time the workman had usually his residence in the country, where, with a little garden and perhaps grass for a cow, he carried on his trade and earned a comfortable subsistence. ‘How much more,’ says a philanthropic writer, ‘of the comforts of life and of the means of natural enjoyment belong to this state of manufacture than to the more advanced, in which combined systems of machinery and a more perfect division of labour collect the workmen into factories and towns!’

It will not be necessary to enumerate here the well-known improvements of Arkwright, Hargreaves, and Crompton, or the changes which followed the introduction of machines for carding, roving, and spinning. Suffice it to observe that these improvements inaugurated a new system of operations, and created a new demand for power and the means of transmitting it to the different machines required in the manufacture. It was about this time and at a rather later period that the improvements of the motive power and machinery of transmission were introduced.

To the steam engine in the first place, and subsequently to the improved machinery and mill-work, we may attribute the present gigantic extent of our manufactures. The factory system, which has supplanted the cottage manufacture, has enlarged
the resources of the country far beyond those of any former period. This island stands pre-eminent in productive industry, and it is a source of pride and gratification to find that these blessings, springing out of the application of physico-mechanical science, have been attained by the skill and indomitable perseverance of our own countrymen.

To the immediate action, foresight, and intelligence of the Government of this country, the workers in coal, iron, and cotton are under no obligation; but they owe much to their own invention, skill, and industry in the prosecution and development of these pursuits, and the only merit that can be claimed by the Government is its non-interference and the protection it affords through the laws of the kingdom, which give security to property and to individual exertion in the varied departments of productive industry. Further, Dr. Ure, in his 'Philosophy of Manufactures,' argues that 'the constant aim of scientific improvements in manufactures is philanthropic, as they tend to relieve the workman either from niceties of adjustment, which exhaust his mind, or from painful repetition of efforts which distort or wear out his frame.' Illustrations of this truth are presented every day from the remarkable extent to which labour is saved, by self-acting machines, all of them within the domain of automatic science, and producing a result of superior quality and beauty in the manufacture.

The division of labour carried out by means of the factory system is not exclusively applied in the manufacture of cotton, flax, silk, and woollen cloths; it pervades almost the whole of our manufacturing industry, and is beginning to show itself in mining and agriculture, and the time is probably not far distant, when we shall witness almost every operation of the human hand carried on by a system of divided activity, equally conducive to the interests of individual enterprise and to the public benefit.

The term Factory, according to Dr. Ure, designates, 'the combined operation of many orders of workpeople, adult and young, tending with assiduous skill a system of productive machines, continuously impelled by a central power. This definition includes cotton mills, flax mills, silk mills, woollen mills, and certain engineering works, but it excludes those in
which the mechanisms do not form a connected series, or are not dependent upon one prime mover.' The factory system is so much extended since these words were written as to change the relations of labour, and to affect almost every manufacturing process. It has created a much higher and more intelligent class of workmen than existed under the hand system, more respectable, better paid, better housed, and better clothed than heretofore.

**Iron Manufactures.**—We are at the present time in a state of transition in the manufacture of iron and steel, which is making rapid strides towards improvement. The inventive talent of the country has been directed to this object, and the production of homogeneous plates, having the elasticity and tenacity of steel, together with the improvements of Mr. Bessemer, Mr. Clay, and others, are likely to produce a complete revolution by a greatly increased economy in the production of iron. Mr. Bessemer is now proposing to roll plates in the form of a continuous web from liquid metal, run direct from the furnace to the rolls. We cannot vouch for the success of this enterprise, but we are most anxious to see its results realised; and there cannot exist a doubt, from the number of able chemists and practical men at work, that the iron trade of this country is destined to undergo a great change, and perhaps with as much benefit as was accomplished by Mr. Cort on the introduction of the puddling and rolling processes.

In the machinery department of iron manufacture there is nothing to boast of; it is still crude and rough in its character, perhaps necessarily so, on account of its liability to breakage in rolling, and other processes requiring great power. It is, however, possible, that the processes now in progress may introduce new and more perfect machinery into the manufacture, and that the ironmaster may calculate with the same certainty upon continued progress in his manufacture as now exists in trades where machinery is employed.

Although much change has not been effected in the machinery of the iron manufacturer, considerable improvements have nevertheless been made in the smelting of the ores, and since the introduction of hot blast by Mr. Neilson the production of the furnaces has been more than doubled. Looking
forward, therefore, to the improvements and changes now in progress, we may reasonably conclude that a new era is not only imminent, but has in great part been accomplished. The same progress, and even greater improvements, are observable in the conversion of iron into steel, and probably the time is not far distant when we shall be enabled to produce from the same furnace iron in either a cast or malleable state, or steel, as may best suit the requirements of the manufacturer. It is quite evident that our increasing knowledge of chemistry in iron manufactures leads to these results, and by a still closer adherence to chemical research, whereby impurities, such as phosphorus, sulphur, &c., are removed, the process just alluded to will be fully and satisfactorily realised.

In addition to the changes now in progress in the manufacture of iron and steel, it may be stated that a new system of welding by compression is on the point of being introduced for the purpose of consolidating the mass, increasing its strength, and giving form and variety to the article required. It is immaterial whether it be in the shape of a plate or a forging for particular use—the process is the same, namely, by statical pressure calculated to the extent of 250 to 300 tons upon the square foot. This force is imparted to the mass by the hydraulic press at a welding heat, and the impression of the mould is faithfully given when left to cool under pressure. It has yet to be seen what is the effect of this new process, but I believe it is in successful operation by Mr. Hassal at Vienna.
SECTION II.
PRINCIPLES OF MECHANISM.

CHAPTER I.
GENERAL VIEWS.—LINK-WORK.—WRAPPING CONNECTORS.—WHEEL-WORK.—SLIDING CONTACT.

I. GENERAL VIEWS RELATIVE TO MACHINES.

Definitions and Preliminary Expositions.

1. Mechanism may be defined as the combination of parts or pieces of a machine, whereby motion is transmitted from the one to the other.

2. When a body, or any piece of mechanism, moves in a straight line it is said to have a rectilinear motion, and when it moves in a curved line it is said to have a curvilinear motion. When a point moves constantly in the same path, it is said to have a continuous motion, but if it moves backwards and forwards it is said to have a reciprocating motion. We may have reciprocating rectilinear motions as well as reciprocating curvilinear motions.

If a body moves over equal spaces in equal intervals of time, it has a uniform motion; but if it moves over unequal spaces in equal intervals of time, it has a variable motion.

3. The velocity of a body is the rate at which it moves. In uniform motion the velocity is constant; but in variable motion the velocity continually changes. If the velocity of a body increase it is said to be accelerated, and if the velocity decrease it is said to be retarded.

The motion of a body is said to be periodical when it undergoes the same changes in the same intervals of time.

4. In order to express the velocity of a body, we must have a certain number of units of space passed over in a certain unit
of time. It is customary to take a foot as the unit of space, and a second as the unit of time.

In uniform motion, the space passed over is equal to the product of the velocity by the time. Thus, let \( s \) be the space in feet, \( t \) the time in seconds, and \( v \) the velocity per second; then

\[
s = v t \quad (1)
\]

which expresses the general relation of space, time, and velocity, in uniform motions. Any two of these elements being given, the remaining one may be found; thus we have

\[
v = \frac{s}{t} \quad (2), \quad t = \frac{s}{v} \quad (3).
\]

5. If the velocity in one certain direction be taken as positive, then that in the opposite or contrary direction will be negative.

6. If two wheels perform a revolution in the same time, their angular velocities are equal, whatever may be the dimensions of the wheels. The angular velocity of a revolving wheel or rod is the velocity of a point at a unit distance from the centre of motion. The wheel or rod will revolve uniformly when the angular velocity is uniform. If \( \lambda \) be the angular velocity, \( r \) the radius of the wheel or length of the rod, \( v \) the velocity at this distance from the centre of motion; then

\[
\lambda = \frac{v}{r} \quad (1), \quad \text{and} \quad v = \lambda r \quad (2).
\]

7. The motion of wheels is conveniently expressed by the number of rotations which they perform in a given time. Thus, let \( n \) be the number of revolutions performed per min., the other notation being the same as in Art. 6; then

\[
v = \frac{1}{30} \pi n r \quad (1), \quad \text{and} \quad n = \frac{30 v}{\pi r} \quad (2).
\]

Or substituting \( \lambda \) for \( \frac{v}{r} \), see formula (1), Art. 6,

\[
n = \frac{30 \lambda}{\pi} \quad (3), \quad \text{and} \quad \lambda = \frac{1}{30} \pi n \quad (4).
\]

Hence the number of turns performed in a given time varies as the angular velocity.

The number of turns which two wheels respectively make in the same time is called their \textit{synchronous} rotations. Let \( q \) and
PRINCIPLES OF MECHANISM.

\( q \) be the synchronal rotations of two wheels whose angular velocities are \( \lambda \) and \( \alpha \), respectively; then \( \frac{Q}{q} = \frac{\lambda}{\alpha} \); that is, synchronal rotations are in the ratio of the angular velocities.

Example.—Let a wheel whose radius is 6 ft. perform 50 revolutions per min., required 1st, the velocity of its circumference, and 2nd, its angular velocity.

Here, by eq. (1), \( n = 50 \), and \( r = 6 \), then

\[
v = \frac{1}{30} \times 3\cdot1416 \times 50 \times 6 = 31\cdot416 \text{ ft. per sec.}
\]

And, by eq. (4), \( \lambda = \frac{1}{30} \times 3\cdot1416 \times 50 = 5\cdot236 \).

8. If \( v \) and \( v \) be the velocities of two parts of a piece of mechanism, then \( \frac{V}{v} \) is the velocity ratio of these parts. Let \( s \) and \( s \) be the corresponding spaces described in the same time, then when the motion is uniform

\[
\frac{V}{v} = \frac{s}{s} = \text{a constant;}
\]

that is, when the velocities are uniform, the velocity ratio is constant.

9. If the velocity ratio of the two parts remains constant, then, however variable the velocities themselves may be, we still shall have \( \frac{V}{v} = \frac{s}{s} \); where \( s \) and \( s \) are the entire spaces described in the same interval of time.

10. When a body moves with a variable motion, its velocity at any instant is determined by the rate at which it is moving at that particular instant, that is, by the space which it would move over in one second, supposing the motion which it then has to remain constant for that time.

Variable motions may be graphically represented, by taking the abscissa of a curve equal to the units of time, and the ordinates equal to the units of the corresponding velocities. Thus, let \( a \) be equal to the units of velocity at the commencement of the motion; \( a \) the units in

![Fig. 3](image-url)
interval of time; \( CD \) the units in the corresponding velocity; and so on; then the area of the curved space \( ABDFE \) will be equal to the space described in the interval of time represented by \( AL \).

If the motion be uniform, the curve \( BDF \) will become a straight line parallel to \( OX \), and the space described in any given time will be represented by the area of a rectangle, whose length is equal to the units of time, and breadth equal to the units of velocity.

If the motion be uniformly accelerated or retarded, the curve \( BDF \) will become a straight line inclined to the axis \( OX \), and the space described, in this case, will be represented by the area of a trapezoid, whose base is equal to the units of time, and parallel sides respectively to the velocity at the commencement and end of that time.

11. THE PARTS OF A MACHINE.—A machine consists of three important parts.

(1.) The parts which receive the work of the moving power—these may be called RECEIVERS of work.

(2.) The parts which perform the work to be done by the machine—these may be called WORKING PARTS, or more simply, OPERATORS.

(3.) The mechanism which transmits the work from the receivers to the working parts or operators—these pieces of mechanism may be called COMMUNICATORS OF WORK, or the TRANSMISSIVE MACHINERY.

The form of the mechanism must always be determined from the relation subsisting between the motions of the receivers and operators.

If there were no loss of work in transmission (from friction, &c.) the work applied to the receiver would always be equal to the work done by the operator. Thus, let \( p \) be the lbs. pressure applied to the receiver, and \( s \) the space in feet which it moves over in a certain time; \( P \), the lbs. pressure produced at the working part, and \( S \), the space in feet which it moves over in the same time; then, neglecting the loss of work by friction, we have—

\[
\text{Work applied to the receiver} = \text{work done upon the operator},
\]

or \( p \times s = P \times S \) \( \ldots (1) \).
However, it must be borne in mind, that the actual or useful work done by a machine is always a certain fractional part of the work applied; this fraction, determined for any particular machine, is called the modulus of that machine. If $m$ be put for this modulus, then we have from eq. (1)

$$m \times p \times s = p_1 \times s_1 \cdots (2).$$

In treating of the motion of these parts of a machine it is generally most convenient to find an expression for their proportional velocities. Thus, let $v$ be the velocity of the receiver, and $v_1$ that of the operator; then $\frac{v}{v_1}$ is their velocity ratio. See Art. 8.

It must be observed, that this velocity ratio is not at all affected by the actual velocities of the parts, provided the velocity ratio of the mechanism be constant for all positions. In the more ordinary pieces of mechanism (such as common toothed wheels, wheels moved by straps, levers, &c.) the velocity ratio is constant; that is to say, it remains the same for all positions of the mechanism.

In eq. (1) $s$ may be taken as the velocity of the power $p$, estimated in the direction in which it acts, and $s_1$ that of the resistance $p_1$; then this equality becomes—

$$p \times v = p_1 \times v_1 \cdots (3),$$

or $\frac{p_1}{p} = \frac{v}{v_1} = \text{the velocity ratio} \cdots (4).$

Now $\frac{p_1}{p}$ is called the advantage gained by the machine, or the number of times that the resistance moved is greater than the power applied. Hence the advantage gained by a machine, irrespective of friction, &c., is equal to the velocity of the power divided by the velocity of the resistance, or the velocity ratio of the power and resistance.

This is called the principle of virtual velocities. Workmen express this dynamic law by saying, 'What is gained in power is lost in speed.'

12. The directional relation of the motion of the receiver and the operator admits of every possible variation. It may be constant or it may be variable. By the intervention of me-
Elementary forms of Mechanism.

13. In analysing the parts of a machine we find motion transmitted by jointed rods or links, by straps and cords, by wheels rolling on other wheels, and by pieces of various forms sliding or slipping on other pieces. Hence we have the following elementary forms of mechanism:

1. Transmission of motion by jointed rods,—LINK-WORK.
2. By straps, cords, &c.,—WRAPPING CONNECTORS.
3. By wheels or curved surfaces, revolving on centres, rolling on each other,—WHEEL-WORK.
4. By pieces of various forms, sliding or slipping on each other,—SLIDING-PIECES.

14. The velocity ratio, as well as the directional relation, in an elementary piece of mechanism may be either constant or varying. The number of combinations of which these elementary pieces admit, is almost unlimited. The eccentric wheel is a combination of sliding pieces and link-work. The common crane is a combination of wheel-work, link-work, and wrapping connectors; and so on to other cases.

A train of mechanism must be supported by some framework; the train of pieces being such, that when the receiver is moved the other pieces are constrained to move in the manner determined by the mode of their connection. Revolving pieces, such as wheels and pulleys, are so connected with the frame that
every portion of them is constrained to move in a circle round the axis; and sliding pieces are constrained to move in straight lines by guides.

Mechanism is to a great extent a geometrical inquiry. The motion of one piece in a train may differ, both in kind and direction, from the motion of the next piece in the series; these changes are effected by the geometrical construction of the pieces, as well as by their mode of connection. The investigation of the law of these changes constitutes one of the chief objects of the principles of mechanism.

II. ON LINK-WORK.

15. If a bent rod or lever $ABC$ turn upon the centre $C$, the velocities of the extremities $A$ and $B$ will be to each other in the ratio of their distances from the centre of motion $C$; that is,

\[
\frac{\text{velocity } A}{\text{velocity } B} = \frac{\text{circum. cir. } A Q_1}{\text{circum. cir. } B Q} = \frac{AC}{BC}
\]

Fig. 4.  

It is not necessary that the arms $AC$ and $BC$ should be in the same plane. Thus let $CD$ be an axis round which the arms $AB$ and $BF$ revolve, then,

\[
\frac{\text{velocity } A}{\text{velocity } B} = \frac{\text{perpend. dis. } A \text{ from the axis}}{\text{perpend. dis. } B \text{ from the axis}}
\]

Fig. 6.
16. Let \( AB, BD, DE \), be a series of levers turning on the fixed centres \( C, Q, \) and \( R \); then when the arcs through which the extremities \( A \) and \( E \) are moved are small the velocity ratio will be expressed by the following equality:

\[
\frac{\text{velo. } A}{\text{velo. } E} = \frac{AC \cdot BQ \cdot DR}{BC \cdot DQ \cdot ER};
\]

that is to say, the velocity ratio of \( P \) and \( P_1 \) is found by taking the product of the lengths of the arms lying towards \( P \), and dividing by the product of those lying towards \( P_1 \).

17. To find the velocity ratio of the rods \( AB \) and \( CD \) turning on the fixed centres, \( A \) and \( D \); and connected by the link \( BC \).

Through the centres \( A \) and \( D \), draw the straight line \( DE \) \( A \), cutting \( CB \) in \( E \); and from \( A \) and \( D \) let fall the perpendiculars \( AG \) and \( DK \) upon \( CB \), or it may be upon \( CB \) produced. Then

\[
\frac{\text{ang. velo. } DC}{\text{ang. velo. } AB} = \frac{AG}{DK} \quad (1);
\]

that is to say, the angular velocities of the rods \( DC \) and \( AB \) are to each other in the inverse ratio of the perpendiculars let fall from their respective axes upon the direction of the link.

Similarly we also have,

\[
\frac{\text{ang. velo. } DC}{\text{ang. velo. } AB} = \frac{AE}{DE} \quad (2);
\]

that is to say, the angular velocities of the rods \( DC \) and \( AB \) are to each other in the inverse ratio of the segments into which the link divides the line joining their axes.

These velocity ratios are obviously varying, depending upon the relative positions of the rods.

18. The Crank and Great Beam.—Let \( AB \) represent one half of the great beam of a steam engine, \( DC \) the crank, and \( BC \) the connecting rod. Putting \( \beta \) for the angle \( DCB \), and \( \beta_1 \) for the angle \( ABC \); then
PRINCIPLES OF MECHANISM.

\[
\frac{\text{velo. crank}}{\text{velo. beam}} = \frac{\sin \beta}{\sin \beta} \quad (1).
\]

When the connecting rod \( b \ c \) is very long as compared with the length of the crank \( d \ c \), then \( \beta \) is nearly constant, being nearly equal to \( 90^\circ \), in this case, eq. (1) becomes

\[
\frac{\text{velo. crank}}{\text{velo. beam}} = \frac{1}{\sin \beta} \quad (2).
\]

The crank must be in the same straight line with the connecting rod, at the highest and lowest points of the stroke of the beam, and then \( \beta = 0 \). In these positions the crank is said to be at its dead points.

The velocity ratio, expressed by eq. (2), will be a maximum when \( \beta = 0 \), that is, the velocity of the crank will be a maximum when it is in its dead points. When \( \beta = 90^\circ \), or when the crank is at right angles to the connecting rod, then the velocity of the crank is a minimum.

If \( r = A \ b \), or one-half the length of the great beam; \( r = d \ c \), the length of the crank; and \( \lambda = \) the angular oscillation of the beam, or the whole angle described by the beam in one stroke; then

\[
\tau = r \sin \frac{\lambda}{2} \quad (3)
\]

which expresses the length of the crank in terms of the radius of the beam and angle of its stroke.

A double oscillation of the beam produces one complete rotation of the crank, or conversely, taking the crank as the driver, each rotation of the crank produces a double oscillation in the beam.

From eq. (1) it follows, that the velocity of the crank is equal to the velocity of the beam, when \( \beta = \beta_1 \) or angle \( d \ c \ b \) is equal to angle \( a \ b \ c \); that is, when the position of the crank is parallel to that of the beam.

By this form of the crank the reciprocating circular motion of the extremity of the beam is changed into a continuous circular motion; and conversely a continuous circular motion is changed into a reciprocating circular motion.
19. To determine the various relations of position and velocity of the crank and piston in a locomotive engine.

Here the connecting rod, DE, is attached to the extremity of the piston rod, PD, and the length of the stroke of the piston is equal to double the length of the crank, FE. Moreover, the centre, F, of the crank is in the same straight line with the axis of the cylinder, or the direction of the piston rod.

Let $l = DE$, the length of the connecting rod;

$l_1 = PD$, the length of the piston rod;

$r = FE$, the length of the crank;

$k = FD$, the varying distance of the extremity of the piston rod from the axis of the crank;

$h = $ the corresponding height of the stroke of the piston;

$\theta = $ the varying angle, FE D, which the crank forms with the direction of the connecting rod.

(1.) The velocity ratio of the crank and piston is expressed by the following equality:

$$\frac{\text{velo. crank}}{\text{velo. piston}} = \frac{k}{l \sin \theta} \ldots (1), \text{ or}$$

$$= \frac{1}{\sin \beta} \ldots (2),$$

where $\beta$ in eq. (2) is put for angle $EF D$; that is, the angle which the crank makes with the direction of the piston rod.

This latter form of the expression is the same as that given in eq. (2), Art. 18.

(2.) When the piston is at the bottom point of its stroke,
its distance from \( F = F E + E D + D F = r + l + l_1 \); also
\[ FD = F E + D E = r + l. \]

When the piston is at the middle point of its stroke, then
\( FD = ED \); that is to say, in this position of the piston \( DEF \)
will be an isosceles triangle.

(3.) The position of the crank at any point of the stroke of the
piston is determined by the two following general equations:

\[ k = r + l - h \ldots (3). \]

\[ \cos \theta = \frac{r^2 + l^2 - (r + l - h)^2}{2rl} \ldots (4). \]

When the piston is at the middle point of its stroke, then
\( h = r \), and eq. (4) becomes

\[ \cos \theta = \frac{r}{2l} \ldots (5). \]

When the crank is at right angles to the connecting rod
\( \theta = 90^\circ \), and then we find from eq. (4),

\[ h = r + l - \sqrt{r^2 + l^2} \ldots (6). \]

This expression is, obviously, less than \( r \), or half the whole
stroke of the piston. Hence it appears that the crank is at
right angles with the connecting rod before the piston has
attained the middle point of its upward stroke.

20. Fig. 9 shows how a rotation of the axis \( \alpha \) is transmitted
to another \( c \), by means of the two equal cranks
\( A B \) and \( C D \), connected by the connecting rod \( D B \),
whose length is equal to the distance \( A C \), be-
tween the two axes. In all positions of
the cranks, the figure \( ABCD \) will be a parallelogram,
and the velocity of \( D \) will always be equal to the
velocity of \( B \), and the motion of the axis \( C \) will
be exactly the same as that of the axis \( A \).

21. Two sets of cranks may be placed upon
the axes, having the cranks on each axis at right
angles to each other, similar to the mode of
connecting the wheels of a locomotive engine,
as shown in fig. 10, where the cranks are formed
by bending, or loops made in the axes. These
axes must be parallel to each other, and the connecting rods
must also be of equal lengths.
The advantage of this combination consists in maintaining a constant moving pressure, by which means an equable motion is sustained without the aid of the inertia of the machinery.

22. The double universal joint represented in fig. 11 furnishes another example of link-work for transmitting motion from one axis to another axis. This useful piece of mechanism should be constructed so that the extreme axes, \(AB\) and \(CD\), would meet in a point, if produced, and the angles which they respectively make with the central line of the intermediate piece, \(EFHG\), shall be equal to each other.

23. This beautiful and useful piece of mechanism is formed by a combination of link-work.
Let $AB$ and $CD$ (see figs. 12 and 13) be two rods, turning on the fixed centres $A$ and $D$, and connected together by the short link $CB$; then, when motion is given to the rods, there is a certain point, $E$, in the link $CB$, which will move, or very nearly move, in a straight line. In matter of fact the path, or locus, of this point is a curve of the fourth degree; but when the motion of the rods is limited, and their lengths are considerable as compared with the length of their connecting link, this path becomes almost exactly a straight line.

In fig. 13, $CBK$ is a parallel frame of links; to the joint $C$ is attached the piston rod $RP$ of the steam engine; and to the point $E$ is attached the piston rod of the air-pump.

1. To find the point $E$ (see fig. 12) to which the air-pump rod must be attached, having given the radius rod $CD$, the link $CB$ or $QG$, and the rod $AB$ or $AG$ forming a part of the great beam.

Let $DQ$, $AG$ be an extreme position of the rods. Let the rods be moved to the position $ABCD$, where the link $CB$ is perpendicular to $AB$ and $DC$. Produce $BC$, meeting the link $QG$ in the point $E$; then $E$ will be that point of the link which will most nearly move in a vertical straight line. The ratio of $QE$ to $GE$ is generally expressed by the following equality:

$$\frac{QE}{GE} = \frac{R}{r} \times \left(\frac{r \sin \alpha}{2} \right) \times \left(\frac{R \sin A}{2} \right) \quad (1);$$

where $R = AB$, $r = DC$, $\alpha = \angle CDQ$, and $A = \angle BAG$.

Practically, the link $QG$ or $CB$ deviates very little from the vertical; and the angles $\alpha$ and $A$ are small; hence, $r \sin \frac{\alpha}{2} = R \sin \frac{A}{2}$ very nearly; in this case, therefore, eq. (1) simply becomes

$$\frac{QE}{GE} = \frac{R}{r} \quad (2);$$
and from this equality we readily find,

\[ GE = \frac{DQ \times GQ}{DQ + AG} \] (3),

which gives the position of the point E, as required.

When \( DQ = AG \), then \( GE = \frac{GQ}{2} \), that is to say, in this case, the point E is at the middle of the link QG or CD.

Example.—Let \( AB \) or \( AG = 5 \text{ ft.} \); \( DC \) or \( DQ = 4 \text{ ft.} \); and \( CB \) or \( GQ = 1\frac{1}{2} \text{ ft.} \); then by eq. (3) we have—

\[ GE = \frac{\frac{4}{1} \times 1\frac{1}{2}}{\frac{4}{1} + 5} = \frac{2}{3} \text{ ft.} \]

(2.) To find the length of the radius rod DC (see fig. 13), when the divisions, A B and B K, on the beam are given.

In this case,

The radius rod, \( DC = \frac{AB^2}{BK} \) ... (4).

When \( AB = BK \), then \( DC = AB \); that is, in this case, the radius rod will be equal to the division AB on the beam.

Example.—Let \( AB = 6 \text{ ft.} \), and \( BK = 4 \text{ ft.} \); then by eq. (4) we have—

The radius rod, \( DC = \frac{6^2}{4} = 9 \text{ ft.} \)

To multiply Oscillations by means of Link-work.

24. Fig. 14 represents a system of links B C, C D, and D E, turning on the fixed centres A and E, and having the arms AB and AC united to the same centre A. The construction is such, that while the rod AB makes a single oscillation from B to I, the rod ED will make a double oscillation, viz., from D to F and back from F to D. The oscillations of AB are produced by the rotation of a crank (see Art. 17), or by any other means.
The conditions of the construction may be stated as follows:

Given the lengths of the arms $AC$ and $ED$, the lengths or angles of their oscillations, and the length of the connecting link $CD$, to construct the mechanism, so that the rod $ED$ shall perform two oscillations whilst $AB$ makes one.

Let $BA$ be the position of the bent lever at the commencement of the upward oscillation. Draw $AI$ and $AH$, making the angles $BAI$ and $CAH$ each equal to the angle of the oscillation. From $A$ as a centre, with $AB$ and $AC$ as radii, describe the arcs $BI$ and $CH$. Through $A$ draw $AGF$, bisecting the angle $CAH$, cutting the arc $CH$ in $G$. On $AGF$ take $AF$, equal to the sum of the rods $AC$ and $CD$, and make $FD$ equal to the given length of the oscillation of $ED$. From $D$ and $F$ as centres, with a radius equal to the length of the rod $ED$, describe circles, cutting each other in $E$; then $E$ will be the centre of the rod $ED$, which will perform two oscillations, whilst the rod $AB$ makes one.

When $AB$ and $AC$ are in the middle points of their oscillations, the rod $ED$ will have the position $EF$; that is, it will have performed a complete upward oscillation. When $AB$ and $AC$ have performed the remaining halves of their oscillations, the rod $EF$ will have returned to the original position; that is, it will have performed a complete downward oscillation.

In like manner the oscillations may be further multiplied by connecting $ED$ with another series of links.

**To produce a Velocity which shall be rapidly retarded by means of Link-work.**

25. In fig. 15, $RAC$ and $ED$ represent two rods, turning on fixed centres $A$ and $E$, and connected by a link $CD$: the rod $ED$ is supposed to oscillate uniformly between the positions $ED$ and $EF$. Now the construction is such as to produce a rapidly retarded motion of the rod $RC$ in moving from the position $RAC$ to the position $SAE$, and conversely.

The conditions of the construction may be stated as follows:

Given the rods $ED$ and $DC$ in position and magnitude, the angle of oscillation $DEF$, and the length of the rod $AC$, to construct the mechanism.
RECIROCATING INTERMITTENT MOTION.

Bisect the arc $DF$ in $G$, and then bisect the arc $FG$ in $K$; through the points $K$ and $E$ draw the straight line $KEC$; from

Fig. 16.

$D$ and $K$ as centres, with a radius equal to the length of the link $DC$, describe arcs cutting $KEC$ in the points $C$ and $B$; from $B$ and $C$ as centres, with a radius equal to the length of the rod $AC$, describe arcs cutting each other in the point $A$; then $A$ will be the centre of the rod $AC$.

When the rod $ED$ arrives at the position $EG$, the rod $EAC$ will have the position $SAE$ very nearly, and it will have moved with a rapidly retarded motion. During the remaining half of the oscillation $GF$, the rod $SAE$ will remain, virtually, stationary.

This piece of mechanism was first employed by Watt for opening the valves of the steam engine.

To produce a Reciprocating Intermittent Motion by means of Link-work.

26. $AB$ and $CD$ (fig. 16) are two rods, turning on the fixed centres $A$ and $D$, and connected by a link $BC$. The rod $AB$ is made to oscillate between the positions $AB$ and $AI$, by means of a crank and connecting rod. The construction of the mechanism is such, that the rod $DC$ will oscillate between the positions $DC$ and $DF$, but with an intermittent motion.
The conditions of the construction may be stated as follows:
Given the rods $AB$, $BC$, and $CD$ in position and magnitude, to construct the mechanism.

Fig. 16.

From $A$ as a centre, with the radius $AB$, describe the arc $BI$; through $C$ and $A$ draw the straight line $CA$, meeting the arc in $G$; make $GE$ equal to one-third the arc $GE$, and on the arc take $GI$ equal to $GE$; on the line $GA$ take $GF$ equal to $EC$; then half the chord $BI$ will give the length of the crank, and $CF$ will be the arc through which the rod $DC$ oscillates.

Bisecting the angle $BAE$, &c., the position of the rod $D'C'$ is found, which being connected with $E$, by the link $BC'$, will oscillate exactly in a contrary manner to that of the rod $DC$; that is to say, when $DC$ is stationary $D'C'$ will be in motion, and conversely.

When the point $E$ arrives at $E$, the rod $DC$ will have completed, practically, its oscillation, and there it will remain stationary until the rod, turning on the centre $A$, returns from the position $AI$ to $AE$. 
The Ratchet-wheel and Detent.

27. In fig. 17, \( A \) represents the ratchet-wheel and \( D \) the detent, falling into the angular teeth of the ratchet, thereby admitting the wheel to revolve in the direction of the arrow, but at the same time preventing it from revolving in the opposite direction.

In certain kinds of machinery, the action of the moving force undergoes periodic intermissions; in such cases the ratchet and detent are used to prevent the recoil of the wheels, and sometimes to give an intermittent motion to the wheel, as in the following example.

*Intermittent Motion produced by Link-work connected with a Ratchet-wheel.*

28. \( BE \) is a rod, turning on the fixed centre \( B \), to which a reciprocating motion is given by the connecting rod \( C \) of a crank, or by any other means; \( EF \) is a click, jointed to the rod \( BE \) at its extremity, and gives motion to the ratchet-wheel \( A \). At each upward stroke of the rod \( BE \), the click \( EF \), acting upon the saw-like teeth of the ratchet-wheel, causes it to move round one or more teeth; and when the extremity \( F \) of the click is drawn back by the descent of the lever \( BE \), it will slide over the bevelled sides of the teeth without giving any motion to the wheel, so that at every upward stroke of the rod \( C \) the ratchet-wheel will be moved round, and it will remain at rest during every downward stroke of the rod. Thus the reciprocating motion of the connecting rod \( C \) will produce an intermittent circular motion in the axis \( A \).
III. ON WRAPPING CONNECTORS.

29. When the moving force of the machinery is not very great, cords, belts, and other wrapping connectors are most usually employed in transmitting motion from one revolving axis to another.

30. The *endless cord or belt* $\text{A B C D}$, represented in figs. 19 and 20, passes round the wheels $\text{A B}$ and $\text{C D}$, revolving on the parallel axes $\text{R K}$ and $\text{Q F}$, and transmits motion from the axis $\text{Q F}$ to the axis $\text{R K}$, with a constant velocity ratio. In all such cases the motion is entirely maintained by the frictional adhesion of the cord or belt to the surface of the wheel.

When the cord passing round the wheels is *direct*, as in fig. 19, the motions of the wheels take place in the *same direction*, and when the cords cross each other, as in fig. 20, the motions of the wheels take place in *opposite directions*.

If the wheel $\text{C D}$ makes one revolution, then

$$\text{No. revo. A B} = \frac{\text{circum. C D}}{\text{circum. A B}} = \frac{\text{radius C D}}{\text{radius A B}} \quad \text{... (1).}$$

Or putting $R$ and $r$ for the radii of the wheels $\text{C D}$ and $\text{A B}$ respectively, and $q$ and $Q$ for their respective synchronal rotations, then

$$\frac{q}{Q} = \frac{r}{R} \quad \text{... (2).}$$

*Example.*—If the radius of the wheel $\text{C D}$ be 12 inches, and that of $\text{A B}$ 9 inches, what will be the least number of entire revolutions which they must make in the same time?

Here, by eq. (2), we have

$$\frac{q}{Q} = \frac{r}{R} = \frac{12}{9} = \frac{4}{3}.$$
The fraction \( \frac{12}{9} \) reduced to its least terms is \( \frac{4}{3} \); therefore the least number of synchronal rotations are 4 and 3; that is to say, whilst the wheel C D makes three rotations, the wheel A B will make 4.

31. Fig. 21 represents a system of three revolving axes, in which motion is transmitted from one to the other, by means of a series of belts.

The belt being direct in the wheels A and D C, their axes will move in the same direction, but, as the belt crosses in passing from D C to H G, their axes will move in opposite directions.

Here, whilst the axis B makes one rotation, the

No. rotations \( \Lambda = \frac{\text{rad. H G} \times \text{rad. D C}}{\text{rad. E F} \times \text{rad. I K}} \). (1).

Or putting \( r_1 = \text{rad. D C} \), \( r_4 = \text{rad. H G} \), &c., \( r_1 = \text{rad. I K} \), \( r_2 = \text{rad. E F} \), &c., and putting \( q \) and \( q \) for the synchronal rotations of the first and last axes respectively; then

\[ q = \frac{r_1 \times r_2 \times r_3 \times \text{&c.}}{r_1 \times r_2 \times r_3 \times \text{&c.}} \] (2).

Example.—In the mechanism represented in fig. 21, let \( r_1 = 8 \), \( r_2 = 15 \), \( r_3 = 5 \), \( r_4 = 4 \); required the least number of entire rotations performed in the same time by the axes \( \Lambda \) and B.

Here, by eq. (2) we have

\[ \frac{q}{q} = \frac{8 \times 15}{5 \times 4} = \frac{6}{1}; \]

that is, whilst the axis B makes one revolution, the axis \( \Lambda \) will make six.

32. In raising buckets from deep wells or from pits, a continuous cord coils round an axle or a drum wheel, as the case may be, the full bucket being attached to one end of the cord and the empty bucket to the other end; the rotation of the axle coils up the cord to which the full bucket is attached and at the same time uncoils the cord to which the empty one is attached, so that whilst the former is ascending the latter is descending.
Speed Pulleys.

33. Fig. 22 represents an arrangement of speed pulleys; A B and C D are two parallel axes, upon each of which is fixed a series of pulleys, or wheels, adapted for a belt of given length, so that it may be shifted from one pair of wheels to any other pair, say, for example, from the pair a a₁ to the pair c c₁. In order to suit this arrangement, if the belt be crossed, the sum of the diameters of any pair of pulleys must be a constant quantity, that is to say, it must be equal to the sum of the diameters of any other pair. By this contrivance, a change in the velocity ratio of the two axes is produced by simply shifting the belt from one pair to another.

In practice it is customary to make the two groups of pulleys exactly alike, the smallest pulley of one being placed opposite to the largest of the other.

In a group of speed pulleys, let \( s \) = the constant sum of the diameters of the driver and follower, \( d \) = the diameter of the driver, \( d \) = the diameter of the follower, and \( q, q \) the number of their synchronal rotations respectively; then \( \frac{q}{q} \frac{d}{d} \), and

\[
\frac{d}{d} = \frac{q \times s}{q + q} \quad \ldots \ (1)
\]

\[
d = \frac{q \times s}{q + q}, \text{ or more simply,}
\]

\[
= s - d \quad \ldots \ (2).
\]

Example.—Required the diameters of a pair of speed pulleys, when the sum of the diameters is 30 inches, and the driver makes two revolutions, whilst the follower makes 3.

Here \( s = 30 \), \( q = 2 \), and \( q = 3 \); then by eq. (1) and (2) we have

\[
d = \frac{3 \times 30}{5} = 18 \text{ in.}; \text{ and } d = 30 - 18 = 12 \text{ inches.}
\]
If the constant sum of the diameters of a group of 5 pairs of speed pulleys be 12 inches, and the diameters of the pulleys \( a_1, b_1, c_1, d_1, e_1 \), be 10, 8, 6, 4, and 2 inches respectively, then the diameters of the pulleys \( a, b, c, d, e \), will be 2, 4, 6, 8, and 10 inches respectively; and as the strap is shifted from one pair of wheels to another, the relative velocities of the axes \( CD \) and \( AB \) will be as the numbers \( \frac{1}{3}, \frac{1}{2}, 1, 2, \) and 5.

34. It is customary to construct the pairs of speed pulleys so that the rotations of the follower may be increased or decreased in a certain geometric ratio. Thus, if \( r \) be this ratio, then for 5 pairs of speed pulleys we shall have the series of terms \( \frac{1}{r_2}, \frac{1}{r}, l, r, r^2 \), for the different values of \( \frac{Q}{q} \), the ratio of the synchronal rotations of each pair. Or generally if \( n \) be the number of pairs, then \( \frac{1}{r^\frac{(n-3)}{2}}, \ldots, \frac{1}{r}, \frac{1}{r^\frac{(n-1)}{2}} \), will be the different values of \( \frac{Q}{q} \).

In this case, let \( d_1, d_2, \ldots, d^n \) = the diameters of the 1st, 2nd, ..., and \( n \)th pulleys, respectively, on the driving axis; and these symbols, taken in a reverse order, will be the corresponding diameters of the pulleys on the driven axis; then

\[
d_1 = \frac{s}{1 + r^\frac{(n-3)}{2}}, \quad d_2 = \frac{s}{1 + r^\frac{(n-5)}{2}}, \text{ and so on; moreover we have } d = s - d_1, \quad d_{n-1} = s - d_n, \text{ and so on.}
\]

Example.—To find the diameters of a set of 5 pairs of speed pulleys, so that values of \( \frac{Q}{q} \) (the ratio of the synchronal rotations of the different pairs) shall have the common ratio of \( \frac{3}{2} \); the constant sum of the diameters of each pair being 26 inches.

Here \( r = \frac{3}{2}, \quad n = 5, \) and \( S = 26, \) then from the foregoing formulae we find—

\[
d_1 = \frac{26}{1 + \left(\frac{3}{2}\right)^2} = 18; \quad d_2 = \frac{26}{1 + \frac{3}{2}} = 15\frac{1}{2};
\]

\[
d_3 = \frac{26}{1 + \left(\frac{3}{4}\right)^3} = 13; \; \text{and so on.}
\]

But the remaining diameters will be better found as follows:

\[
d_5 = 26 - 18 = 8; \quad d_4 = 26 - 15\frac{1}{2} = 10\frac{1}{2}.
\]

\[\text{PART I.}\]
35. Two plain cones, having their axes parallel, as shown in Fig. 23, will obviously answer the same purpose as the ordinary form of speed pulleys. The slant faces of the cones may be formed by any continuous curve; but with this condition—that the sum of the diameters at every position of the band shall be a constant.

*Guide Pulleys.*

36. By the intervention of guide pulleys the direction of cords may be changed into any other direction. Thus, by means of the guide pulleys $B$ and $C$, the motion of the chord in the direction $CD$ is changed into the direction $AE$.

The cords $DC$ and $CB$ should be in the plane of the pulley $C$; and the chords $CB$ and $BA$ should be in the plane of the pulley $B$.

37. Two guide pulleys, $E$ and $H$, may be employed to transmit motion from the wheel $A$ to the wheel $B$, when the axes of these wheels have any given direction.

Let $EH$ be the line where the planes, passing through the two wheels, intersect each other. In this line assume any two convenient points $E$ and $H$; in the plane of the wheel $A$ draw the tangents $EC$ and $HD$; and in the plane of the wheel $B$ draw the tangents $EF$ and $HG$; then $CEFHD$ will be the path of the endless cord, which will be kept in this path by a guide pulley at $E$, in the plane of $CEF$, and another guide pulley at $H$, in the plane of $DHEG$.

The relative velocities of the axes $A$ and $B$ depend entirely upon the ratio of the radii, $AD$ and $BG$, of the two wheels. See Art. 30.
To prevent Wrapping Connectors from Slipping.

38. The slip of the band on the wheel, when it is not excessive, is in many cases rather an advantage than otherwise; but when motion is to be transmitted from one wheel to another according to some given exact ratio, gearing chains of various forms are employed as the wrapping connectors.

39. In some cases the links of the gearing chain lay hold of pins or teeth formed upon the wheel, as shown in fig. 27. In other cases, the links of the gearing are joined together, some-

![Fig. 26](image)
![Fig. 27](image)

thing like a watch chain, and carry teeth which pass into certain notches made at corresponding distances on the edge of the wheel, as shown in fig. 26.

40. When a belt moves a conical wheel, it always happens that the belt gradually moves towards the broad end of the

![Fig. 28](image)
![Fig. 29](image)
![Fig. 30](image)

wheel: this is owing to the belt being more stretched on that side than it is on the other.

41. This property enables us to construct a wheel so that a belt shall not shift on its edge; this is simply effected by making the edge to swell a little in the middle, as shown in fig. 29.
42. When two rollers have to make only a limited number of revolutions in each direction, the slip of the cord may be prevented by having a cord coiled round each end of the rollers in opposite directions, so that while one cord is coiled on one extremity of the roller, the other cord is uncoiled from the other extremity, as shown in fig. 30.

43. By a similar arrangement of cords on the cylinder \( EF \) (see fig. 31), a reciprocating motion of this cylinder will produce a back and forward motion of the carriage \( AB \).

**Systems of Pulleys.**

44. A system of pulleys must at least contain one movable pulley. When a wheel, forming a part of a system of wheels connected together by cords, has a progressive motion, it materially affects the velocity ratio of the receiver and the operator of the mechanism. There are a great many different systems of pulleys, but they all depend upon the different combinations of movable and fixed pulleys, and the different modes of duplication of a cord.

45. In this system of pulleys there is one movable block and a single continuous cord with three duplications, so that whilst the moving force \( P \) acts by one cord, the movable block with its load is suspended by six cords: if \( W \) ascend one foot, each of these cords will be shortened one foot, and therefore the cord \( P \) will be lengthened six feet; that is to say, the velocity of \( P \) will be six times that of \( W \).

46. In the system of pulleys represented in fig. 33 there are two distinct cords and two movable pulleys \( A \) and \( B \), making two duplications of cord; then if \( A \) ascends one foot, \( B \) must ascend two
feet, and the cord at \( P \) must be lengthened four feet; that is, the velocity of \( P \) will be four times the velocity of \( W \).

Generally if there are \( n \) movable pulleys in such a system, then,

\[
\text{velo. } P = 2^n \times \text{velo. } W.
\]

47. The system of pulleys represented in fig. 34, contains two movable pulleys, one fixed pulley, and two single cords. In this case the velocity ratio of \( P \) to \( W \) is as four to one.

48. Fig. 35 represents a similar system of pulleys, in which the velocity ratio of \( P \) to \( W \) is as five to one.

In all these systems of pulleys the velocity ratios are constant.

49. In the compound wheel and axle, represented in fig. 36, the axle is made of different thicknesses as at \( A \) and \( B \), and a continuous cord coils round these parts in different directions, and passes round the wheel of the movable pulley \( D \). In one revolution of the wheel \( C \) the space moved over by the pulley \( D \) is equal to half the difference of the circumferences of the axles \( A \) and \( B \). Putting \( r_1 \) for the radius of the wheel \( C \), \( r \) for
the radius of the axle $A$, and $r$ for the radius of the axle $B$; then we have for the velocity ratio

$$\frac{\text{velo. } P}{\text{velo. } W} = \frac{2R_1}{R - r}$$

If $R_1 = 10$, $R = 4$, $r = 3\frac{1}{2}$; then $\frac{\text{velo. } P}{\text{velo. } W} = \frac{2 \times 10}{4 - 3\frac{1}{2}} = 80$.

This piece of mechanism belongs to a class which produces what has been called differential motions, their object being to produce a slow and definite motion in a body by the most simple and practicable means.

**TO PRODUCE A VARYING VELOCITY RATIO BY MEANS OF WRAPPING CONNECTORS.**

50. To find the ratio of the angular velocities of two eccentric wheels, moved by a cord wrapping over each.

Let $D$ $C$ be a cord wrapping round the wheels, whose axes of motion are $A$ and $B$; their line $C$ $D$ will be a tangent to the two curves forming the edges of the wheels. On $D$ $C$ produced let fall the perpendiculars $A$ $Q$ and $B$ $K$; then the velocity of the cord, in this position of the wheels, will be equal to the velocity of the point $Q$, and at the same time it will also be equal to the velocity of the point $K$; hence we find,

$$\frac{\text{angular velocity } A\, C}{\text{angular velocity } B\, D} = \frac{B\, K}{A\, Q} \quad \ldots \quad (1);$$

that is to say, the angular velocities are inversely as the perpendiculars let fall upon the cord from the axes of motion.

51. Let $B$ be a movable pulley suspended from the continuous cord $P\, A\, B\, C$, passing over a fixed pulley $A$, and attached to a point $C$ in the same horizontal line with $A$. Let fall $B\, D$ perpendicular to $A\, C$; then $B\, C$ will always be equal to $B\, A$, and $B$ will move in the vertical line $B\, D$. Hence we find—
WRAPPING CONNECTORS.

\[
\frac{\text{velocity } P}{\text{velocity } W} = 2 \times \frac{BD}{BA} \quad (1).
\]

This expression may be put in the following trigonometrical form:

\[
\frac{\text{velocity } P}{\text{velocity } W} = 2 \times \cos PA \times B \quad (2).
\]

52. Fig. 39 represents a simple and ingenious contrivance for communicating a varying velocity to the axis B, by means of an endless band QKQ, passing over an eccentric wheel A; a pulley BK, and a stretching pulley C. The curve of the eccentric wheel, A, must be such as to produce the varying velocity required. The weight W, attached to the stretching pulley C, keeps the band constantly stretched, so that whatever may be the velocity of the cord, upon leaving the eccentric wheel, it communicates the same velocity to the circumference of the pulley BK. From the axis A let fall AQ perpendicular to the cord QK; then by eq. (1), Art. 50, the velocity ratio may be expressed as follows:

\[
\frac{\text{ang. velo. axis } A}{\text{ang. velo. axis } B} = \frac{BK}{AQ}
\]

Let the axis A revolve uniformly, and let the radius, BK, of the pulley be given; then

**The ang. velo. axis B will vary as the perpend. AQ.**
IV. ON WHEEL-WORK PRODUCING MOTION BY ROLLING CONTACT WHEN THE AXES OF MOTION ARE PARALLEL.

53. Two wheels $e$ and $f$, in contact with each other, revolve on the parallel axes $a\ b$ and $c\ d$; now if the wheels are in contact in any one position, they will also be in contact in every other position, and their circumferences will roll upon each other, so that if the driver $f$ revolve on its axis $c\ d$ it will communicate a rotatory motion to the follower $e$ in a contrary direction, by the frictional adhesion of the parts successively brought in contact. The edges of these wheels must have the same velocity, and therefore their angular velocities will be inversely as their radii.

54. In order to render the transfer of motion perfectly exact, the edges of the wheels are formed into teeth, placed at equal distances from each other, so that when one wheel is turned its teeth successively enter into the spaces formed on the edge of the other wheel. Thus, even with slight errors of construction, one wheel cannot escape from the other, which may happen in the case of simple rollers.

The numbers of teeth in the wheels, acting upon each in this manner, are in proportion to their radii. Thus, let the radius of the wheel $A$ be 15 inches, that of $B$ 6 inches, and let $B$ contain 8 teeth; then

$$\text{No. teeth in } A = 8 \times \frac{15}{6} = 20.$$ 

Or generally, if $r$ and $r'$ be put for the radii of the wheels, and $n$ and $n'$ the number of their teeth respectively; then

$$\frac{n}{n'} = \frac{r}{r'} \ldots (1).$$ 

Hence angular velocities, as well as the synchronal rotations, of wheels may be expressed in terms of their numbers of teeth; thus we have—
MOTION BY ROLLING CONTACT.

\[
\frac{\text{ang. velo. } A}{\text{ang. velo. } B} = \frac{n}{N} \quad \ldots (2);
\]

also,

\[
\frac{\text{synchronal rotation } A}{\text{synchronal rotation } B} \quad \text{or} \quad \frac{Q}{q} = \frac{n}{N} \quad \ldots (3).
\]

Example.—Required the least number of teeth in the wheels \( A \) and \( B \), so that \( B \) shall make 105 revolutions per min. and \( A \) only 40.

Here by eq. (3), \[ \frac{n}{N} = \frac{40}{105} = \frac{8}{21} ; \]

that is, \( B \) will contain 8 teeth and \( A \) 21 teeth.

The form which must be given to the teeth of wheels, so as to maintain a perfect rolling contact, will be explained in another part of this work.

55. If the wheel \( A \) be the \textit{driver} then \( B \) will be called the \textit{follower}. Wheels acting in this manner are sometimes called \textit{spur wheels}. Small-toothed wheels are called \textit{pinions}; thus \( B \) may be called a pinion in relation to \( A \).

56. Toothed wheels are said to be in gear when their teeth are engaged together, and they are said to be out of gear when they are separated.

57. In the train of wheels represented in fig. 42, let \( N_1, N_2, N_3, \ldots \), \&c., be the number of teeth in the \textit{driving} wheels, and \( n_1, n_2, n_3, \ldots \), \&c., the number in the \textit{driven} wheels; \( q_1 \) = the no. of rotations of the first axis, \( q_2 \) = the no. of the second axis, and so on, performed in the same time; then

\[
\frac{q_{m+1}}{q_1} = \frac{N_1 \cdot N_2 \cdot N_3 \cdot \ldots \cdot N_m}{n_1 \cdot n_2 \cdot n_3 \cdot \ldots \cdot n_m} \quad \ldots (1).
\]

This equality may be expressed in language as follows:—The ratio of the synchronal rotations of the last and first axes is equal to the continued product of the number of teeth in the driving wheels divided by the continued product of the number of teeth in the driven wheels.
Similarly we have—

\[
\frac{q_m \cdot \text{equals} \times \frac{q_2}{q_1} \times \frac{q_3}{q_2} \times \ldots \times \frac{q_{m+1}}{q_m} \ldots (2),
\]

which may be expressed in language as follows:—The ratio of the synchronal rotation of the first and last axes is equal to the product of the separate synchronal ratios of the successive pairs of axes.

The number of axes in this combination is always one more than the number of pairs of wheels.

It is evident from eq. (1), that the drivers and followers may be placed in any order in a train of wheel-work without changing the velocity ratios of the first and last axes.

Example.—Let the number of pairs of drivers and followers be 3, that is, let \( m = 3 \), \( n_1 = 16 \), \( n_2 = 15 \), \( n_3 = 14 \), \( n_4 = 7 \), \( n_5 = 6 \), \( n_6 = 5 \); required the least number of synchronal rotations of the first and last axes in the train of wheels.

Here by eq. (1) we have—

\[
\frac{q_4}{q_1} = \frac{16 \times 15 \times 14}{7 \times 6 \times 5} = \frac{16}{1};
\]

that is, whilst the first axis makes one revolution, the last will make sixteen.

58. If the number of teeth in a driving wheel be some exact multiple of the number of teeth in the follower, then the same teeth will come into contact in every revolution of the driver. Thus, if the driver contains 30 teeth and the follower 6, then the same teeth will come into contact at every revolution of the driver. This arrangement of teeth is preferred by the clock and watch maker; but the millwright would add one tooth, called the Hunting Cos, to the large wheel; that is, he would have 31 teeth in the driver and 6 in the follower, because 31 and 6, being prime to each other, and at the same time nearly in the same ratio as 30 and 6, the same pair of teeth would not come again into contact until the large wheel had made 6 revolutions and the small one 31.

59. Eq. (3), Art. 53, enables us readily to find the number of revolutions which the wheels must make in order that the same teeth may come again into contact with each other; for it is only
necessary to reduce the fraction \( \frac{n_2}{N} \) to its least terms, and the
denominator of this reduced fraction will give the number of revo-
lutions of the driving wheel as required. Thus, let \( n = 144 \), and
\( n = 54 \), then \( \frac{Q}{q} = \frac{54}{14} = \frac{3}{8} \); that is, the driver must make 3
complete revolutions, or the follower 8, before the same teeth
can again come into contact.

60. In a combination of wheels, whose motions are expressed
by the equality \( \frac{Q_2}{Q_1} = \frac{N_1 \cdot N_2}{n_1 \cdot n_2} \), an indefinite number of values
may be assigned to the numbers of teeth, which shall produce a
given synchronal ratio of the first and last axes; but if \( n_1 \) and \( n_2 \)
be given, and \( n_1 \) and \( n_2 \) be comprised within certain given limits,
then a limited number of values may be found for \( n_1 \) and \( n_2 \).

Thus, for example, let \( \frac{Q_2}{Q_1} = 60 \), \( n_1 = n_2 = 8 \), and the values
of \( n_1 \) and \( n_2 \) not to exceed 100 nor to be less than 40.
Here we have—
\[
\frac{N_1 \cdot N_2}{8 \times 8} = 60;
\]
\[
\therefore N_1 \cdot N_2 = 60 \times 64;
\]
hence \( n_1 \) may be 60 and \( n_2 \) may be 64; but in order to deter-
mine all the combinations, we must put the product, \( 60 \times 64 \),
into prime factors, and then distribute these factors into different
groups answering to the limiting values of \( n_1 \) and \( n_2 \).

Here, \( 60 \times 64 = 2^8 \times 3 \times 5 \); hence we have—
1st combination, \( (2^4 \times 3) \times (2^4 \times 5) = 48 \times 80 \);
2nd combination, \( (2^5 \times 3) \times (2^3 \times 5) = 96 \times 40 \);
3rd combination, \( 2^6 \times (2^2 \times 3 \times 5) = 64 \times 60 \).

61. When all the drivers contain the same number of teeth,
and also the followers, then eq. (1), Art. 57, becomes
\[
\frac{Q_m + 1}{Q_1} = \left(\frac{N_1}{n_1}\right)^m \ldots (1).
\]
By means of this formula we may readily determine the least
number of axes requisite for producing a given synchronal ratio of rotation between the first and last axes, when the number of teeth in the drivers cannot exceed \( n_1 \) and the number in the followers cannot be less than \( n_1 \).

Find \( m \), in eq. (1), equal to the highest whole number, which does not make the right member greater than the left; then the least number of axes will be \( m + 2 \). But if \( m \), a whole number, can be found so as to make the right-hand member exactly equal to the left, then, in this case, the least number of axes will be \( m + 1 \).

Example.—Required the least number of axes in a train of wheels which shall cause the last axis to revolve 180 times as fast as the first axis, allowing that none of the drivers can contain more than 54 teeth, and none of the followers less than 9.

Here we must find the greatest whole number for \( m \), so that

\[
\left( \frac{54}{9} \right)^m \text{ or } (6)^m
\]

shall not exceed 180. This value of \( m \) is obviously 2; and the least number of axes will be 4.

**Idle Wheels.**

62. The wheel \( c \), placed between two other wheels, \( a \) and \( b \), does not affect the velocity ratio of these wheels; and hence the wheel \( c \) is called an idle wheel. This intermediate wheel, however, causes the wheels \( a \) and \( b \) to revolve in the same direction, whereas, if \( a \) and \( b \) were in contact, they would revolve in opposite directions.

**Annular Wheels.**

63. Fig. 44 represents an annular wheel \( A \), having its teeth cut on the internal edge of the annulus or rim. The toothed wheel \( B \), revolving within the annular wheel \( A \), causes it to revolve in the same direction; whereas two ordinary spur wheels revolve in opposite directions.
MOTION BY ROLLING CONTACT.

Concentric Wheels.

64. When two separate wheels revolve about the same centre of motion they are called concentric wheels. The pinion \( d \) is fixed to the axis \( FE \), whilst the concentric wheel \( c \) is fixed to a tube, or cannon, \( n \), which revolves freely upon the axis \( FE \). The driving wheels, \( a \) and \( b \), fixed to the parallel axis \( HG \), communicate the relative velocities to the axis \( FE \) and to the cannon \( n \).

Wheel-work when the axes are not parallel to each other.

65. When the axes of two wheels are not parallel to each other, motion is generally communicated from the one to the other by bevel wheels or bevel gear. When the axes are perpendicular to each other, the face wheel and lantern and the crown wheel are frequently employed.

Face Wheel and Lantern.

66. In fig. 46, \( f \) represents a face wheel, with its lantern \( l \). Here motion is transmitted from the vertical axis \( AB \) to the horizontal axis \( AC \). The teeth \( f \) on the face of the face wheel are called cogs, which are usually made of iron, whilst the round staves forming the teeth of the lantern, \( L \), are made of hard wood. The axes \( AB \) and \( CD \) should, when produced, intersect in a point.
Crown Wheels.

67. Fig. 47 represents a crown wheel B, with its pinion A, having their axes at right angles to each other. The teeth of the crown wheel are cut on the edge of a hoop, the plane of which is at right angles to its axis, and the pinion is thicker than wheels are commonly made.

Case I. To construct Bevel Wheels or Bevel Gear when the axes are in the same plane.

68. Let AC and AB be two axes of rotation in the same plane, and cutting each other in the point A. On these axes two right cones, ADF and ADE, may be formed, touching each other in the line AHD; and also two right frusta, DFGH and DKEF, of these cones may be formed.

Now, if the frustum DFGH revolve on its axis BA, it will communicate, by rolling contact, a rotatory motion to the frustum DKEF upon its axis CA.

These frusta of cones will obviously perform their rotations in the same time as the ordinary spur wheels previously described.

On the surfaces of these frusta a series of equidistant teeth are cut, directed to the apex A of the cones, so that a straight line passing through the apex to the outline of the teeth upon the bases DF and DE of the frusta shall touch the teeth in every part, as shown in the diagram.

Wheels cut in this manner are called bevel gear.

Two wheels of this construction will always transfer motion, with a constant velocity ratio, from one axis to the other, provided these axes meet each other in a point, which point being always made the apex of the frusta forming the bevel of the wheels.

69. General Problem.—Given the radii of two bevel wheels, and the position of their axes, to construct the frusta forming the wheels, the two axes being in the same plane.
Let \(AB\) and \(AC\) be the position of the axes cutting each other in \(A\). Draw \(IJ\) parallel to \(AB\) at a distance equal to the radius of the wheel on the axis \(AB\); and draw \(ML\) parallel to \(AC\), at a distance equal to the radius of the wheel on the axis \(AC\), cutting the line \(IJ\) in the point \(D\). From the point \(D\), draw \(DBF\) perpendicular to \(AB\), and \(DCE\) perpendicular to \(AC\). Take \(BF\) equal to \(BD\), and \(CE\) equal to \(CD\). Join \(AE\), \(AD\), and \(AF\). At a distance equal to the thickness of the wheel, draw \(HG\) parallel to \(DF\), cutting \(AD\) in \(H\); and through \(H\), draw \(HK\) parallel to \(DE\). Then \(DFGH\) and \(DHKE\) will be the frusta required.

**Case II. To construct Bevel Gear when the axes are not in the same plane.**

70. This is usually done by introducing an intermediate wheel with two frusta formed upon it, one frustum rolling in contact with the driving wheel, and the other frustum in contact with the driven wheel.

71. Let \(AB\) and \(CD\) be the direction of the given axes; take \(AD\) as a third axis, meeting the axes \(AB\) and \(CD\) at any convenient points, \(A\) and \(D\); then \(A\) will be the vertex of two rolling frusta of cones \(G\) and \(H\), and \(D\) will be the vertex of two other rolling frusta of cones \(I\) and \(K\). Whilst the intermediate axis, with its two frusta of cones, revolves, the teeth of the frustum \(H\) will have a rolling contact with the teeth of the frustum \(G\), and at the same time the teeth of frustum \(I\) will have a rolling contact with the teeth of the frustum \(K\); and thus motion will be transmitted from the axis \(AB\) to the axis \(CD\) with a constant velocity ratio.
PRINCIPLES OF MECHANISM.

Let \( q_1 \) and \( q_3 \) be the number of rotations performed by the axes \( AB \) and \( CD \) respectively in the same time; \( n_1 \) = the number of teeth in the bevel wheel \( G \); \( n_2 \) = the number in the edge \( I \); \( n_3 \) = the number in the edge \( K \); then,

\[
\frac{q_3}{q_1} = \frac{n_1 \cdot n_2}{n_1 \cdot n_3} \quad (1),
\]

which is similar to the expression given in eq. (1), Art. 57. When \( n_1 = n_2 \), then this equality becomes,

\[
\frac{q_3}{q_1} = \frac{n_1}{n_3} \quad (2).
\]

In this case the intermediate bevel wheel, \( IH \), may be regarded as an idle wheel.

VARIABLE MOTIONS PRODUCED BY WHEEL-WORK HAVING ROLLING CONTACT.

72. Two curved wheels, \( EP \) and \( FP \), having rolling contact, revolve on the axes \( A \) and \( B \). In order that these wheels may roll on each other without slipping, or without producing any strain upon the axes \( A \) and \( B \), these axes must always be in the line of contact \( APB \), and if the curve \( EB \) on the one wheel be equal to the curve \( FP \) on the other wheel, the sum of the lines \( AE \) and \( BF \) must always be equal to \( AB \), the distance between the centres of motion. Various curves may be constructed having this property. For example, two equal ellipses, \( EP \) and \( FP \), revolving on their foci, \( A \) and \( B \), and having \( AE \) and \( BF \) in the line of their major axes, will have a perfect rolling contact. Two equal logarithmic spirals have also the same property.

Let \( DPC \) be the common tangent to the point of contact \( P \); from \( A \) and \( B \) let fall \( AC \) and \( BD \) perpendicular to \( DPC \); then,

\[
\text{angular velocity} \frac{AP}{BP} = \frac{BD}{AC} \quad \text{or} \quad \frac{BP}{AP} \quad (1).
\]

This result may be expressed in language as follows:---The
angular velocities of the wheels are inversely as the perpendiculars let fall upon the common tangent from the centres of motion.


Fig. 52.

Fig. 53.

73. The form of wheels represented in fig. 52 is used in silk-mills and in the Cometarium. The curves may be indefinitely varied, but they must always be constructed to answer the conditions explained in Art. 72.

74. Roemer's Wheels.—E F and C D are the axes of two conical wheels or bevel wheels K and G, having their vertices turned in opposite directions; the teeth of K are formed like those of the ordinary bevel wheel; but the teeth on G are formed by a series of pins, e k, fixed on the surface of the frustum G. By varying the relative position of these pins any given velocity ratio may be obtained.

75. Various combinations have been invented for producing a varying angular velocity; such as the eccentric crown wheel and broad pinion, the eccentric spur wheel with a shifting intermediate wheel, and so on.

INTERMITTENT AND RECIPROCATING MOTIONS PRODUCED BY WHEEL-WORK HAVING ROLLING CONTACT.

76. The following is an example of an intermittent motion produced by the continuous motion of a toothed wheel:—

A driving wheel A, having sunk teeth on a portion of its edge,
communicates an intermittent motion to the wheel $B$, which has a corresponding number of teeth on a portion of its edge. The portion $D C$ of the wheel $B$, being a plain arc of a circle described from $A$ as centre, allows the plain portion of the wheel $A$ to revolve without any interruption. The wheels are brought into gear by a pin $P$ fixed to the wheel $A$, and a guide-plate $G$ fixed to the wheel $B$.

Now, when $A$ revolves in the direction of the arrow, the plain portion of its edge runs past $D C$ without moving the wheel $B$, and at the same time keeps it from shifting; but when the pin $P$ comes into contact with the guide-plate, the wheel $B$ is moved round, and the teeth $D E$ engage themselves with the teeth on $B$, and thus the wheel $B$ is constrained to make a revolution; it then remains at rest until the pin $P$ again comes round to meet the guide-plate.

77. *The Rack and Pinion.*—By this combination a circular reciprocating motion is changed into a reciprocating rectilinear one. Teeth are cut upon the edge of the straight bars, $B C$ and $D E$, so as to work with the teeth upon the pinion $A$. These toothed bars are called racks, and they are constrained to move in rectilinear paths by guides or rollers. The racks in this combination move in opposite directions.

78. Fig. 55 represents an application of the double rack, for converting a continuous circular motion of a wheel, $A$, into a reciprocating rectilinear motion, given to the frame $B E$.

The teeth on $A$ are formed by pins or staves placed about one quarter round the face of the wheel; these staves act alternately
upon the racks formed on the upper and under sides of the frame. The tooth on each rack which comes first into contact with the stave of the pinion is made longer than the others, in order that the first stave should act obliquely upon it, thereby tending to lessen the shock. In this figure the lower stave is represented as leaving the last rack on the under side, and the upper stave as commencing its action on the elongated tooth of the upper rack.

V. ON SLIDING-PIECES, PRODUCING MOTION BY SLIDING CONTACT.

The Wedge or Movable Inclined Plane.

79. Let $A B C$ be a movable inclined plane or wedge, sliding along the smooth surface $D E$, by a pressure $F$ applied to the end $B C$, and producing a vertical motion in a heavy rod $G F$, resting on the plane $A C$, and constrained to move in a straight path by means of guide rollers. The velocity ratio of $P$ and $P_1$ will be constant, being expressed by the following equality:

$$\frac{\text{velocity } P}{\text{velocity } P_1} = \frac{A B}{B C} \text{ or } \frac{\text{length of the wedge}}{\text{thickness of the wedge}}$$

To transmit motion from an axis $A D$ to another axis $B C$, parallel to it.

80. The axis $A D$ carries an arm $A E$, and a pin $E F$, which enters and slips freely in a slit made in the arm $G B$, attached to the axis $B C$. When the axis $A D$ revolves it communicates a rotation in the same direction to the other axis $B C$, but with a varying velocity ratio, for the pin $F$ continually changes its distance $B F$ from the axis $B C$.

When the distance between the parallel axes is small, and the axis $A D$ revolves uniformly, the angular velocity of the axis $B C$
varies, very nearly, inversely as the distance, \( b \ v \), of the pin from this axis.

**The Eccentric Wheel.**

81. This mechanism is usually employed to give motion to the slide valve of the steam engine. In fig. 59, \( b \) represents the axis of the eccentric wheel; \( c \) the centre of the circle; \( e f k \) a hoop which embraces the eccentric wheel so that the one may revolve freely within the other; \( e f d \) a frame connecting this loop with the extremity \( d \) of the bent lever \( d \ l \ o \), turning on the fixed centre \( l \). Now, when the eccentric wheel revolves in the direction of the arrow shown in the figure, the frame with the pin \( d \) is pushed to the right, and when the lob side of the eccentric has passed the line of centres, \( b \) and \( d \), the frame with the pin \( d \) is drawn to the left, and so on. Thus the continuous rotation of the axis \( b \) produces a reciprocating circular motion in the pin \( d \). The stroke of the pin \( d \) will be equal to twice \( c \ b \), or double the eccentricity of the wheel.

**Cams, Wipers, and Tappets.**

82. Cams are those irregular pieces of mechanism to which a rotatory motion is given for the purpose of producing, by sliding contact, reciprocating motions in rods and levers.

83. In fig. 60, \( b \ c \ d \) represents the camb, turning on its axis \( a \), and giving a reciprocating rectilinear motion to the heavy rod \( b \ f \), which is restrained to move in its rectilinear path by the guide rollers. The rotation of the axis \( a \) being in the direction of the arrow, the rod \( b \ f \) has an upward motion until the extreme point \( b \) of the camb comes in a line with the rod, then the portion \( b \ g \) of the camb allows the rod to fall, by its own weight or by the action of a spring, until the point \( g \) comes in a line with the rod, and so on; thus one revolution of the camb here presented will cause the rod
MOTION BY SLIDING CONTACT.

53

to make three upward and three downward strokes. By varying the curve of the camb any law of motion may be given to the rod.

84. In fig. 61, the pin $E$ of the rod is made to traverse a groove $E G D$, cut in the camb plate, so that the pressure of the camb upon the pin produces the downward stroke of the rod as well as its upward stroke. In this case the rod will only make one upward and one downward stroke in every revolution of the camb plate. The length of the stroke of the rod will be equal to the difference between $A D$ and $A G$, where $D$ is the point in the groove furthest from the centre $A$, and $G$ is the point nearest to it.

85. To find the curve forming the groove of a camb, so that the velocity ratio of the rod and the axis of the camb may be constant.

Let $A$ be the centre of the camb, and $C A B Q$ the direction of the rod. From $A$ as a centre, with any convenient distance $A C$, describe the circle $C E D B N$. On $B A$ take $B a$, equal to the length of the stroke of the rod: divide it into any convenient number of equal parts, say five, in the points $b, c, d, e$; and divide the semicircle $B D E F G$ into the same number of equal parts by the radial lines, $A D, A E, A F$. From $A$ as a centre, with $A b, A c, A d, A e$, as radii, describe circles cutting $A D, A E, \&c.,$ respectively, in the points $g, k, l, m$; then through these points draw the curve $a j k l m c$; and similarly in the semicircle $B N C$ draw the other curve $a n p c$.

All lines drawn through the centre $A$ of this curve are equal; thus $A C = A n = A g p = \&c$. Hence, if the rod had two pins placed at $a$ and $c$, the camb would revolve between them, and
would cause the rod to make a downward as well as an upward stroke. This curve is the spiral of Archimedes.

By dividing the line \( h a \) into parts having a varying ratio to one another, any proposed law of velocity may be given to the rod.

86. In fig. 63, the continuous rotation of the camb \( a n c \), revolving on the axis \( a \), gives an oscillating motion to the rod or lever \( f a \), turning on the centre \( n \). In one revolution of the camb the rod makes a double oscillation in the \( a n \).

\[ \text{Fig. 63.} \quad \text{Fig. 64.} \]

87. *Wipers.*—When the rod is to receive a series of lifts with intervals of rest, the camb is made into the from of projecting teeth, which are commonly called *Wipers* or *Tappets*.

88. In fig. 64, the revolving cylinder \( c \) has five wipers upon its circumference, which give five downward strokes to the hammer \( h \), placed at the extremity of the lever \( a h \), in each revolution of the cylinder.

89. In fig. 65, two tappets, upon the revolving cylinder \( c \),
give two downward strokes to the heavy bar or stamper \( AB \) in each revolution of the cylinder. In this case the bar \( AB \) is constrained to move in a rectilinear path by means of guide rollers.

90. In fig. 66, a single wiper on the cylinder \( C \) gives an intermittent rotation to the ratchet wheel \( A \) with its detent \( D \). At each revolution of \( C \) only one tooth in \( A \) is moved round, so that for the greater portion of the revolution of \( C \) the wheel \( B \) is at rest.

91. In fig. 67, the continuous rotation of three wipers \( a, b, c \), communicates a reciprocating rectilinear motion to the frame \( ABCD \). The wiper \( a \) is engaged with the pallet \( e \), and at the instant of disengagement the wiper \( b \) becomes engaged with the pallet \( g \), and then the frame starts in motion in a direction contrary to that of the arrows; and so on.

The Swash Plate.

92. By this mechanism the continuous rotation of an axis produces a reciprocating rectilinear motion in a rod in the direction of its length.

Here \( CB \) represents the revolving axis, to the top of which is fixed the inclined circular flat plate \( AB \), called the swash plate; \( AD \) the rod to which a reciprocating motion is given in the direction of its length, having a frictional wheel \( A \) at its lower extremity resting on the swash plate. This rod is kept in contact with the plate by its own weight, or, if this be not sufficient, by means of a spring. Now, as the swash plate turns round, the rod \( AF \) is alternately raised and depressed, so that at every revolution of the plate the rod performs an upward and a downward stroke. Supposing the rod, as represented in this figure, to be at the lowest point of its stroke; from \( C \), the centre of motion of the plate, let fall \( CD \) perpendicular to \( AF \); then \( AD \) will be equal to half the stroke of the rod. Moreover, let \( \theta \) be any angle...
moved over by the axis, and let $h$ be the corresponding space moved over by the extremity $A$ of the rod; then

$$h = AD \times (1 - \cos \theta),$$

which gives the position of the rod at any point of the rotation of the plate.

93. There is an almost endless variety of combinations for producing reciprocating motions of this kind by means of sliding contact.

94. In fig. 69, an eccentric revolving pin $e$, sliding or working in the slit of the arm $r s$, gives a reciprocating motion to the rod $p q$ in the direction of its length.

95. In fig. 70, the same effect is produced by the rotation of an eccentric wheel, $a b$, on its axis $a$, within the frame $c d f e$.

**SCREWS.**

96. *Construction of a Helix or Screw.*—Let $A a K$ be a cylinder, and $A D E$ a piece of paper cut in the form of a right-angled triangle, having its height $D E$ equal to the height $A K$ of the cylinder. Now, if this paper be wrapped round the cylinder, the slant edge $A E$ of the paper will trace the helix or screw $A a L b c K$ upon the cylinder. If $A B = B C = C D$ be equal to the circumference of the cylinder, the edge of the paper will form four convolutions, and the perpendiculars
MOTION BY SLIDING CONTACT.

BF = IG = HE will be the distance between the threads of the screw.

97. The pitch of a screw is the distance BF between two successive convolutions. If \( t = BF \), the distance between the threads of the screw, \( r = \) the radius of the cylinder, \( \theta = \) angle BAF; then

\[
t = \frac{2 \pi r}{\tan \theta}
\]

98. We may also conceive the helix of the screw to be formed by the compound motion of a point. Suppose the cylinder to rotate uniformly upon its axis, whilst a point A upon its surface at the same time moves uniformly in the direction of its length; then, with this compound motion, the point A will trace the helix of a screw.

99. Transmission of motion by the screw.—Let c a n c m g be a spiral groove cut upon a cylinder; A B the axis on which it turns; D E a rod parallel to the axis A B, and constrained to move in the direction of its length; e a tooth attached to this rod fitting the groove of the screw. Now, when the wheel c is turned in the direction of the arrow, the tooth with the rod D E will be moved from left to right in the direction of its length; that is, parallel to the axis of the screw.

The velocity ratio of the wheel c and the rod D E will be constant, for we have

\[
\frac{\text{velocity c}}{\text{velocity c d}} = \frac{\text{circum. described by c}}{\text{pitch of the screw}}.
\]

If R be the radius of the wheel c, \( r = \) the radius cylinder D B, \( v = \) velocity circum. c, \( u \) the velocity of the bar D E, and so on as in Art. 97; then the above equality becomes—

\[
\frac{v}{u} = \frac{2 \pi R}{t} \ldots (1); \;
\]

\[
\therefore \frac{v}{u} = \frac{R}{r} \tan \theta \ldots (2); \]

Fig. 72.
and when \( r = r \), then—

\[
\frac{v}{v} = \tan \theta \quad (3);
\]

that is, the velocity ratio is equal to the tangent of the angle which the thread of the screw makes with the sides of the cylinder.

100. It is obvious that the number of teeth in the bar \( \text{D E} \) will not at all alter its motion.

In fig. 73, the screw acts upon a series of teeth upon the rack \( \text{D E} \). This arrangement, called the rack and screw, converts a circular motion into a rectilinear one.

**Solid Screw and Nut.**

101. In general the piece acted upon by the screw has its teeth, or rather its threads, formed in a cavity which embraces the whole circumferences of the screw, and the threads of the one exactly fitting the threads of the other. This modification is shown in fig. 74, where \( \text{N} \) is the hollow screw fitting the threads of the screw \( s \). The solid piece \( s \) is called the male screw, and the hollow piece the female screw or nut.

102. Screws are either left-handed or right-handed, according to the direction of the threads.

103. It is important to observe that the following relations of motion subsist between the solid screw and the nut.

1. When the nut is fixed, the solid screw will have a motion in the direction of its length upon being turned round.

2. If the nut revolves without having any longitudinal motion, the solid screw will have a motion in the direction of its length provided it is incapable of revolving.

3. If the solid screw revolves without having any motion in the direction of its length, the nut will have a longitudinal motion provided it is incapable of revolving.
MOTION BY SLIDING CONTACT.

The first two cases are exemplified in the different forms which are given to the common press, and the last case is exemplified in the construction of the self-acting slide rest of the lathe, and in other kinds of mechanism.

The screw is usually employed for producing very slow uniform motions, and for exerting great pressure through a limited space.

The Common Press.

104. In fig. 75, s s is the solid screw, n the nut, n p the lever, b the lower press-board which is constrained to move in an upward direction by means of the guide-frame.

Case 1.—In this case the nut n revolves, but does not move longitudinally, but the screw s s is incapable of revolving. Hence the press-board b is moved upwards at every revolution of the nut over a space equal to the pitch of the screw, or the distance between the threads; that is,

\[
\frac{\text{velo. } P}{\text{velo. } B} = \frac{\text{circum. described by } P}{\text{distance between the threads}}
\]

Example.—Let the distance between the threads = \( \frac{1}{4} \) in., the length of the lever n p = 2\( \frac{1}{2} \) ft.; required the velocity ratio of the point p and the press-board b.

\[
\frac{\text{velo. } P}{\text{velo. } B} = \frac{2 \times 2\frac{1}{2} \times 12 \times 3.1416}{\frac{1}{4}} = 753.984 ;
\]

that is, the velocity of p is 753.984 times that of b.

Case 2.—In this case n is a perforated cylinder forming part of the solid screw s s, and therefore turns with it on a pivot which works in a socket placed on the under side of the press-board b; the piece k fixed to the frame contains the hollow or female screw; so that the solid screw s s is capable of revolving and of moving longitudinally, whilst the nut k remains absolutely fixed.
Compound Screw.

105. This mechanism consists of two screws A and D, the smaller one D working within the larger one A. The screw A works in a fixed nut or female screw at K, and is capable of revolving and moving in the direction of its length; the small screw D is incapable of revolving, but is capable of moving in the direction of its length. In one revolution of the lever P, the screw A descends a space equal to the distance between its threads, but at the same time the screw D enters the hollow screw formed in A a space equal to the distance between the threads on D, so that the extremity B will only descend a space equal to the difference between the thickness of the threads on A and the thickness of the threads on B; hence we have

\[
\frac{\text{velo. } P}{\text{velo. } B} = \frac{\text{circum. described by } P}{\text{dist. bet. threads on } A - \text{dist. bet. threads on } D}.
\]

If the length of the lever \( P = r \), the pitch of the screw \( A = t \), and the pitch of \( D = t_1 \); then

\[
\frac{\text{velo. } P}{\text{velo. } B} = \frac{2 \pi r}{t - t_1} \quad \text{(1)}.
\]

Example.— Let \( r = 5 \text{ ft.}, t = \frac{1}{2} \text{ in.}, t_1 = \frac{3}{8} \text{ in.} \); then

\[
\frac{\text{velo. } P}{\text{velo. } B} = \frac{2 \times 5 \times 12 \times 3.1416}{\frac{1}{2} - \frac{3}{8}} = 3015.936.
\]

The same velocity ratio might be attained by making the pitch of a single screw A equal to \( t - t_1 \), but the threads, in this case, might be too weak to stand the pressure; hence the advantage of the compound screw.
The Endless Screw.

106. When the threads or teeth of a revolving screw are made to act upon the teeth of a wheel, as in fig. 77, the mechanism is called the endless screw. Here, each rotation of the axis $AB$ of the screw turns round one tooth of the wheel $C$; the pitch of the screw on the axis $AB$ being equal to the pitch of the teeth on the wheel.

If $q$ and $Q$ be the synchronal rotations of the wheels and the screw respectively, and $N$ the number of teeth in the wheel; then

$$\frac{q}{Q} = N \ldots (1).$$

If $N = 40$, then, $\frac{q}{Q} = 40$; that is, for every revolution performed by the wheel the screw will make 40.

If $r, R$ be the respective pitch-radii of the wheel and screw, $\theta$ being, as before, the angle which the thread of the screw makes with its axis; then

$$\frac{q}{Q} = \frac{R}{r} \tan \theta \ldots (2).$$

The Differential Screw.

107. $AD$ is an axis on which are formed two screws, $AB$ and $BC$, whose pitches are different. The screw $AB$ passes through a fixed nut or female screw $E$, whilst $BC$ passes through a nut $N$ which is capable of moving longitudinally, but incapable of revolving from the intervention of the guides.

Let the screw make one turn so as to move the cylinder from
right to left, then the screw $A\,B$ will move through the fixed nut $E\,A$ a space equal to the distance between its threads; but, at the same time, the screw $B\,C$ will move through the nut $N$ a space equal to the thickness of the threads on $B\,C$; so that the nut $N$ will only be moved through a space equal to the difference between the thickness of the threads on $A\,B$ and $B\,C$; that is—

In one revolution of $A$, the space moved over by the nut $\begin{align*} N &= \text{pitch screw } A\,B - \text{pitch screw } B\,C = t - t_1, \text{ where } t \text{ is put for the pitch of the screw } A\,B, \text{ and } t_1 \text{ for that of } B\,C. \end{align*}$

If $t = t_1$, then nut $N$ will remain at rest.

If the screw $A\,B$ be right-handed, and $B\,C$ left-handed, then $t + t_1$ will be the space moved over by the nut $N$ in one revolution of $A$.

The Archimedean Screw Creeper.

108. This machine is used for conveying corn from one part of a corn-mill to another. It consists of a wooden cylindrical trough, $A\,B\,C\,D$, with which revolves a shaft, $E\,F$, having a deep

![Fig. 79.](image)

spiral thread formed upon its surface. The corn is dropped in at one extremity of the trough by a hopper, and by the revolution of the creeper the corn is pushed along towards the other extremity of the trough.

Mechanism for Cutting Screws.

109. $C\,D$ is the cylinder or axis on which the screw is to be cut, revolving with the mandril $D$ of the lathe; $A\,A$ toothed wheel revolving with the axis $C\,D$, and giving motion to the toothed wheel $B$, round its axis $E\,F$, on which is cut the parent
screw; this screw gives a longitudinal motion to the nut \( N \), as in Case 3, carrying the sliding table or saddle upon which is securely clamped the cutting tool \( P \) intended to cut the thread of the screw on the cylinder \( C D \). In the place of the wheels \( A B \), any combination of wheels may be used so as to produce any relative longitudinal velocity to the cutting tool \( P \), and thereby to form a screw of any given pitch on \( C D \) with the same parent screw \( F B \).

Let \( n \) = the no. teeth on the wheel \( A \), \( n_1 \) = the no. teeth on \( B \), \( t \) = the pitch of the screw on \( C D \), \( t_1 \) = the pitch of the screw on \( F B \); then

\[
 t = \frac{n}{n_1} \cdot t_1 \ldots (1),
\]

which expresses the pitch of the screw on \( C D \).

From this equality we get

\[
 \frac{t}{t_1} = \frac{n}{n_1} \ldots (2);
\]

that is to say, the pitches of the screws are in the ratio of the number of teeth on their respective wheels.

If \( n_1 \) and \( t_1 \) be constant, then

\[
 t \propto n;
\]
that is to say, the pitch of the screw on C D varies with the number of teeth on its wheel A.

Let \( k \) and \( k_1 \) be the number of threads per inch on the cylinders C D and F E respectively, then

\[
\frac{1}{k} = t, \quad \text{and} \quad \frac{1}{k_1} = t_1,
\]

and eq. (2) becomes

\[
\frac{k}{k_1} = \frac{n}{n_1} \quad \ldots \quad (3).
\]

Now, let there be an intermediate pinion and wheel, turning on the same axis, placed between A and B; and let the pinion (acted upon by A) contain \( e \) teeth, and the wheel \( e \) teeth; then the velocity ratio of the axis F E will be increased by the ratio \( \frac{e}{e_1} \), and hence eq. (3) becomes

\[
\frac{k}{k_1} = \frac{n}{n_1} \cdot \frac{e}{e_1} \quad \ldots \quad (4).
\]

**Example.**—Let \( n = 30, n_1 = 10, t_1 = \frac{1}{2} \) in.; required \( t \).

Here by eq. (1),

\[
t = \frac{n}{n_1} \cdot t_1 = \frac{30}{10} \times \frac{1}{2} = 1\frac{1}{2} \text{ in.}
\]

To produce a changing reciprocating rectilinear motion by a combination of the camb and screw.

110. E F is a conical shaped camb, turning on the eccentric axis A B, on which is cut the screw K B, working in the fixed nut or hollow screw N; D C a rod resting on the camb, constrained to move in the direction of its length, and to which the varying reciprocating motion is to be given. Here, whilst the camb revolves, it has a continuous motion in the direction of the axis A B, so that the lower extremity C of the rod D C describes a spiral or screw curve upon the cone whose pitch is equal to the pitch of the screw K B. The effect of this is to make C D reciprocate in its path in such a manner that the stroke in one direction is shorter than that in the opposite direction.
To produce a boring motion by a combination of the screw and toothed wheels.

111. Here it is required to produce a rapid rotation combined with a very slow motion in the direction of the axis.

The screw \( \mathbf{AB} \) is cut upon a portion of the revolving axis \( \mathbf{AB} \); this screw passes through a nut \( \mathbf{K} \) capable of revolving with the wheel \( \mathbf{C} \), but incapable of moving in the direction of its axis, as in Case 2, page 59; the wheel \( \mathbf{C} \) is driven by the pinion \( \mathbf{F} \), revolving on the parallel axis \( \mathbf{DC} \); \( \mathbf{E} \) is a long pinion, turning on this axis, and acting on the wheel \( \mathbf{L} \), which transmits a rotatory motion to the screw axis \( \mathbf{AB} \). Now, the rotation of \( \mathbf{CD} \) produces a rotatory motion in the axis \( \mathbf{AB} \), and at the same time causes it to advance, in the direction of its length, with a velocity determined by the following formula.

Let \( q, q_1, q_2 \) be the synchronal rotations of the axis \( \mathbf{CD} \), the nut \( \mathbf{K} \), and wheel \( \mathbf{C} \), and the wheel and axis \( \mathbf{AB} \), respectively; \( N, N_1, n, n_1 \), the number of teeth in the wheels \( \mathbf{F}, \mathbf{G}, \mathbf{E}, \mathbf{L} \), respectively; \( s \) the space moved over by \( \mathbf{AB} \) in the direction of its length; and \( t \) = the pitch of the screw \( \mathbf{AB} \).

Now, \( q, q_1 \) rotations of the nut \( \mathbf{K} \) move the screw \( \mathbf{AB} \) through a space equal to \( q_1 \times t \); but \( q_1 \) rotations of \( \mathbf{L} \) move the screw through a space, in the opposite direction, equal to \( q_1 \times t \); therefore in \( q \) rotations of the axis \( \mathbf{CD} \) the screw \( \mathbf{AB} \) will be moved through a space equal to the difference between \( q \times t \) and \( q_1 \times t \); that is,

\[
\begin{align*}
    s &= (q_1 - q_1) t; \\
\text{but } q_1 &= \frac{N}{N_1}, \text{ and } q_1 = \frac{n}{n_1}; \\
\therefore s &= \left(\frac{n}{n_1} - \frac{N}{N_1}\right) q t \ldots (1).
\end{align*}
\]

Now, the difference \( \frac{n}{n_1} - \frac{N}{N_1} \) may be very small as compared with \( q \), and consequently \( s \) may be made as small as we please as compared with \( q \), which is the condition required for the construction of a boring instrument. The boring tool is placed upon one extremity of the axis \( \mathbf{AB} \).

PART I.
SECTION III.
ON PRIME-MOVERS.

CHAPTER I.
ON THE ACCUMULATION OF WATER AS A SOURCE OF MOTIVE POWER.

The machinery of mills, as a whole, may be generally divided into three classes:—the prime-movers, from which the power is derived for keeping the machinery of the mill in motion; the transmissive machinery or millwork (shafting, gearing, &c.), by which the power obtained through the prime-mover is distributed over the different parts of the mill, so that it may be applied at the most convenient place and at the required velocity; and lastly, the machines, technically so called, by which the special operations of the mill in the preparation of its manufactures are carried out. It will be convenient to treat of these divisions in separate sections and in the order just named.

Prime-movers are those combinations of mechanism which receive motion and force directly from some natural source of power, and convert it into that condition in which it is applicable to the purposes of manufacture. Thus the water-wheel takes from the falling water a part of the work accumulated in it, and imparts it as a rotatory motion to the machinery of the mill; and, similarly in the steam-engine, the heat force of the fuel is converted through the medium of the pressure of the steam into motive power in a condition for producing work or mechanical effect. Also the force of currents in the atmosphere impinging upon the expanded sails of windmills has been in former days extensively employed as a motive power. From these three sources, falling or moving water, the combustion
of coal in the production of steam, and wind, we derive almost exclusively at the present time the motive power necessary for carrying on our immense mining and manufacturing systems.

It is only of late years that in this country the steam-engine has nearly superseded the use of air and water as a prime-mover. Until recently steam has been auxiliary to water; it is now the principal source of power, and waterfalls are of comparatively small value, except in certain districts. So long as water was depended upon, the mills of Great Britain and Ireland were necessarily circumscribed in their operations and diminutive in size; they have now become so colossal that they require steam-engines of much greater power than the largest water-wheels, and there appears to exist no limit to the magnitude and importance to which they may yet attain.

Water-wheels, therefore, are those prime-movers which receive a certain portion of their energy from falling or flowing water, and their power or dynamic effect clearly depends upon the amount of water supplied and the height through which it falls, or its velocity at the point of application. Hence water-wheels are usually placed on the banks of rivers where a large body of water is at hand, and near some considerable natural or artificial fall in the bed of the stream.

A curious and interesting phenomenon occurs in the neighbourhood of Argostoli, and is taken advantage of, as described in Ansted's Ionian Islands, in the following manner:

"At four points on the coast, the sea, at its ordinary level, enters a very narrow creek, or broken rocky channel, and after running somewhat rapidly through this channel and among broken fragments of rock for a short distance, it gradually becomes sucked into the earth and disappears. By conducting the water through an artificial canal for a few yards, and so regulating its course and forcing all the water that enters to pass in a single stream beneath an undershot wheel, power enough is obtained in two cases to drive a mill. Mills have, in fact, been placed there by an enterprising Englishman, and are constantly at work. The stream, after being utilised, is allowed to take to its natural channel, and is lost among the rocks."
'It is common enough to drive a wheel by a current of water going from the land towards the sea; but it is certainly rare, and, as far as I am aware, peculiar to the locality, to find mills driven by a current of sea-water acting quite independently of tide, the water constantly and steadily rushing in over the earth's surface and finally disappearing.

'The general condition of the surface is as follows:—

'The small harbour of Argostoli is enclosed on both sides by the hard, broken, limestone rock so common in the islands. On the east side it rises immediately into hills of moderate elevation; and on the west side, behind the town, there is a plateau, scarcely above the usual level of the water, rising about two or three hundred yards from the shore into a low ridge, which, in fact, by its projection into the gulf, makes the harbour. Between the shore line and this low ridge there is an evident depression of the surface in all that part over which the sea when it enters is sucked in. There is evidently beneath this part an extensive cavernous tract, which may well hold much more water than during any ordinary season or succession of seasons can drain naturally into it, in consequence of the rainfall at the surface.

'But what, it will be asked, becomes of the waters of the sea thus pouring in continually to fill the cavern? Certainly, in time, any cavity must be filled, if it has no natural outlet, and if water is constantly entering it. How, also, can the water run off, if its level in the cavern is below the sea-level? It is not, perhaps, so difficult as may be thought to answer these queries.

'The water that everywhere enters the earth is always circulating. It not only pours down into and amongst all rocks, but is afterwards lifted, and the level of these subterranean stores is greatly elevated by operations going on at the surface, often at a great distance above.

'The cause of this is evaporation, which proceeds incessantly from the surface of all rocks, but especially from limestones. The narrow crevices, common in limestone rocks, act as capillary tubes. When water falls on the surface of such rock, it finds its way down readily, and this seems quite natural; but
when, in hot countries, where there is a long summer season of
great drought, the surface becomes dry and hot, moisture rises
in steam from below; and, as the heat and dryness increase, the
accumulated waters become more and more exhausted. All
this goes on without reference to the actual level of the water-
line within the earth, which may be far beneath the level of
the sea.

' That this is the case in the softer limestone rocks, even when
not cracked, has been proved by actual experiment. That it
takes place to an enormous extent in the limestones of the
eastern Mediterranean is proved, if in no other way, by the
fact that vines planted among bare stones, without soil, obtain
an ample supply of moisture from the earth, and ripen their
fruit to perfection in the hottest and driest seasons. No doubt
the earth and rocks are hot, and appear dry; but so long as
there remains any water below that has passed down during the
rainy season, so long will a part of that water be given back to
the dry and thirsty soil above.

' If, then, as is probably the case, there is so large an evapora-
tion from that part of the surface of the Island of Cephalonia
within range of this district as to keep the water-level of the
year below the sea-level, in spite of the joint supply of rain and
sea-water, it is clear that the water may run in for ever at the
same rate without filling up the space. And this I believe to be
the correct explanation of the phenomenon.

' The influx of water, however, is not small. It amounts, as
far as I could make out, to more than half a million of gallons
per diem for the two mills together. The fall of water from
the sea-level into the cavities, where it disappears, seems to be
little more than a foot or eighteen inches.

' It will be evident that, if the sea-water finds its way into any
large natural cavity from which it is afterwards evaporated, a
deposit of salt must be taking place in this cavity, or in rocks
adjacent or connected with it. Assuming the influx to be at the
rate already mentioned, this may be estimated roughly at about
equivalent to an area of 10 acres or 12 acres of solid matter, 1
foot thick, accumulated each year. It is an interesting question
to consider where this deposit is going on, and whether saline
springs may not thus be fed. There are no known springs in the Island of Cephalonia that present any large quantity of saline matter.’

At the commencement of the present century, when the land was imperfectly drained, the soil and surrounding marshes, having no outlet, retained and stored up the rainfall, and became the great holders or reservoirs by which the waters were impounded, and the flow of our rivers regulated with greater uniformity than at present. Since the introduction of an extended system of drainage the whole character of our rivers has been changed, and now discharge their contents with much greater rapidity and in larger volumes than they were accustomed to do before these improvements were introduced. The result of this has been favourable to the land but injurious to the mills, both as regards uniformity and the loss of power, as nearly one half the supply is carried off by floods and cannot be retained for the use of the mills. In all districts of the country where drainage and an improved system of tillage have come into operation, the effect has been a serious loss to the owners of water-mills, and has driven most of them to the use of steam, either as an auxiliary, or in some instances exclusively as a substitute for water.

In some districts and on some rivers the system of impounding the rainfall on the higher lands has been introduced; and particularly where manufacturing processes are carried on, and a large body of men employed, it is essential to success that there should be no stoppages, and that there should be always at command a uniform power equal to the requirements of the mill. Now, as the quantity of water in rivers varies considerably at different periods of the year and in different conditions of weather, it has been found necessary, in many instances, to impound the water by means of reservoirs placed at the sources or the higher portions of the river, so as to retain the waters of wet seasons, and to part with them again in periods of drought and deficiency. To a small extent this may be effected by weirs thrown across the river, so as to retain the water which comes down at night for the use of the mill during the day. But in many instances large reservoirs of a hundred or more acres in extent, and containing when full several mil-
lion cubic feet of water, have been constructed. In these the drainage from a large extent of country is collected during the rainy seasons, and remains stored for use whenever the supply of water in the river becomes inadequate; in this way damage from floods is prevented on one hand, and the supply for an indefinite period of time is equalised on the other. Among the large works of this kind are the Shaw's waterworks at Greenock, and the Lough Island Reavy or Bann reservoirs in the county of Down in the north-east of Ireland, together with later works of the same kind for the supply of water to the cities of Glasgow and Manchester, Melbourne (Australia), &c.

Reservoirs are best placed in hilly districts, at the bottom of a valley into which the water drains from a considerable extent of country. In selecting a site for reservoirs regard must first be had to the value of the land. They should be placed in retired valleys, where the cost of the land does not bear a high ratio to the cost of construction, and, should there exist a natural lake, it may be converted into a reservoir with greatly increased economy. Regard must also be had to the nature of the site. The reservoir should be restrained as far as possible by the natural rise of the ground around it, in order that as few embankments as possible may be requisite for the retention of the water. Again, the geological structure of the country must be examined, as the quantity of water to be expected to flow from a flat country, well clothed with vegetation, will be very different from that which will pour in torrents down the steep declivities of uncovered mountains. In districts of limestone, abounding in vertical fissures and subterranean cavities, a very much smaller quantity of water will drain off the higher districts than from a non-absorbent formation of primitive rock, or where the beds are horizontal and impervious. The steeper the district and the more rapidly the water is discharged to the reservoir, the less will be lost by evaporation and absorption.

It is necessary, in constructing reservoirs, to obtain some measure of the quantity of water which may be expected to accumulate annually, in order to provide sufficient storage. For this purpose it is most important to determine the area of land draining into the valley chosen for the formation of the
reservoir, and the average annual rainfall of the district, with, if possible, the probable loss or waste arising from the re-evaporation and absorption by vegetation, &c.

To ascertain the drainage area it is sufficient to determine the summit level or watershed, i.e., the ridge surrounding the valley which marks the line at which the streams flow in opposite directions into contiguous valleys. This may be determined by a special survey, with a careful examination of an accurate chart like the Ordnance map, on which the contour of the country, brooks, &c., are plainly marked. The whole of the basin included within the watershed is termed the catchment basin. In the case of the Bann reservoirs it amounts to 3,300 statute acres in extent; in that of the Greenock reservoirs to 5,000 acres; at the Manchester waterworks to 19,000 acres.

Of late years an immense number of experiments have been made on the rainfall in different parts of Europe, and with considerable success in determining the laws of rain distribution. For England the annual average rainfall amounts to about 36 in. in depth over the entire surface, distributed throughout the year as in the following table:

<table>
<thead>
<tr>
<th>Month</th>
<th>Greenwich *</th>
<th>Manchester †</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Average for 64 years in ins.</td>
<td>Greatest fall in one month</td>
</tr>
<tr>
<td>January</td>
<td>1.68</td>
<td>4.83</td>
</tr>
<tr>
<td>February</td>
<td>1.58</td>
<td>3.69</td>
</tr>
<tr>
<td>March</td>
<td>1.61</td>
<td>3.45</td>
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<tr>
<td>April</td>
<td>1.73</td>
<td>4.79</td>
</tr>
<tr>
<td>May</td>
<td>1.96</td>
<td>4.16</td>
</tr>
<tr>
<td>June</td>
<td>1.83</td>
<td>4.26</td>
</tr>
<tr>
<td>July</td>
<td>2.37</td>
<td>6.65</td>
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<td>2.40</td>
<td>4.65</td>
</tr>
<tr>
<td>September</td>
<td>2.40</td>
<td>4.79</td>
</tr>
<tr>
<td>October</td>
<td>2.67</td>
<td>5.37</td>
</tr>
<tr>
<td>November</td>
<td>2.53</td>
<td>4.33</td>
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<td>2.02</td>
<td>4.72</td>
</tr>
<tr>
<td>Mean annual depth</td>
<td>24.781</td>
<td></td>
</tr>
</tbody>
</table>

* J. H. Belville.
† Principally from Dr. Dalton; see Manchester Memoirs.
This would give a mean of 30 inches, but it must be borne in mind that in the lake districts and all along the west coast there is an annual fall of rain greatly exceeding that amount, and in some places in the higher districts in Cumberland the returns have been as high as 180 to 200 inches; from this it will be seen that 36 inches is a fair average for the whole surface of Great Britain.

It is, however, important in the construction of reservoirs to have observations of the rainfall in the district in which they are to be placed. Local causes greatly influence the quantity of rain; thus the average fall in Essex is about 20 in., whilst at Keswick, in Cumberland, it is as much as 67·5 in., and at Seathwaite, in the same county, it averages the enormous quantity of 141·5 in.

The method of determining the rainfall is very simple. A cylindrical vessel, of the form shown in section in fig. 83, is placed on the ground or sunk into it in such a manner that its mouth is about 12 in. above the surface. Sometimes a permanent rod and float is added by means of which the depth of rain received on the funnel and preserved in the vessel is read off at sight; and for ordinary purposes this is probably the best plan. But where the greatest accuracy is requisite it is necessary either to tie down the rod or to remove it altogether after making an observation, as otherwise the rain in driving obliquely impinges upon the rod instead of passing over the funnel, and a slight excess is in this way registered above the true rainfall upon the area of the vessel. It is most accurate, however, to draw off the rain and measure it in a graduated glass tube. By placing two or three of these rain-gauges at different elevations around the site of a proposed reservoir, and examining them at convenient intervals of a week or month, it is easy to estimate the exact quantity of rain which falls upon the catchment basin in the course of one year; which, with certain deductions, is the quantity to be provided for in the reservoir. The precaution of placing the
gauges within 5 in. or a foot of the ground is important, as, in accordance with an ill-understood law, the quantity of rain rapidly decreases even at slight elevations from the ground, and it is also important to place the gauge where no artificial currents of air are created, as by the sloping side of the roof of a house. This subject was fully investigated several years ago by Mr. J. F. Bateman and a committee of the Manchester Philosophical Society. Observations had been made on and near the lines of the Ashton and Peak Forest Canals, about the accuracy of which, from their disagreement, doubts had arisen. The gauges in these observations were placed on the ridging of the roofs of the houses of the various lock-keepers, under the impression that, from the exposure of the position, all the rain which fell must there be caught. New gauges were placed in the same localities, but at the surface of the ground, and the results of these experiments were as follows:

<table>
<thead>
<tr>
<th>Locality</th>
<th>Gauge on roofs</th>
<th>Gauge on ground</th>
<th>Excess per cent. on ground</th>
</tr>
</thead>
<tbody>
<tr>
<td>Near Middleton</td>
<td>18.14</td>
<td>28.8</td>
<td>58.76</td>
</tr>
<tr>
<td>Near Rochdale</td>
<td>20.50</td>
<td>30.3</td>
<td>47.8</td>
</tr>
<tr>
<td>Whitelom Reservoir</td>
<td>22.64</td>
<td>35.1</td>
<td>55.0</td>
</tr>
<tr>
<td>Blackstone Edge</td>
<td>23.46</td>
<td>34.2</td>
<td>45.84</td>
</tr>
<tr>
<td>Blackhouse</td>
<td>24.89</td>
<td>36.9</td>
<td>44.23</td>
</tr>
<tr>
<td>Sowerby Bridge</td>
<td>18.77</td>
<td>23.8</td>
<td>41.92</td>
</tr>
</tbody>
</table>

This enormous difference, amounting to 50 per cent. on the average, fully proves the unfitness of the roofs of houses for registering the rainfall. The upward currents of wind created by the sloping roof appear to have carried the raindrops over the edge of the gauge.

Dr. Heberden found the annual fall of rain at the top of Westminster Abbey to be 12·099 in.; on the top of a house close by of much inferior altitude, 18·139 in.; on the ground, 22·608 in.

Mr. Phillips, at York, found the total fall for three years at an altitude of 213 feet to be 38·972 in.; at 44 feet, 52·169 in.; and on the ground, 65·430 in.

Notwithstanding the explanations of these facts which have
been offered, Sir J. F. W. Herschel has within the last year asserted that the cause is yet to seek. The raindrops certainly appear to increase in size in the moist lower strata of the atmosphere.

Mr. Phillip's explanation has been accepted by some Meteorologists, that this augmentation is caused by the deposition of moisture on the surface of the drop, in consequence of its temperature being lower than that of the moist strata of air through which it passes. But this does not appear to be consistent with the fact, that in the condensation of vapour a large amount of latent heat would be liberated. Mr. Baxendale, who pointed this out, estimates from Professor Phillips's observations that in the condensation of the amount of water which corresponds to the augmentation of the raindrop in a fall of 213 feet sufficient heat would be liberated to raise the temperature of the drop to 434° F.

The quantity of rain which falls in twenty-four hours is about 1 in. at the maximum in average districts in England, although in the remarkably exceptional district in Borrowdale, already alluded to, 6·7 in. have been known to fall in the same period. The western coasts generally receive a larger proportion of water than other districts. Mountainous districts in this country, to an elevation of 2,000 feet, receive a larger proportion of rain than lowlands. According to the late Dr. Miller, there fell in twenty-one months in the lake district:

<table>
<thead>
<tr>
<th>Location</th>
<th>Rainfall (inches)</th>
</tr>
</thead>
<tbody>
<tr>
<td>In the valley, 160 feet above the sea</td>
<td>170·55</td>
</tr>
<tr>
<td>Styhead, 1,290</td>
<td>185·74</td>
</tr>
<tr>
<td>Seatoller, 1,394</td>
<td>180·38</td>
</tr>
<tr>
<td>Sparkling Tarn, 1,900</td>
<td>207·91</td>
</tr>
<tr>
<td>Great Gable, 2,925</td>
<td>136·98</td>
</tr>
<tr>
<td>Seawfall, 3,166</td>
<td>128·15</td>
</tr>
</tbody>
</table>

Mr. Bateman's observations agree with these results in proving the increase of rainfall corresponding to increased elevation,*

* The increase of rainfall in passing from the valley to the mountain must be carefully distinguished from the decrease as we ascend upward into the atmosphere, as shown in Mr. Phillips's observations.
as shown by the following figures, representing the rainfall near Glossop in one year:

<table>
<thead>
<tr>
<th>Location Description</th>
<th>Yearly Rainfall</th>
<th>inches</th>
</tr>
</thead>
<tbody>
<tr>
<td>Western foot of hills, 500 feet above the sea</td>
<td>45.0</td>
<td></td>
</tr>
<tr>
<td>&quot; edge of table-land, 1,600 &quot;</td>
<td>67.8</td>
<td></td>
</tr>
<tr>
<td>Easterly edge of Kinder scout, 1,600 &quot;</td>
<td>77.45</td>
<td></td>
</tr>
<tr>
<td>&quot; foot of hills &quot;</td>
<td>40.85</td>
<td></td>
</tr>
</tbody>
</table>

After having determined from these considerations the quantity of water annually falling on the drainage district of a proposed reservoir, it is necessary in the next place to ascertain the probable loss from evaporation and other causes during the transmission to the reservoir. The numerous experiments on evaporation made upon small surfaces of water and of earth may be dismissed as having afforded too inconsistent results to be of any practical value.* Dr. Dalton’s experiments are accurate and valuable as far as they go, but they are deficient in points of application to practical investigations. The area from which evaporation takes place is identical neither with the area of the catchment basin nor with the reservoir surface; but is a variable quantity, depending on the season, the climate, and the locality. It appears to me that the evaporation from a surface of water in low flat land charged with moisture, or a level vegetated surface, is very different from the evaporation in mountainous districts where there are precipitous descents to the brooks. In the former case the waters are retained and remain for weeks more or less exposed to the solar rays and the drying influences of wind. In the latter the rain pours in torrents down the barren hill-sides, and is launched into the valley where the principal evaporation takes place upon a very limited area of surface.

So also in tropical countries; the evaporation from a surface of water is greater than the rainfall upon the same surface, but then the rain falls in torrents, and is rapidly carried away to its

* Dr. Dalton gives the annual evaporation from a surface of water as 25.158 inches; Dr. Dobson, 36.78 inches; Dr. Thomson, 32 inches. The above views in regard to these experiments I expressed in a report on the Bann reservoirs in 1836. Mr. Conybeare gives the evaporation from a surface of water at Greenwich Observatory 8 feet, at Bombay 8 feet, and at Calcutta 15 feet per annum.
natural or artificial reservoirs, and then the evaporation takes place from a very small area of surface.

Since the establishment of reservoirs and the carrying out of large drainage operations, opportunities of estimating the relation of the rainfall to the discharge by rivers have been generally available, and several important experiments have been made in this way. The method of arriving at results is to ascertain the rainfall over a catchment basin the area of which is known. The whole of the water discharged by brooks, &c., is then conveyed over a rectangular weir or waste-board, and the mean velocity of the current and its breadth and depth determined by observations made once or twice every day. The comparison of the amount of water discharged with the total fall will afford the data for ascertaining the amount of evaporation.

Observations of this kind were made by Mr. Bateman with great care in the years 1845, 1846, 1847, with reference to the construction of reservoirs for the supply of Manchester with water, from the Derbyshire hills beyond Staleybridge and Mottram. Gauges were placed at the bottom of the Swineshaw valley (through which flows a tributary of the Tame) and near the summit of Windyate edge, and for some time a gauge was placed midway between these places. Similar gauges were placed in Longendale valley, and the stream in each was measured two or three times a day. From these observations the following table is compiled:

<table>
<thead>
<tr>
<th>Locality</th>
<th>Year</th>
<th>Mean rain</th>
<th>Mean discharge</th>
<th>Waste or loss by evaporation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Swineshaw Brook</td>
<td>1845</td>
<td>59·8*</td>
<td>40·70</td>
<td>19·10</td>
</tr>
<tr>
<td></td>
<td>1846</td>
<td>42·6</td>
<td>33·24</td>
<td>9·36</td>
</tr>
<tr>
<td></td>
<td>1847</td>
<td>49·3</td>
<td>37·10</td>
<td>12·20</td>
</tr>
<tr>
<td>Longendale Valley</td>
<td>1847</td>
<td>55·2</td>
<td>49·46</td>
<td>5·74</td>
</tr>
</tbody>
</table>

The first was a yet year, the second one of the dryest on record, the third an average year.

By uniting the observations at the Swineshaw and the Longendale valleys, we get the following general table of the monthly fall and flow for three years:

<table>
<thead>
<tr>
<th>Month</th>
<th>Rain (in.)</th>
<th>Discharge (in.)</th>
<th>Difference (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>January</td>
<td>2.36</td>
<td>2.85</td>
<td>-0.49</td>
</tr>
<tr>
<td>February</td>
<td>4.30</td>
<td>4.10</td>
<td>+0.20</td>
</tr>
<tr>
<td>March</td>
<td>1.70</td>
<td>1.30</td>
<td>+0.40</td>
</tr>
<tr>
<td>April</td>
<td>5.22</td>
<td>4.25</td>
<td>+1.07</td>
</tr>
<tr>
<td>May</td>
<td>6.48</td>
<td>4.75</td>
<td>+1.73</td>
</tr>
<tr>
<td>June</td>
<td>3.40</td>
<td>1.65</td>
<td>+1.75</td>
</tr>
<tr>
<td>July</td>
<td>1.52</td>
<td>0.99</td>
<td>+0.53</td>
</tr>
<tr>
<td>August</td>
<td>4.32</td>
<td>2.24</td>
<td>+2.08</td>
</tr>
<tr>
<td>September</td>
<td>7.38</td>
<td>5.12</td>
<td>+2.26</td>
</tr>
<tr>
<td>October</td>
<td>4.66</td>
<td>5.27</td>
<td>-0.61</td>
</tr>
<tr>
<td>November</td>
<td>8.48</td>
<td>6.25</td>
<td>-2.23</td>
</tr>
<tr>
<td>December</td>
<td>6.74</td>
<td>8.55</td>
<td>-1.81</td>
</tr>
</tbody>
</table>

|            | 53.36      | 46.59          | +6.77            |

In the following table I have collected the most reliable results on the relations of discharge, rainfall, and evaporation:

<table>
<thead>
<tr>
<th>District</th>
<th>Year</th>
<th>Area of country drained in acres</th>
<th>Rainfall in inches</th>
<th>Discharge in inches</th>
<th>Differences or loss by evaporation</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bute</td>
<td>1826-7</td>
<td></td>
<td>45.4</td>
<td>23.9</td>
<td>21.5</td>
<td>Dry year, Mr. Thom.</td>
</tr>
<tr>
<td>Greenock</td>
<td>1828</td>
<td></td>
<td>60.0</td>
<td>41.0</td>
<td>19.0</td>
<td>Mr. Thom.</td>
</tr>
<tr>
<td>Gorbals</td>
<td>1852</td>
<td>2,750</td>
<td>60.0</td>
<td>48.0</td>
<td>12.0</td>
<td>Mr. Bateman.</td>
</tr>
<tr>
<td>Swineshaw Brook</td>
<td>1846-7</td>
<td>1,250</td>
<td>50.58</td>
<td>37.01</td>
<td>13.5</td>
<td>Mr. Hawksley</td>
</tr>
<tr>
<td>Rivington Pikes</td>
<td>1847</td>
<td>10,000</td>
<td>56.5</td>
<td>44.0</td>
<td>12.5</td>
<td>Flat country, Mr. Betagh.</td>
</tr>
<tr>
<td>Lough Mask, Ireland</td>
<td>1851-2</td>
<td>70,000</td>
<td>49.34</td>
<td>28.59</td>
<td>20.75</td>
<td></td>
</tr>
</tbody>
</table>

The above table shows a loss of from 12 to 20 in., or an average waste of 16 in., of rainfall arising out of re-evaporation and other causes of absorption.

The storage requisite for equalising the supply of water between dry and wet years should be provided with a due reference to the continuance of drought, and the quantity of water which will flow off the ground: in extreme wet seasons no water should be allowed to run to waste. Experience has shown that
in the regions of comparatively moderate rain in this country the storage to effect this object should vary from 20,000 or 30,000 to 50,000 or 60,000 cubic feet per acre of collecting ground, the smaller quantity being about sufficient for an available rainfall of perhaps 18 in., and the larger for one of about 36 to 40 in.* 80,000 cubic feet per acre of collecting ground are provided at Lough Island Reavy; 60,000 at the Gorbals reservoirs, Glasgow; 49,000 at Rivington Pike, and 34,000 at Manchester; at the last, the whole fall not being impounded.

I proceed, neglecting further details on this subject, which belongs rather to the province of the civil than the mechanical engineer, to give an example of the carrying out of these views, of the utility and importance of reservoirs in districts abounding with waterfalls, and where mills are numerous and depending in whole or in part on a steady and regular supply of water.

In 1836 I was called upon to report upon the best means of regulating the water supply upon the river Bann, which, from its excessive variations of flow, was a source of great inconvenience to the manufacturers on its banks. The river Bann rises among the lofty bare summits of the Mourne mountains, in the north-east of Ireland, where there is a heavy rainfall, and in consequence devastating floods frequently poured down its channel, carrying bridges, embankments, and other obstructions before them. On the other hand, during the summer months the ordinary supply of water was totally inadequate to the demands of the mills; whilst the flourishing state of the linen trade called for an extended application of power in a district where steam was not available as a motive power, unless at great cost. Hence, in co-operation with Mr. Bateman, the ground was surveyed and two reservoirs erected in the upper part of the river, by which these evils were removed, and a continuous and adequate supply of water rendered available.

Lough Island Reavy, the site selected for the principal reservoir, was a natural lake, bounded on the north and south by land of considerable elevation, which, although having a comparatively small extent of drainage (3,300 acres ultimately), was supplied by good feeders, which, united to the surplus waters of the river Muddock, would fill the reservoir at least once or twice a year. The original surface of the Lough, fig. 84, was 92½ acres in extent; on this it was proposed to raise a depth of 35 feet more water, by the aid of embankments, and to draw off at a depth of 40 feet under that height. The area thus enlarged would be 253 statute acres, and the capacity of the reservoir is 287,278,200 cubic feet.

Corbet Lough was the second site, and, although at first abandoned from its proximity to the town of Banbridge, was afterwards adopted. At a small expenditure for embankments, Corbet Lough was raised 18 feet above its summer level; so as to cover 74½ acres, and to have a capacity of 46,783,440 cubic feet of water.

A third site was selected further up amongst the mountains, but at this part the works were never executed.

It is understood that 12 cubic feet of water per second falling one foot will, in its best application on a water-wheel, afford a force equivalent to 33,000 lbs. raised one foot high per minute, or one-horse power. Now, supposing the reservoirs to discharge 40 cubic feet of water per second, the fall from the lowest point of outlet at Lough Island Reavy to the tail water of the lowest mill on the Bann being 350 feet, we have a total force of 1,166 horses available for mill purposes; or in other words, the mill-owners will derive an average advantage of 3·3 horse power for every foot of fall. This, it must be observed, is not a supposed quantity, but the result of certain data taken by calculation from the waters of the Bann. It must be noticed further that this supply of 2,400 cubic feet per minute is not the whole power. The calculations are for one-half, the river supplying the remainder, except in extremely low water, when the demands from the reservoir may be increased to meet the emergency.
WATER AS A SOURCE OF POWER.

From the estimates made at the time, the expenditure to secure this result would be

<table>
<thead>
<tr>
<th></th>
<th>£</th>
<th>s.</th>
<th>d.</th>
</tr>
</thead>
<tbody>
<tr>
<td>For Lough Island Reavy</td>
<td></td>
<td>12,600</td>
<td>0 0</td>
</tr>
<tr>
<td>&quot; Corbet Lough</td>
<td></td>
<td>3,612</td>
<td>0 0</td>
</tr>
</tbody>
</table>

At Lough Island Reavy it was necessary to construct four embankments, marked A, B, C and D, in fig. 84.

<table>
<thead>
<tr>
<th>Section</th>
<th>Cubic Yards</th>
</tr>
</thead>
<tbody>
<tr>
<td>The principal SW. side</td>
<td>137,400</td>
</tr>
<tr>
<td>Small do.</td>
<td>17,400</td>
</tr>
<tr>
<td>&quot; NW. end</td>
<td>5,200</td>
</tr>
<tr>
<td>&quot; E. end</td>
<td>99,781</td>
</tr>
<tr>
<td>Total</td>
<td>259,781</td>
</tr>
</tbody>
</table>

The substratum of the valley being water-tight, the footing for the puddle was easily obtained by sinking a trench into the water-tight stratum, whence the puddle wall was carried up vertically with the bank to the required height. It was 12 feet in width, at 40 feet below the top, diminishing to 8 feet wide at the summit. A layer of peat was brought up on the inside of the puddle, and a similar layer on the face of the slope. Above the peat a layer of three feet of gravel was laid, and on that the stone pitching forming the inner side of the bank. The inner slopes of the embankments were 2½ horizontal to 1 vertical, and 3 horizontal to 1 vertical. The outer slopes 2 horizontal to 1 vertical, and 2½ horizontal to 1 vertical. The discharge pipes, two in number, each 18 in. in diameter, were placed at the bottom of a stone culvert, at the lowest part of the embankment, with suitable discharge valves, &c. The rainfall for the district amounted to from 72 to 74 in. annually, of which at least 48 in. found its way to the reservoirs.

Fig. 84 is a plan of the original disposition of Lough Reavy and its feeders. The original area of the lake is shaded, and its present area is indicated by the dotted line connecting the embankments A, B, C and D. The diversions of roads and new feeders rendered necessary are also indicated.

Fig. 85 represents a section of the embankment of the Belmont reservoir, which will sufficiently explain the arrangement of the culvert and discharge pipe α α, with the top and discharge valves ν ν, in the valve-house τ, which in works of this

PART I.
Map of Lough Island Reavy Reservoir.
kind is always under lock and key. The water entering the pipe through the tunnel \(b\) flows out into the well \(c\), and gauge basin \(d\), where, as it passes over the gauge or dam board \(g\), its quantity may be ascertained. The construction of the regulating discharge valve is shown in figs. 86 and 87. Fig. 86 is an elevation of the valve at the side at which the water flows in, and fig. 87 a cross section. \(a\) is the valve case, closed below and fitted with a bonnet \(b\) at top; the valve \(v\) works up and down in the valve box, against a brass facing \(c\), and is confined by a guard \(d\) behind; the adjustment of the valve is affected by a valve spindle \(f\), of wrought iron, cased in gun metal, so as to slide freely in the stuffing box \(g\), and is worked by a fly-wheel \(h\), and screw above. By means of this fly-wheel the valve may be adjusted to any required opening.

Of late years Mr. Bateman has introduced an ingenious valve admirably adapted for the discharge of reservoirs of great depth, where the amount of pressure upon the valve is an impediment to its employment. To remedy this evil, the valve is divided into three parts; first, the small valve by which about \(\frac{1}{6}\) of the area is opened; secondly, the intermediate valve of about \(\frac{1}{4}\) the total area; lastly, the large valve unclosing the remainder. It will be seen that the small valve is drawn first, and is followed by the second, and ultimately by the largest, after the pressure is removed or partially neutralised.

The pressure of water against the side of an embankment is enormous in most instances, and varies upon any part in the
ratio of its depth below the surface. Let \( h \) = the depth of water in a reservoir; \( A \) = the area in square feet of a vertical section of the embankment of the depth \( h \); then the lateral pressure upon the embankment in a horizontal direction is, in lbs.,

\[
P = \frac{1}{2} h \times 62\frac{1}{2} \times A = 31.25 A \times h,
\]
a cubic foot of water weighing 62\(\frac{1}{2}\) lbs.

Or, generally, the whole pressure of water upon a submerged plane surface is equivalent to the area of the surface, multiplied by the weight per cubic unit of the fluid, and by the head of water measured from the centre of gravity of the submerged surface. That is, for water

\[
P = 62\frac{1}{2} A_1 h_1.
\]

Where \( h_1 \) = the depth of the centre of gravity below the level of the water in feet; \( A_1 \) the area of the surface in feet; \( P \) = the pressure on the surface in lbs.
And the whole pressure in any one direction is equal to the area of a section of the fluid vertical to that direction, multiplied by the weight of a cubic unit of the fluid and by the distance of the centre of gravity of the section from the level of the water.

Putting $l$ = the length $a\; b$
$s$ = the slope $a\; d$; $h$ = the height $a\; f$; $k$ = the breadth $f\; d$, all in feet;
$p$ the centre of gravity of $a\; b\; c\; d$.
Then the distance of the centre of gravity of $a\; b\; c\; d$ from the level of the water, $o\; p$, is equal to $\frac{1}{3}h$; and the distance of the centre of gravity of the plane $a\; b\; e\; f$ from the level of the water is also $\frac{1}{3}h$.

Therefore, the whole pressure upon

$$a\; b\; c\; d = \frac{1}{3} l \times s \times h \times 62.5 = 31.25 l \times s \times h.$$  

The horizontal pressure against the embankment

$$= \frac{1}{3} l \cdot h^2 \times 62.5 = 31.25 l \cdot h^2.$$  

The vertical pressure

$$= l \times k \times h \times 62.5$$  

To the statistics given above of the rainfall and evaporation in this country it will be necessary to add some account of their amount in tropical climates, where the conditions are essentially different. In such climates for three-quarters of the year the rain never falls, and the whole quantity for the annual consumption falls during the remaining quarter.

At the Bombay Water Works constructed by Mr. Conybeare, the annual rainfall is 124 inches, of which $\frac{5}{6}$ are assumed to be available for storage. The area draining into the basin is 3,948 acres, so that the supply is upwards of 6,600,000,000 gallons. The storage capacity of the reservoir is 10,800,000,000 gallons, or 1,733,000,000 cubic feet.  

At the Melbourne Water Works constructed under the direction of Mr. Matthew Bullock Jackson, the area of the reservoir when full is 1,303 acres, greatest depth 25 feet 6 inches, average depth 18 feet, and capacity 6,400,000,000 gallons. The area of the natural Catchwater basin is 4,650 acres, together with

600 acres drained by a watercourse. This area, however, may be increased if a larger supply is necessary. This watercourse at the same time opens a connection with the River Plenty, through which flows the water drained from an extent of 40,000 acres of country. This watercourse is opened during the winter to fill the reservoir from this source. The following table gives the detail of the rainfall and evaporation observed by Mr. Jackson during the construction of the works:

**Table, showing the Amount of Spontaneous Evaporation and Rainfall for Twelve Months ending 31st January 1858.**

<table>
<thead>
<tr>
<th>Months</th>
<th>Melbourne, 94 feet above the level of the sea</th>
<th>Geelong, 96 feet above the level of the sea</th>
<th>Ballarat, 1450 feet above the level of the sea</th>
<th>Spontaneous Evaporation of Melbourne</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>inches</td>
<td>inches</td>
<td>inches</td>
<td>inches</td>
</tr>
<tr>
<td>February</td>
<td>3.98</td>
<td>1.33</td>
<td>2.39</td>
<td>3.75</td>
</tr>
<tr>
<td>March</td>
<td>3.50</td>
<td>3.61</td>
<td>1.98</td>
<td>1.55</td>
</tr>
<tr>
<td>April</td>
<td>0.99</td>
<td>0.73</td>
<td>1.67</td>
<td>1.88</td>
</tr>
<tr>
<td>May</td>
<td>2.00</td>
<td>2.06</td>
<td>1.72</td>
<td>1.88</td>
</tr>
<tr>
<td>June</td>
<td>1.99</td>
<td>1.89</td>
<td>1.58</td>
<td>0.00</td>
</tr>
<tr>
<td>July</td>
<td>1.16</td>
<td>2.39</td>
<td>1.16</td>
<td>0.00</td>
</tr>
<tr>
<td>August</td>
<td>1.69</td>
<td>2.43</td>
<td>1.14</td>
<td>2.42</td>
</tr>
<tr>
<td>September</td>
<td>3.83</td>
<td>3.70</td>
<td>3.19</td>
<td>2.88</td>
</tr>
<tr>
<td>October</td>
<td>4.28</td>
<td>4.70</td>
<td>2.63</td>
<td>4.63</td>
</tr>
<tr>
<td>November</td>
<td>2.12</td>
<td>1.80</td>
<td>3.15</td>
<td>2.27</td>
</tr>
<tr>
<td>December</td>
<td>0.83</td>
<td>1.76</td>
<td>0.33</td>
<td>0.73</td>
</tr>
<tr>
<td>January</td>
<td>0.88</td>
<td>1.07</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>Totals</td>
<td>23.55</td>
<td>27.50</td>
<td>20.34</td>
<td>20.11</td>
</tr>
<tr>
<td></td>
<td>61.46</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

It is to be presumed that the evaporation given above, nearly three times the rainfall, is the evaporation from a surface of water such as that of the reservoir itself. The rain, however, is collected from a surface thirty-five times as great as that of the reservoir when at its maximum height.

*Weirs* or *Dams*, thrown across the beds of rivers, have always been employed in order to raise the head of water in the river bed, and to divert a portion of it for the purposes of the mill. We have now to consider how most economically to secure a sufficient fall, and to protect the dam from the destructive effects of floods.

There is hardly any department of engineering which re-
WATER AS A SOURCE OF POWER.

quires more careful consideration than that of forming barriers to large quantities of moving water; and when the nature of rivers carrying off the drainage from a large area is considered, and the enormous power of suddenly accumulating floods, the nature of the resistance required from a dam may be easily conceived, and when all the care of the engineer has been exercised it nevertheless sometimes occurs that the torrents tear up and destroy in a night the work which was intended to perform the quiet industrial duties of a mill for ages, leaving, in place of the well-turned arch across the stream, only the horns of the abutments and an indistinguishable mass of rubbish mingled with the mountain debris of the flood.

Such is frequently the case with weir constructions, particularly those across the rapids of mountain torrents, and this not unfrequently causes the construction of a temporary dyke of boulder stones capable of withstanding the ordinary action of the river, and easily replaced when floods have caused its partial destruction. This description of weir is carried diagonally across the stream at $a$ (fig. 89), and being considerably longer than its breadth, forces part of the water into the conduit $b$, and passes the remainder over the top in a thin sheet, which does little or no damage to the banks below. In the above description of weir it seldom happens that much fall can be obtained, and they are

therefore adopted where there is a large supply of water employed upon an undershot wheel.
Another description of weir, which is generally employed on moderate-sized rivers, is the V form constructed across the bed of the river, as shown in fig. 90, in plan. The object of adopting this form of weir is to increase its resisting powers, and, by spreading the fall of water over a large surface, to diminish its destructive effects upon the apron below; the descending currents meeting in the angle of the V neutralise their effects on the foundations, and do less injury to the banks on either side. This weir is generally formed of piles (fig. 91), with an open frame of timber, into which are inserted large boulder stones, forming a compact mass of boulder sheeting resting on gravel, and nearly impervious to water. Another weir, preferred to most others where timber is plentiful, is formed into a series of steps (fig. 92), over which the water falls in cascades, which destroys its injurious effect on the foundations; it is composed
of piles placed at right angles with the direction of the stream, and placed in rows properly stayed and covered with planking firmly nailed to the horizontal and vertical timbers. When it is necessary to have the structure watertight, a line of sheet piling is usually driven in, in the line of the weir across the whole breadth of the stream, and these again, supported by foot piles and stays at different distances, form a perfectly tight and very durable weir.

The most perfect weirs, however, are formed of stone, built of solid ashlar, and usually forming part of the segment of a circle across the breadth of the river (fig. 93). These are made

Fig. 93.

1st, with long inclined slopes on either side; 2nd, solid, with nearly perpendicular walls; or 3rd, with a curved apron to break the force of the fall.

Of the first kind we have a good example in the weir constructed by Smeaton at Carron (fig. 94), where \( a, b \), represent

Fig. 94.

two courses of flag stones, breaking joint, and packed with live moss, to prevent the silt being driven through; these are footed upon grooved sheet piling with bearing piles and stringer \( d \), the flags being supported on rubble; at the foot of the dam is another row of sheet piling \( f \), similarly supported and protected.
by a fir plank at top from the action of the water. Over the rubble is placed a row of regular stones, laid endways so as to be perfectly secure from derangements by floods.

The second description of stone weir is a solid ashlar wall, having its convex side to the current (fig. 93) and abutting upon heavy masses of masonry on each side of the stream. Fig. 95 exhibits this weir modified by having a curved apron, so as gradually to convert the vertical fall of the water into a horizontal flow in the direction of the stream.

It will suffice to observe further, that the head of water immediately over the crest is less than the head of water at some distance behind. It is usual to cut a channel, with a sluice gate in one of the wing walls of the weir, to draw off superfluous water, when requisite. The utmost caution is needed, both in observing the conditions of the river and the effects likely to result in times of flood from the increased head of water above the weir. Rapid rising of the waters and sudden changes in the state of the river are too often neglected, with disastrous consequences to works of this kind, just on the eve of completion, or to the lands above the dam in consequence of flooding caused by the obstruction of the dam. In cases where this last danger is apprehended, a self-acting dam has sometimes been employed, consisting of a massive frame of planks carried across the river and attached by hinges to the crest of the dam. This plank is maintained in a vertical position in ordinary conditions of flow by balance weights attached or hung over wheels upon the wing walls, so as to
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retain the maximum desirable head of water. In floods the increased pressure of the overflowing water overcomes the balance weights and throws down the plank into a horizontal position, opening a free passage for the water.

Conduits.—Having thus considered the means of accumulating water power and regulating its supply by means of reservoirs and weirs, we have yet to consider the formation of conduits or lades, as they are called in some places, for the actual discharge of the water upon the water-wheel or other machine by which its power is to be utilised. By the construction of a weir we may have dammed back the water half a mile or a mile, and formed the upper part of the stream into a reserve from which the supply of water can be drawn and two or three feet or more of fall gained; but unless the mill is built close up to the banks of the stream, head courses, canal and tail races have to be cut in order to make the fall available, and these conduits are not unfrequently as difficult of construction and as expensive as the weir. In several large works with which I have been connected, the cost of conduits has extended to many thousands of pounds, as at the Catrine Works in Ayrshire, or the Deanston in Perthshire. In the former case a large tunnel, with retaining walls and embankments several hundred yards in extent, had to be constructed, and at the latter a wide and spacious canal, nearly a mile long, before the water reached the mills where it was turned to account in driving the different machines for spinning, weaving, &c.

The large expenditure in these and similar works operates much against the economy of water power, and when the extremes of floods and droughts, including the interest of capital sunk, is considered, it will be seen that it frequently happens that steam power might have been purchased and maintained at as economical a rate. Let us take, for example, the Catrine Mills, at which there is a fall at forty-eight feet, and a power of 200 horses, nearly constant throughout the year. In this establishment there are two colossal water-wheels, each fifty feet in diameter and twelve feet wide. Now taking the weir, the tunnel, the upper conduit, tail race, &c., arched to a distance of a third of a mile down the river, we may estimate the ultimate cost, approximately, as follows:—
### ON PRIME-MOVERS.

<table>
<thead>
<tr>
<th>Description</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water privileges and land</td>
<td>£4,000</td>
</tr>
<tr>
<td>Cost of weir</td>
<td>£1,000</td>
</tr>
<tr>
<td>Head race, tunnel, and canal</td>
<td>£3,000</td>
</tr>
<tr>
<td>Archways, cisterns, sluices, &amp;c.</td>
<td>£1,000</td>
</tr>
<tr>
<td>Wheelhouse and foundations</td>
<td>£1,500</td>
</tr>
<tr>
<td>Tail race</td>
<td>£1,500</td>
</tr>
<tr>
<td>Water wheels and erection</td>
<td>£4,500</td>
</tr>
<tr>
<td>Contingencies</td>
<td>£1,500</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>£18,000</strong></td>
</tr>
</tbody>
</table>

The cost of power independent of mill-work equivalent to an annual rental for interest of capital, repairs, and wear and tear, at 7 per cent., amounting to 1,260l.

This may be contrasted with steam power in a district where coal can be purchased at 7s. per ton, and we have—

<table>
<thead>
<tr>
<th>Description</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cost of engines of 100 nominal horse power</td>
<td>£4,000</td>
</tr>
<tr>
<td>Engine house, foundations</td>
<td>£1,500</td>
</tr>
<tr>
<td>Contingencies</td>
<td>£500</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>£6,000</strong></td>
</tr>
</tbody>
</table>

This at 10 per cent. for interest of capital, repairs, and renewals, will be equivalent to

<table>
<thead>
<tr>
<th>Description</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>An annual rental of</td>
<td>£600</td>
</tr>
<tr>
<td>Add consumption of coal at 4 lbs. per indicated horse power per hour, engineers' wages, &amp;c.</td>
<td>900</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>£1,500</strong></td>
</tr>
</tbody>
</table>

Against the higher rental in the case of steam, must be set the cost of transit of the raw material and products of the mill, which must be transported to and from the market at a greatly increased cost, as in the case of the Catrine Works, with the risk of stoppage also from want of water in long-continued drought or frost. It is true that labour may be had cheaper in the country than in towns, but that is no counterpoise for want of skill amongst the operatives, or for the loss of those numerous conveniences which are to be obtained in the great foci of labour where the whole powers and energy of the country have been concentrated.

On the whole, there appears (in the present improved state of the steam engine and the price of coal) to be no advantage in
WATER AS A SOURCE OF POWER.

this country in water power as applied to manufactures, and it is only at out districts, and where the mere wants of the inhabitants have to be supplied, that water mills can be used with profit. Before the introduction of the steam engine, water power was invaluable, but we now see that it cannot at all times be depended upon, and that in most cases where a large amount of power is required, the chief source from which it must be derived is steam.
CHAPTER II.

ON THE FLOW AND DISCHARGE OF WATER, AND THE ESTIMATION
OF WATER POWER.

In the present chapter it is proposed to enter only so far into
those questions of Hydrodynamics which relate to the measure-
ment of the discharge of water, and the estimation of water
power, as it is necessary they should be understood by the prac-
tical millwright, in order that he may be at no loss in comparing
the efficiency of various forms of water machinery, calculating
their power, and proportioning them to their position and their
work. For minute and accurate mathematical investigations,
the reader is referred to special treatises on hydrodynamics, in
which the subject is treated from another point of view.

From the nature of a non-elastic fluid such as water, in which
the particles are free to move over one another without friction,
the following relations hold between pressure, velocity and dis-
charge.

1st. The pressure \( p \) upon a unit of area at the depth \( h \) be-
neath a fluid surface is equal to the weight of a column of the
liquid \( h \) units high; that is, if \( w \) be the weight of a unit of
volume,

\[
p = w \, h \ldots (1).
\]

And therefore the pressure on a horizontal surface of \( a \) units
area = \( w \, h \, a \).

2nd. The velocity with which a fluid flows from a small orifice
at the depth \( h \) beneath the surface, is the same as the velocity
it would have acquired in falling freely the same distance under
the action of gravity, if we neglect those causes of retardation
to be considered presently. If we take \( v \) = mean velocity of
the effluent water; \( h \) = mean depth of orifice beneath the sur-
face, or, in other words, the head of fluid; \( g = 32.1908 \) = the
velocity generated in a falling body in one second; then by the laws of accelerating motion,

\[ v = \sqrt{2 gh}, \ldots (2) \]

that is, the theoretical velocity of effluent water is equal to the square root of 64·38 times the mean head; understanding by mean head the head measured from the centre of the orifice.

Thus we have in the following table the theoretical velocity at various heads.

**Table I.—Theoretical Velocity of Effluent Water.**

<table>
<thead>
<tr>
<th>Head (ft)</th>
<th>Velocity per second (ft)</th>
<th>Head (ft)</th>
<th>Velocity per second (ft)</th>
<th>Head (ft)</th>
<th>Velocity per second (ft)</th>
<th>Head (ft)</th>
<th>Velocity per second (ft)</th>
<th>Head (ft)</th>
<th>Velocity per second (ft)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>8·02</td>
<td>11</td>
<td>26·6</td>
<td>21</td>
<td>36·8</td>
<td>31</td>
<td>44·6</td>
<td>41</td>
<td>51·3</td>
</tr>
<tr>
<td>2</td>
<td>11·34</td>
<td>12</td>
<td>27·8</td>
<td>22</td>
<td>37·6</td>
<td>32</td>
<td>45·4</td>
<td>42</td>
<td>52·0</td>
</tr>
<tr>
<td>3</td>
<td>13·90</td>
<td>13</td>
<td>28·9</td>
<td>23</td>
<td>38·5</td>
<td>33</td>
<td>46·1</td>
<td>43</td>
<td>52·6</td>
</tr>
<tr>
<td>4</td>
<td>16·04</td>
<td>14</td>
<td>30·0</td>
<td>24</td>
<td>39·3</td>
<td>34</td>
<td>48·8</td>
<td>44</td>
<td>53·2</td>
</tr>
<tr>
<td>5</td>
<td>17·93</td>
<td>15</td>
<td>31·1</td>
<td>25</td>
<td>40·1</td>
<td>35</td>
<td>47·4</td>
<td>45</td>
<td>53·8</td>
</tr>
<tr>
<td>6</td>
<td>19·64</td>
<td>16</td>
<td>32·1</td>
<td>26</td>
<td>40·9</td>
<td>36</td>
<td>48·1</td>
<td>46</td>
<td>54·4</td>
</tr>
<tr>
<td>7</td>
<td>21·21</td>
<td>17</td>
<td>33·1</td>
<td>27</td>
<td>41·7</td>
<td>37</td>
<td>48·8</td>
<td>47</td>
<td>55·0</td>
</tr>
<tr>
<td>8</td>
<td>22·68</td>
<td>18</td>
<td>34·0</td>
<td>28</td>
<td>42·4</td>
<td>38</td>
<td>49·4</td>
<td>48</td>
<td>55·6</td>
</tr>
<tr>
<td>9</td>
<td>24·09</td>
<td>19</td>
<td>34·9</td>
<td>29</td>
<td>43·2</td>
<td>39</td>
<td>50·1</td>
<td>49</td>
<td>56·1</td>
</tr>
<tr>
<td>10</td>
<td>25·38</td>
<td>20</td>
<td>35·9</td>
<td>30</td>
<td>43·9</td>
<td>40</td>
<td>50·7</td>
<td>50</td>
<td>56·7</td>
</tr>
</tbody>
</table>

3rd. The *quantity* of water which issues from an orifice at a depth \( h \) beneath the surface of a fluid is equal to the area of the orifice multiplied by the velocity of the effluent water, that is, neglecting the diminution from the *vēnā contractā* to be mentioned shortly.

Let \( q = \) units of volume discharged per second

\( a = \) area of orifice

\( v = \) velocity of effluent water

\( q = a v = a \sqrt{2 gh} \ldots (3) \).

And in \( t \) seconds \( q t = a v t \) will be discharged.

Where \( q \) is called the *theoretical discharge*, and is found by multiplying the area of the orifice in feet by the velocity of the effluent water in feet per second, found as above.

4th. If the orifice instead of opening freely into the air, as supposed above, opens into another reservoir of fluid, we must substitute in the above equations the difference of level of fluid

\* Or in feet \( v = 8·03 \sqrt{h} \).
in the two reservoirs for the head above the centre of the orifice. Let \( h' \) be the head above the centre of the orifice in the higher reservoir, and \( h'' \) in the lower; then the effective head \( h = h' - h'' \ldots (4) \).

5th. If the water escape by a rectangular notch instead of an orifice, that is, an aperture such that the upper level surface of the water does not come in contact with the sides of the vessel, falling freely in the air, the theoretical discharge is two-thirds of the area of the effluent vein multiplied by the velocity of efflux; or, more accurately, if \( h = \) head of water, \( b = \) breadth of notch.

\[
q = \frac{3}{2} b \cdot h \cdot \sqrt{2gh} \ldots (5).
\]

We must next examine certain properties of fluid motion which cause the actual or effective discharge to differ materially from the theoretical discharge given in the above equations, although in a constant ratio, so that the one may always be calculated from the other.

1st. Thick-lipped orifices or mouth pieces. For smooth orifices, the length of which is about twice or three times the smallest diameter, the actual does not widely differ from the theoretical discharge. The velocity of the effluent current is, however, never so great as that in equation (2), but is diminished for a constant ratio for each kind of orifice, and the discharge is less in the same proportion. For a simple cylin-

![Fig. 96.](image)
![Fig. 97.](image)
![Fig. 98.](image)

![Fig. 98.](image)

drical tube, fig. 96, of about 1\( \frac{1}{2} \) diameters in length, the velocity of the effluent water is equal to \( 0.8 v = 0.8 \sqrt{2gh} \) and the actual discharge \( = a \times 0.8 \times v = 0.8 \ q \). Where the interior angle of the tube is rounded, as in fig. 98, the velocity amounts to as much as 0.96 \( v \) to 0.98 \( v \), and hence the discharge to 0.96 \( q \) to 0.98 \( q \), where \( q \) as before is the theoretical discharge given by the above formulæ. This constant ratio is called the coefficient of velocity.
Hence we have this rule for determining the quantity of water discharged by a thick-lipped orifice; seek first in Table I. the velocity corresponding to the given head of water, measured from the centre of the orifice; multiply this velocity by the area of the orifice in square feet, and the product will be the theoretical discharge in cubic feet per second. For the actual discharge, this must be multiplied by 0.7, if the orifice be of the form of fig. 97; by 0.8, if the orifice be of the form of fig. 96; and by 0.97 if it be of the form of fig. 98. The importance of the form of orifice is manifest, and hence a trumpet mouth* should be employed in all water pipes, wherein a maximum discharge is desirable, the quantity being increased whichever way the trumpet mouth is turned, whether as in fig. 98 or 99, but most in the former case. For conical converging tubes, d'Aubuisson found the coefficient of efflux to vary from 0.829 to 0.946 as the lateral convergence increased from 0° 0' to 13° 24', and from 0.946 to 0.847 as the convergence increased from 13° 24' to 48° 50'; the area of the orifice being measured at the small extremity. For tubes which at first converge and then diverge, so as to take the form of the fluid vein, the coefficient of discharge is 1.55, that is, of course, taking the minimum area of the tube.

2nd. Thin-lipped orifices, the fluid escaping freely into the air. With orifices of this nature, the fluid vein contracts very remarkably at a short distance beyond the orifice, and the discharge is diminished in the ratio of the least area of the vein to that of the orifice. This contraction amounts to five-eighths of the area of the orifice in most cases, and hence the actual discharge is scarcely more than five-eighths that estimated by equation (3). Putting \( m \) = the coefficient of contraction, we have the actual discharge from an orifice \( Q = m \alpha \sqrt{2gh} \).

The velocity of the effluent vein is also diminished in a slight degree, perhaps by three or five per cent., but it will be most convenient to combine the coefficients of contraction and velocity together, and to call \( m \) the coefficient of discharge or ratio of actual to theoretical discharge.

* As for instance in the reservoir drawing fig. 37.
A very large number of experiments have been made upon the values of the coefficient \( m \) for various forms of orifices; the most important of which we owe to Michelotti, Castel, Bidone, Bossut, Rennie, and others. But by far the most important and complete are those conducted by MM. Poncelet and Lesbros under the auspices of the French government, and all interested in hydraulic investigations must feel indebted to them for the skill, perseverance, and accuracy with which they have registered so large a body of results. These determinations go to show that the value of the coefficient of discharge ranges between 0.58 and 0.7, being greater for small orifices and small velocities and less for large orifices and high velocities. For heads of three and four feet and upwards, the coefficient of discharge may be taken at 0.6.

Mr. Rennie's results give the following values of \( m \).

<table>
<thead>
<tr>
<th>Head of 4 feet</th>
<th>Head of 1 foot</th>
</tr>
</thead>
<tbody>
<tr>
<td>Circular orifices</td>
<td>0.621</td>
</tr>
<tr>
<td>Triangular orifices</td>
<td>0.593</td>
</tr>
<tr>
<td>Rectangular orifices</td>
<td>0.593</td>
</tr>
</tbody>
</table>

For more accurate calculations I have abridged the following tables of M. Poncelet's results from the 'Aide-Mémoire' of M. Morin, reducing the measures to the English standard.

**TABLE II.—COEFFICIENTS OF DISCHARGE OF VERTICAL RECTANGULAR ORIFICES, THIN-LIPPED, WITH COMPLETE CONTRACTION. THE HEADS OF WATER MEASURED AT A POINT OF THE RESERVOIR WHERE THE LIQUID WAS PERFECTLY STAGNANT.**

| Head or summit of orifice, ins. | Coefficients of discharge for orifices of a height of |
|---|---|---|---|---|---|---|---|---|
|   | 7 9 ins. | 3 9 ins. | 1 9 ins. | 1 18 ins. | 0 78 ins. | 0 39 ins. |
| 0.79 | 0.572 | 0.596 | 0.615 | 0.634 | 0.659 | 0.694 |
| 1.9 | 0.585 | 0.605 | 0.625 | 0.640 | 0.658 | 0.679 |
| 3.9 | 0.592 | 0.611 | 0.630 | 0.647 | 0.654 | 0.666 |
| 7.9 | 0.598 | 0.615 | 0.630 | 0.643 | 0.654 | 0.665 |
| 11.8 | 0.600 | 0.616 | 0.622 | 0.631 | 0.644 | 0.650 |
| 15.7 | 0.602 | 0.617 | 0.628 | 0.631 | 0.642 | 0.647 |
| 20.4 | 0.605 | 0.615 | 0.626 | 0.628 | 0.633 | 0.632 |
| 29.9 | 0.600 | 0.611 | 0.620 | 0.620 | 0.619 | 0.615 |
| 59.7 | 0.601 | 0.607 | 0.613 | 0.612 | 0.612 | 0.611 |
| 118.1 | 0.601 | 0.603 | 0.606 | 0.608 | 0.610 | 0.609 |

* Rankine. † Weisbach.
ON THE FLOW AND DISCHARGE OF WATER.

TABLE III.—Coefficients of discharge of vertical, thin-lipped, rectangular orifices, with complete contraction. The heads of water measured immediately over the orifice.

<table>
<thead>
<tr>
<th>Heads or summit of orifice in ins.</th>
<th>Coefficients of discharge for orifices of a height of</th>
</tr>
</thead>
<tbody>
<tr>
<td>7-9 ins.</td>
<td>8-9 ins.</td>
</tr>
<tr>
<td>0-78</td>
<td>0-594</td>
</tr>
<tr>
<td>1-97</td>
<td>0-593</td>
</tr>
<tr>
<td>3-94</td>
<td>0-595</td>
</tr>
<tr>
<td>7-87</td>
<td>0-599</td>
</tr>
<tr>
<td>11-81</td>
<td>0-601</td>
</tr>
<tr>
<td>15-74</td>
<td>0-600</td>
</tr>
<tr>
<td>19-67</td>
<td>0-605</td>
</tr>
<tr>
<td>23-60</td>
<td>0-602</td>
</tr>
<tr>
<td>27-53</td>
<td>0-601</td>
</tr>
<tr>
<td>31-46</td>
<td>0-601</td>
</tr>
</tbody>
</table>

Thence we derive this rule for estimating the discharge of water from thin-lipped orifices; seek in Table I. the velocity corresponding to the head of water measured from the centre of the effluent vein; multiply this by the area of the orifice in square feet, and the product is the theoretical discharge. Five-eighths of the theoretical discharge will give the actual discharge in cubic feet a second, if a rough approximation only is required. If the estimation is to be accurate, seek in Tables II. and III. the coefficient of discharge most nearly corresponding to the given head and area of orifice, and multiply the theoretical discharge by the coefficient so found. Thus the following table has been calculated:

TABLE IV.—Theoretical and Actual Discharge from a Thin-lipped Orifice of a Sectional Area of One Square Foot.

<table>
<thead>
<tr>
<th>H Head</th>
<th>v Table I.</th>
<th>m Table II.</th>
<th>x v Theoretical Discharge per second</th>
<th>m av Actual Discharge per second</th>
<th>H Head</th>
<th>v Table I.</th>
<th>m Table II.</th>
<th>x v Theoretical Discharge per second</th>
<th>m av Actual Discharge per second</th>
</tr>
</thead>
<tbody>
<tr>
<td>ft.</td>
<td>ft.</td>
<td>ft.</td>
<td>cub. ft.</td>
<td>ft.</td>
<td>ft.</td>
<td>ft.</td>
<td>cub. ft.</td>
<td>ft.</td>
<td>cub. ft.</td>
</tr>
<tr>
<td>1</td>
<td>8.02</td>
<td>0.60</td>
<td>8.02</td>
<td>4.812</td>
<td>11</td>
<td>26.8</td>
<td>0.60</td>
<td>26.8</td>
<td>15.96</td>
</tr>
<tr>
<td>2</td>
<td>11.34</td>
<td>0.60</td>
<td>11.34</td>
<td>6.804</td>
<td>12</td>
<td>27.8</td>
<td>0.60</td>
<td>27.8</td>
<td>16.68</td>
</tr>
<tr>
<td>3</td>
<td>13.90</td>
<td>0.60</td>
<td>13.90</td>
<td>8.340</td>
<td>13</td>
<td>28.9</td>
<td>0.60</td>
<td>28.9</td>
<td>17.34</td>
</tr>
<tr>
<td>4</td>
<td>16.04</td>
<td>0.60</td>
<td>16.04</td>
<td>9.624</td>
<td>14</td>
<td>30.0</td>
<td>0.60</td>
<td>30.0</td>
<td>18.00</td>
</tr>
<tr>
<td>5</td>
<td>17.93</td>
<td>0.60</td>
<td>17.93</td>
<td>10.75</td>
<td>15</td>
<td>31.1</td>
<td>0.60</td>
<td>31.1</td>
<td>18.66</td>
</tr>
<tr>
<td>6</td>
<td>19.64</td>
<td>0.60</td>
<td>19.64</td>
<td>11.78</td>
<td>16</td>
<td>32.1</td>
<td>0.60</td>
<td>32.1</td>
<td>19.26</td>
</tr>
<tr>
<td>7</td>
<td>21.21</td>
<td>0.60</td>
<td>21.21</td>
<td>12.73</td>
<td>17</td>
<td>33.1</td>
<td>0.60</td>
<td>33.1</td>
<td>19.86</td>
</tr>
<tr>
<td>8</td>
<td>22.68</td>
<td>0.60</td>
<td>22.68</td>
<td>13.61</td>
<td>18</td>
<td>34.0</td>
<td>0.60</td>
<td>34.0</td>
<td>20.40</td>
</tr>
<tr>
<td>9</td>
<td>24.10</td>
<td>0.60</td>
<td>24.10</td>
<td>14.46</td>
<td>19</td>
<td>34.9</td>
<td>0.60</td>
<td>34.9</td>
<td>20.94</td>
</tr>
<tr>
<td>10</td>
<td>25.40</td>
<td>0.60</td>
<td>25.40</td>
<td>15.24</td>
<td>20</td>
<td>35.0</td>
<td>0.60</td>
<td>35.0</td>
<td>21.54</td>
</tr>
</tbody>
</table>
The above table is given as a sample of the method of calculation according to the above rule. For other areas and different heads the calculation may very easily be performed.

3rd. *Discharge with incomplete contraction.*—It is very frequently the case in practice that one of the sides of a thin-lipped orifice is prolonged, so that the vein of fluid no longer contracts upon all sides, as in fig. 99A. In this case the coefficients in Tables II. and III. give too low a result. M. Morin gives the following rule for discharge with incomplete contraction:

Multiply the coefficient of discharge for complete contraction found as above by

\[
\begin{align*}
1.035 \text{ when the vein contracts on 3 sides only} \\
1.072 \text{ " 2 sides "} \\
1.125 \text{ " 1 side "}
\end{align*}
\]

in order to obtain the true coefficient by which the theoretical discharge must be multiplied to give the actual discharge. Hence, for an approximate calculation, we may multiply the theoretical discharge \(= (a \times v) \) by 0.63, when the orifice is prolonged upon one side; by 0.66 when it is prolonged on two sides, and by 0.69 when it is prolonged on three sides. When all four sides are prolonged, the thick-lipped orifice, fig. 94, is formed of which the coefficient of efflux is 0.8.

4th. *Discharge from rectangular notches, waste boards, and weirs.*—In this case the theoretical discharge =

\[
q = \frac{1}{3} bh \sqrt{\frac{g}{h}} \}
\]

\[
= \frac{1}{3} av
\]

where \(q\) = discharge in cubic feet per second.

\(b\) = breadth of notch or weir.

\(h\) = head of water, measured at some distance behind the crest of the weir.

\(v\) = velocity in feet per second = \(\sqrt{\frac{g}{h}}\) ... (2)

\(a\) = area of effluent vein = \(b \times h\).

The actual discharge is found by multiplying the theoretical
discharge by the coefficient of efflux \( m \), which varies under different circumstances. The millwright must select this coefficient from the following tables, so as to suit the particular case to which it is to be applied.

<table>
<thead>
<tr>
<th>Head of Water in inches</th>
<th>0.89</th>
<th>0.78</th>
<th>1.18</th>
<th>1.57</th>
<th>2.36</th>
<th>3.15</th>
<th>3.93</th>
<th>5.90</th>
<th>7.86</th>
<th>8.65</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coefficient of discharge ( \frac{1}{8}m )</td>
<td>0.424</td>
<td>0.417</td>
<td>0.412</td>
<td>0.407</td>
<td>0.401</td>
<td>0.397</td>
<td>0.395</td>
<td>0.393</td>
<td>0.390</td>
<td>0.385</td>
</tr>
</tbody>
</table>

This gives a mean value of 0.4 or \( \frac{2}{5} \)ths for \( \frac{1}{8}m \), and hence we may approximately find the discharge from a waste board by multiplying the head in feet by the breadth of the notch in feet, and by the velocity due to the head found by equation (2) or Table I. Two-fifths of this product will be the discharge in cubic feet per second.

In 1852 the council of the Institution of Civil Engineers awarded to Mr. Blackwell a premium for a valuable series of experiments on the discharge of water from weirs made on a very large scale, and with various conditions of head and with different kinds of overfall bars. What constitutes the principal value of Mr. Blackwell's paper is the scale on which the experiments were made, and their close approximation to actual practice. It must be borne in mind, however, that in calculating the quantity of water discharged in the flow of rivers over weirs, reference must be had to the form of the top, in order to ascertain the state of the overfall as compared with those in the following table, from which the coefficient is taken for calculation.
<table>
<thead>
<tr>
<th>No. of Trials</th>
<th>Description of Overfalls</th>
<th>Head in ins.</th>
<th>$/m.</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>Thin plate 8 feet long</td>
<td>1 to 3</td>
<td>.440</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 to 6</td>
<td>.402</td>
</tr>
<tr>
<td>11</td>
<td>Thin plate 10 feet long</td>
<td>1 to 3</td>
<td>.501</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4 to 6</td>
<td>.435</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6 to 9</td>
<td>.270</td>
</tr>
<tr>
<td>23</td>
<td>Plank 2 inches thick, with notch 3 feet broad</td>
<td>1 to 3</td>
<td>.342</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 to 6</td>
<td>.384</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6 to 10</td>
<td>.406</td>
</tr>
<tr>
<td>66</td>
<td>Plank 2 inches thick, with notch 6 feet broad</td>
<td>1 to 3</td>
<td>.359</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 to 4</td>
<td>.396</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6 to 9</td>
<td>.392</td>
</tr>
<tr>
<td></td>
<td></td>
<td>9 to 14</td>
<td>.358</td>
</tr>
<tr>
<td>40</td>
<td>Plank 2 inches thick, with notch 10 feet broad</td>
<td>1 to 3</td>
<td>.346</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 to 6</td>
<td>.327</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6 to 9</td>
<td>.374</td>
</tr>
<tr>
<td></td>
<td></td>
<td>9 to 12</td>
<td>.336</td>
</tr>
<tr>
<td>4</td>
<td>Plank 2 ins. thick, notch 10 ft. broad, with wings</td>
<td>1 to 2</td>
<td>.476</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4 to 5</td>
<td>.442</td>
</tr>
<tr>
<td>7</td>
<td>Overfall with a crest, 3 feet wide, sloping 1 in 12, 3 feet long like a weir</td>
<td>1 to 3</td>
<td>.342</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 to 6</td>
<td>.328</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6 to 9</td>
<td>.311</td>
</tr>
<tr>
<td>9</td>
<td>Overfall with a crest, 3 feet wide, sloping 1 in 18, 3 feet long, like a weir</td>
<td>1 to 3</td>
<td>.362</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 to 6</td>
<td>.345</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6 to 9</td>
<td>.332</td>
</tr>
<tr>
<td>6</td>
<td>Overfall with a crest, 3 feet wide, sloping 1 in 18, and 10 feet long</td>
<td>1 to 4</td>
<td>.328</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4 to 8</td>
<td>.350</td>
</tr>
<tr>
<td>14</td>
<td>Overfall with a level crest 3 feet wide, by 6 long</td>
<td>1 to 3</td>
<td>.305</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 to 6</td>
<td>.311</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6 to 9</td>
<td>.318</td>
</tr>
<tr>
<td>15</td>
<td>Overfall with level crest, 6 feet long by 3 broad</td>
<td>3 to 7</td>
<td>.330</td>
</tr>
<tr>
<td></td>
<td></td>
<td>7 to 12</td>
<td>.310</td>
</tr>
<tr>
<td>12</td>
<td>Overfall with level crest, 3 feet wide by 10 long</td>
<td>1 to 5</td>
<td>.306</td>
</tr>
<tr>
<td></td>
<td></td>
<td>5 to 8</td>
<td>.327</td>
</tr>
<tr>
<td></td>
<td></td>
<td>8 to 10</td>
<td>.313</td>
</tr>
<tr>
<td>61</td>
<td>At Chew Magna, overfall bar 10 feet long, 2 inches thick</td>
<td>1 to 8</td>
<td>.437</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3 to 6</td>
<td>.499</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6 to 9</td>
<td>.505</td>
</tr>
</tbody>
</table>
ON THE FLOW AND DISCHARGE OF WATER.

The most important of the generalisations from this table are—

1st. That the discharge is decreased in proportion to the breadth and inclination of the crest, being least when the crest is level.

2nd. That converging wing walls, above the overfall, increase the discharge.

Where, as in the case of a river, the water approaches the weir with a certain velocity, it should be taken separately into account, the above coefficients being deduced from experiments on reservoirs so large that the water was approximately stagnant.

Let \( k \) = height of head due to velocity \( v \) of water as it approaches the weir; that is, let \( k = \frac{v^2}{64.38} \);
the effective discharge is then =

\[
Q = \frac{1}{5} m \cdot b \cdot \sqrt{2g \left[ (h + k)^{\frac{3}{2}} - k^{\frac{3}{2}} \right]} \quad (6)
\]

**Table VII.—Examples of Estimation of Discharge from Weirs.**

<table>
<thead>
<tr>
<th>Head of water</th>
<th>Velocity due to head</th>
<th>Coefficient of discharge, Tables V. VI.</th>
<th>Breadth</th>
<th>( \frac{b \cdot A \cdot v}{m \cdot b \cdot A \cdot v} ) Theoretical discharge per second</th>
<th>( \frac{b \cdot A \cdot v}{m \cdot b \cdot A \cdot v} ) Actual discharge per second</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>inches</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>2.32</td>
<td>0.412</td>
<td>1 ft.</td>
<td>1.283</td>
<td>0.739</td>
<td>Thin-lipped waste board</td>
</tr>
<tr>
<td>6</td>
<td>5.67</td>
<td>0.393</td>
<td>1 ft.</td>
<td>1.890</td>
<td>1.114</td>
<td></td>
</tr>
<tr>
<td>12</td>
<td>8.02</td>
<td>0.380</td>
<td>1 ft.</td>
<td>5.35</td>
<td>3.047</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>5.67</td>
<td>0.350</td>
<td>10 ft.</td>
<td>18.90</td>
<td>9.922</td>
<td>Weir with crest</td>
</tr>
</tbody>
</table>

According to the above formula I have computed the following table showing at a glance the velocity in feet, the theoretical discharge in cubic feet per second, and the actual discharge of water over a thin-edged notch or weir for various heads from \( \frac{1}{2} \) an inch to 6 feet—the water approaching the weir with no perceptible current.

* Weisbach.
Mr. Sang of Kirkcaldy has proposed a very ingenious arrangement for the approximate measurement of the flow of water over a rectangular notch in a waste board, particularly applicable in cases where the flow has to be frequently registered, as in the daily observations by which drainage is estimated. He employs a scale graduated variably, so as to give at once the number of cubic feet per minute of water to every inch in breadth of the rectangular notch. Hence instead of employing a complex formula, nothing more is required than to observe at what number the water stands on the rule, and to multiply that by the number of inches of breadth of the notch, and we obtain at once the discharge in cubic feet per minute. He proposes that such a scale engraved on paper should be placed in a glass tube, hermetically sealed, and permanently fixed in a suitable position on the weir. The following table calculated by Mr. Sang shows the position of the divisions of the scale corresponding to cubic feet, and tenths of cubic feet discharge:

<table>
<thead>
<tr>
<th>Head in feet</th>
<th>Velocity in feet per second</th>
<th>Discharge in cubic feet per second</th>
<th>Theoretical discharge per second</th>
<th>Actual discharge per second</th>
<th>Head in feet</th>
<th>Velocity in feet per second</th>
<th>Discharge in cubic feet per second</th>
<th>Theoretical discharge per second</th>
<th>Actual discharge per second</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.05</td>
<td>1.79</td>
<td>0.42</td>
<td>0.096</td>
<td>0.076</td>
<td>2.1</td>
<td>11.62</td>
<td>0.35</td>
<td>16.94</td>
<td>8.900</td>
</tr>
<tr>
<td>1</td>
<td>2.64</td>
<td>0.41</td>
<td>0.168</td>
<td>0.1037</td>
<td>2.2</td>
<td>11.90</td>
<td>0.35</td>
<td>17.44</td>
<td>9.163</td>
</tr>
<tr>
<td>2</td>
<td>3.58</td>
<td>0.40</td>
<td>0.248</td>
<td>0.286</td>
<td>2.3</td>
<td>12.17</td>
<td>0.35</td>
<td>18.66</td>
<td>9.796</td>
</tr>
<tr>
<td>3</td>
<td>4.39</td>
<td>0.40</td>
<td>0.318</td>
<td>0.527</td>
<td>2.4</td>
<td>12.43</td>
<td>0.34</td>
<td>19.98</td>
<td>10.142</td>
</tr>
<tr>
<td>4</td>
<td>5.07</td>
<td>0.40</td>
<td>0.382</td>
<td>0.811</td>
<td>2.5</td>
<td>12.68</td>
<td>0.34</td>
<td>21.14</td>
<td>10.778</td>
</tr>
<tr>
<td>5</td>
<td>5.87</td>
<td>0.39</td>
<td>0.440</td>
<td>1.05</td>
<td>2.6</td>
<td>12.94</td>
<td>0.34</td>
<td>22.42</td>
<td>11.439</td>
</tr>
<tr>
<td>6</td>
<td>6.60</td>
<td>0.39</td>
<td>0.501</td>
<td>1.411</td>
<td>2.8</td>
<td>13.24</td>
<td>0.34</td>
<td>23.78</td>
<td>12.774</td>
</tr>
<tr>
<td>7</td>
<td>7.17</td>
<td>0.39</td>
<td>0.561</td>
<td>1.832</td>
<td>3.0</td>
<td>13.59</td>
<td>0.34</td>
<td>25.04</td>
<td>13.751</td>
</tr>
<tr>
<td>8</td>
<td>7.71</td>
<td>0.38</td>
<td>0.616</td>
<td>2.179</td>
<td>3.2</td>
<td>13.95</td>
<td>0.33</td>
<td>27.88</td>
<td>15.053</td>
</tr>
<tr>
<td>9</td>
<td>8.23</td>
<td>0.38</td>
<td>0.664</td>
<td>2.500</td>
<td>3.4</td>
<td>14.32</td>
<td>0.33</td>
<td>30.00</td>
<td>16.593</td>
</tr>
<tr>
<td>10</td>
<td>8.72</td>
<td>0.38</td>
<td>0.708</td>
<td>2.847</td>
<td>3.6</td>
<td>14.69</td>
<td>0.33</td>
<td>33.12</td>
<td>18.081</td>
</tr>
<tr>
<td>11</td>
<td>9.16</td>
<td>0.37</td>
<td>0.746</td>
<td>3.132</td>
<td>3.8</td>
<td>15.05</td>
<td>0.33</td>
<td>36.25</td>
<td>19.512</td>
</tr>
<tr>
<td>12</td>
<td>9.55</td>
<td>0.37</td>
<td>0.780</td>
<td>3.394</td>
<td>4.0</td>
<td>15.40</td>
<td>0.33</td>
<td>39.32</td>
<td>21.012</td>
</tr>
<tr>
<td>13</td>
<td>9.91</td>
<td>0.37</td>
<td>0.807</td>
<td>3.649</td>
<td>4.2</td>
<td>15.76</td>
<td>0.33</td>
<td>42.38</td>
<td>22.512</td>
</tr>
<tr>
<td>14</td>
<td>10.07</td>
<td>0.37</td>
<td>0.824</td>
<td>3.906</td>
<td>4.4</td>
<td>16.12</td>
<td>0.33</td>
<td>45.43</td>
<td>24.012</td>
</tr>
<tr>
<td>15</td>
<td>10.51</td>
<td>0.37</td>
<td>0.840</td>
<td>4.300</td>
<td>4.6</td>
<td>16.47</td>
<td>0.33</td>
<td>50.47</td>
<td>26.012</td>
</tr>
<tr>
<td>16</td>
<td>11.01</td>
<td>0.37</td>
<td>0.850</td>
<td>4.530</td>
<td>4.8</td>
<td>16.83</td>
<td>0.33</td>
<td>55.52</td>
<td>28.012</td>
</tr>
<tr>
<td>17</td>
<td>11.37</td>
<td>0.36</td>
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5. Friction of fluids in conduits and pipes.—In long tubes an increased retardation arises, which must be ascribed to the friction of the fluid against the sides, and it has been ascertained that this element of retardation, whilst independent of the pressure of the fluid, increases in the ratio of the length of the tube, and decreases in the ratio of the width or diameter. It also increases nearly as the square of the velocity.

For pipes of uniform size and with no considerable amount of bending, it may be shown that the velocity of discharge

\[ v = \sqrt{\frac{2380 \, h \, d}{l + 54 \, d}} - \frac{1}{12} \, \frac{l}{l + 54 \, d} \ldots (7) \]

or if \( h \) be not very small, neglecting the last term,

\[ \sqrt{\frac{2380 \, h \, d}{l + 54 \, d}} \ldots (8) \]

and if the pipes be very long,
\[ v = \sqrt{\frac{2380}{l + 54d}} - \frac{1}{12} \ldots (9) \]

where \( l \) = length of pipe in feet; \( d \) = diameter in feet; \( h \) = head in feet; and the constants have been derived from the experiments of Prony and d'Aubuisson.

Formula (8) very nearly coincides with that given by Poncelet, namely,

\[ v = 47.9 \sqrt{\frac{d h}{l + 54d}} = \sqrt{\frac{2300}{l + 54d}} \]

The most convenient way in practice of estimating the retardation of friction in the pipes is to measure the head of water which is requisite to overcome the friction, without increasing the velocity of the current. In calculations of quantity when the head \( h \), necessary to generate the required velocity of exit, has been estimated by the rule for thick-lipped orifices already given, another head \( h_1 \) must be added as necessary to overcome the friction, if the orifice is prolonged into a tube.

The height to overcome friction may be calculated from the formula

\[ h_1 = n \frac{i}{d} \cdot \frac{v^2}{2g} \ldots (10) \]

where \( n \) is the coefficient of friction derived from experiment. Hence, putting \( q \) for the discharge,

\[ v = \frac{4q}{\pi d^2} \ldots (11) \]

when the pipe is cylindrical.

We may combine this formula with the preceding formula for the discharge from a thick-lipped orifice, putting \( m \) = coefficient of resistance for the portion of tube next the cistern, and \( n \), coefficient of resistance for the remainder of the tube; we then have for the whole head of water

\[ h = m \frac{v^2}{2g} + n \frac{l}{d} \cdot \frac{v^3}{2g} + \frac{v^2}{v g} \ldots (12) \]

or

\[ h = \left( 1 + m + n \frac{l}{d} \right) \frac{v^2}{2g} \ldots (13) \]

and

\[ v = \frac{\sqrt{2g h}}{\sqrt{1 + m + n \frac{l}{d}}} \ldots (14) \]
ON THE FLOW AND DISCHARGE OF WATER. 107

and putting \( a \) = area of orifice, the discharge =

\[ q = av \ldots (15). \]

If there be bends in the tube an increased element of resistance is introduced; if we put \( p \) for the sum of the resistances due to this source,

\[ h = \left(1 + m + n \frac{l}{d} + p\right) \frac{v^3}{2g} \ldots (16) \]

\[ = \left(1 + m + n \frac{l}{d} + p\right) \left(\frac{4q}{\pi}\right)^3 \frac{1}{2gd^3} \ldots (17). \]

These formulæ we have from Weisbach's 'Mechanics of Engineering,' from which the following table has been reduced and adapted to English measures.

<p>| Table of the Value of the Coefficient of Friction ( n ) for Different Velocities. |
|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|</p>
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To use this table look in the horizontal line at top for the nearest velocity in feet, in the vertical column underneath and opposite the nearest number of inches will be found the value of \( n \) required. Thus for a velocity of 6 feet 8 inches per second, the coefficient \( n \) will be found to be 0.211, being under 6 and opposite 8.

From sixty-three experiments Weisbach deduces another general formula for the flow of water in tubes which is very convenient for calculation. It is based on the hypothesis that the resistance to friction increases simultaneously as the square, and as the square root of the cube of the velocity, and is of the form

\[ h = \left(0.0144 + \frac{0.01716}{\sqrt{v}}\right) \frac{L}{D} \cdot \frac{v^2}{64.4} \ldots (18) \]

which gives the head due to friction in feet. From this formula, Mr. James Thomson, M.A., C.E., and Mr. George Fuller, C.E., have calculated the following very complete and convenient table.
**FRICITION OF WATER IN PIPES.**

Table calculated from a formula of Julius Weisbach, to show, for Pipes 100 feet in length, the relation between 1st. The Velocity of the Water, in feet per second.—2nd. The Internal Diameter of the Pipe.—3rd. The head to overcome the Fricition, in Feet.—4th. The number of Cubic Feet of Water delivered per Minute; so that when any two of these four quantities are given, the remaining two can be found.  

By JAMES THOMSON, A.M., C.E., and GEORGE FULLER, C.E., Belfast.

<table>
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<th>Cubic Feet per Minute</th>
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* This Table also shows, by the first and second columns, the relation between the velocity and the head required to produce the velocity, calculated by the laws of falling bodies, independently of friction, contraction of the vein, or other retarding causes.

The formula of Wehmann for this Table is given in his 'Ingenieur-und-Maschinen-Mechanik,' vol. i. p. 434, and when reduced to English measure is as follows:

$$ h = \frac{0.0144 + 0.0171}{45.9} l \times \frac{v^2}{d} $$

where $h$ = head to overcome the friction, in English feet; $l$ = length of pipe, in English feet; $d$ = internal diameter of pipe, in English feet; and $v$ = velocity of water, in English feet per second.
In laying pipes the following directions are not unimportant; the mouth, both for ingress and egress, should be trumpet-shaped; bends should be as far as possible avoided, and especially sharp angular bends; at junctions the smaller pipe should be brought round in a curve to agree in direction with the main. And, lastly, where a pipe rises and falls much, air is apt to collect in the upper parts of the bends, and thus reduce the section at that part, and it is advisable to make provision by a cock or otherwise for drawing it off at intervals.

Flow of water in open channels.—This is a question of importance, and requires careful consideration on the part of the engineer, as it is a case of frequent occurrence in calculations of the flow of water. It is often, from various circumstances, impossible to throw even a temporary waste board or weir across a stream the quantity of discharge from which it is desirable to ascertain, and hence it becomes necessary to determine a formula which takes into account the friction of the river sides.

In estimating the velocity of a stream on a canal or river, by throwing in floating bodies of nearly the same specific gravity as the water, and estimating the time they require to pass a given measured distance, it must be borne in mind that the velocity is greatest in the centre of the stream and near the surface, and less at the bottom and near the sides. It is generally most convenient to ascertain the velocity at the centre, where the stream is fleetest, but it is essential in calculations to know the mean velocity, or the velocity of a stream of the same section, discharging the same quantity of water, but unaffected by friction at the sides. In practice it will be sufficient to assume that the mean velocity of a stream is equal to $0.83$ per cent. or $\frac{1}{3}$ of the velocity at the surface.

Or we may use an empirical formula of Prony's, putting $v$ for the mean velocity, and $v$ for the surface velocity, measured by a floating body at the middle of the stream

$$v = \frac{v (v + 7.77)}{v + 10.33} \quad \ldots \ (19)$$

For small streams the most accurate method of measurement is the formation of a temporary weir by a vertical board thrown across the stream and carefully puddled at the edges. A rect-
angular notch of sufficient capacity to pass the water must be cut in the middle portion. The height of the water above the level of the notch should then be measured either at its crest, or better still at some distance behind, where the water is nearly still, and the constant for calculation will be found in Table V. or VI. as the case may be.

But if a waste board or weir cannot be employed, we may find the surface velocity, and from that obtain its mean velocity by the methods given above. If then we take the depth of the stream at various parts of its breadth and so calculate its sectional area, we may find the cubic feet of water discharged per second by multiplying the mean velocity (in feet per second) by the area so found (in square feet).

Thus, if a body floats along the surface of a stream 300 feet in a minute, its maximum velocity $= \frac{300}{60} = 5$ feet per second, and its mean velocity, according to Prony, $= \frac{5 \left(5 + 7.77\right)}{5 + 10.33} = 4.16$. Now let the depth of the stream, 16 feet broad, measured at equal distances of two feet apart, be 0, 1, $2\frac{1}{2}$, 3, 3, $3\frac{1}{2}$, 3, 1$\frac{1}{2}$, 0 feet respectively, then the area $= 2 \times (1 + 2\frac{1}{2} + 3 + 3 + 3\frac{1}{2} + 3 + 1\frac{1}{2}) = 36$ sq. ft.

:. Cubic feet of water discharged per second $= 36 \times 4.16 = 149.76$ cubic feet.

In rivers, the coefficient of friction $n$ in formulae (12)(13) and (14) may be taken at 0.0075; it varies, according to Weisbach, from 0.00811 to 0.00748 as the velocity increases from 0.1 to 1.0 metres, and from 0.00748 to 0.00743 as the velocity increases from 1 to 3 metres.

The following formulae express the relations of velocity, fall, and discharge, when the flow of the stream is uniform:

$$h = \zeta \cdot \frac{l}{p} \cdot \frac{c^2}{2g} \ldots (20)$$

$$c = \sqrt{\frac{g}{\zeta l}} \cdot 2gh \ldots (21)$$

$$Q = F \cdot c \ldots (3). \ast$$

\* Weisbach, vol. i. p. 493.
Where \( h \) = whole fall, \( q \) = discharge, \( r \) = transverse section of stream, \( c \) = mean velocity of stream, \( l \) = distance which the river flows for a fall \( h \), \( \frac{P}{r} \) the perimeter of the water profile, and \( \zeta \) the coefficient of friction.

The best form of section must be that which presents the least resistance to a given quantity of water flowing through the channel. Now it has been shown that the resistance of friction varies directly as the wetted perimeter and inversely as the area of the section, and when the area is constant it will therefore vary directly as the wetted perimeter. Consequently the best form of section will be that with the least perimeter for a given area. Hence for open channels in which the upper water line is not part of the wetted perimeter, the half square is the best rectangular section, and the semihexagon the best trapezoidal section. For equal flows of water the semicircle will have less friction than the semihexagon, and the semihexagon than the semisquare. In designing conduits, for instance, the head race or tail race of water wheels, not only must the sectional form be attended to, but bends must be avoided as much as possible.

*Estimation of Water Power.*—Where a natural reservoir of mechanical power is employed through the medium of a prime-mover in overcoming resistances, in sawing, grinding, &c., we term the moving force the power, and the resistances overcome the work.

The dynamic unit by which we estimate force or resistance is the *foot-pound*, or the unit of force which is capable of lifting a weight of one pound one foot high. A second unit is employed when estimating large expenditure of force, namely, the *horse-power*. One horse-power, according to the estimate of Watt, was equivalent to 33,000 lbs. raised one foot high in a minute or 550 foot-pounds per second.

It is evident that a power exerted by a weight of water falling a given number of feet is capable of raising an equal weight the same number of feet. The power expended must equal the resistances overcome. In transmitting power through a prime-mover, however, a certain loss necessarily takes place, arising (1) from the loss or waste of the power by spilling, leakage, &c., and (2) from the absorption of a part of the power
THE ESTIMATION OF WATER POWER.

in overcoming the resistances of the prime-mover itself, friction, &c. Hence the work accomplished by a prime-mover is never equivalent to the power expended on it; the useful effect is always only a certain percentage of the power, and this percentage is called the efficiency or modulus of the machine.

Now for a water-wheel on which a stream of water acts by gravity alone:

Let \( h \) = height of fall in feet.
\( w \) = weight of water delivered on the wheel per second.
\( n \) = the number of cubic feet per second.
\( p \) = the dynamic force of the falling water in foot-pounds.
\( p_1 = p \) reduced to horses power.
\( v \) = the useful effect of the machine in foot-pounds and
\( v_1 = v \) reduced to H. P.
\( u \) = the modulus of the machine.

Then for the total water power of the wall we have, in foot-pounds,
\[
p = w h \quad \text{(1)};
\]
and water weighing 62.5 lbs. per cubic foot,
\[
p = 62.5 \, n \, h;
\]
or, in horses power,
\[
p_1 = \frac{w h}{550} = \frac{62.5 \, n \, h}{550} = \frac{n \, h}{8.8}
\]

Hence, for every foot of fall 8.88 cubic feet of water per second, or 1.47 tons per minute, theoretically afford an available force of one horse power.

But by definition,
\[
\frac{u \, p}{100} = u \ldots \text{(22).}
\]
\[
\therefore \, v = \frac{u \, w \, h}{100} \text{ in foot-pounds.}
\]
\[
\therefore \, v_1 = \frac{u \, w \, h}{55000} \text{ in horses power.}
\]

and,
\[
\frac{100 - u}{100} \, p \quad \text{is the sum of the resistances from friction, &c.,}
\]
and the loss from wasted water, in accumulating and transmitting the power.

PART I.
CHAPTER III.

ON THE CONSTRUCTION OF WATER WHEELS.

In the present age, the same importance is not attached to water power as before the introduction of steam, as has been already shown. Nevertheless, since water is still largely employed in some districts and for certain kinds of work, it is of importance that the machinery for rendering it useful should be constructed upon the best principle, so as to secure a maximum effect. In numerous localities in Europe and America, water is the principal motive agent by which manufacturing processes are carried on; and the time has not yet arrived when it can be dispensed with even in our own country. We shall therefore endeavour to point out the difference between the ordinary and improved forms of water wheels, and to lay down sound principles of construction, accompanied by examples for the guidance of the millwright.

CLASSIFICATION OF WATER MACHINES.

Water may be expended upon water machines, 1st. By gravitation, as in vertical wheels generally; 2nd. By pressure simply, as in the water pressure engine, where the water acts on a reciprocating piston; 3rd. By the impulse of effluent water striking float boards, as in the Poncelet wheel; 4th. By the reaction of effluent water issuing from an orifice, as in the Barker's mill and Whitelaw's turbine; or lastly, by momentum, as in the case of the water ram.

It is not, however, always possible in practice to classify water machines according to the mode in which the water expends its force, and hence it will be more convenient to divide them according to the point at which the water is applied, and the direction in which it passes through the wheel, as in the following summary:—

1st. **Vertical Water Wheels**, the plane of rotation being vertical and the water received and afterwards discharged at the
same orifice on the external periphery. These may be subdivided into:

a. Overshot wheels, where the water is applied over the crest, or near the upper extremity of the vertical diameter.

b. Breast wheels, where the water is applied below the crest at the side of the wheel.

c. Undershot wheels, where the water is applied near the bottom of the wheel, and acts, 1. By gravitation, as in the improved undershers hot wheel; or 2. By impulse, as in the ordinary undershot and Poncelet wheels.

2nd. Horizontal Wheels, the plane of rotation being horizontal and the water passing through the wheel from one side to the other. These may be subdivided into:

a. Horizontal wheels strictly so called, in which the water passes vertically down through the wheel, acting as it passes on curved buckets.

b. Turbines, annular wheels in which the water enters the buckets at the internal periphery, and passing horizontally is discharged at the external periphery.

c. Vortex wheels, in which the water entering at the external periphery flows horizontally and is discharged at the internal periphery.

3rd. Reciprocating Engines, in which the water is applied upon a piston and regulated by valves on the same principle as the steam engine.

The Improvements of the Vertical Wheel.—In the present chapter it will be convenient to enter on the consideration of the construction of vertical wheels. Since the time of Smeaton's experiments in 1759, the principle on which vertical water wheels have been constructed has undergone no important change, although considerable improvements have been effected in the details. The substitution of iron for wood has afforded opportunities for extensive changes in their forms, particularly in the shape and arrangement of the buckets, and has given a lighter and more permanent character to the machine than had previously been attained. A curvilinear form for the buckets has been adopted, the sheet iron of which they are composed affording great facility for being moulded into the required shape. It is not the object of the present treatise to enter into the dates
of past improvements, but it will suffice to observe that the breast wheel has taken precedence of the overshot wheel, probably from the increased facilities which a wheel of this description affords for the reception of the water under a varying head. It is in most cases more convenient to apply the water of high falls on the breast at an elevation of about 30° from the vertical diameter, as the support of the pentrough is much less expensive and difficult than when it has to be carried over the top of the wheel. In cases of a variable head, when it is desirable to work down the supply of water, it cannot be accomplished without a sacrifice of power on an overshot wheel; but when applied at the breast, the water in all states of the river is received upon the wheel at the highest level of its head at the time, and no waste is incurred. On most rivers this is important, as it gives the manufacturer the privilege of drawing down the reservoir three or four feet before stopping time in the evening, in order to fill again during the night; or to keep the mill at work in dry seasons until the regular supply reaches it from the mills higher up the river. This becomes an essential arrangement where a number of mills are located upon the same stream, and hence the value of small regulating reservoirs behind the mill as a resource for a temporary supply.

Another advantage of the increased diameter of the breast wheel is the ease with which it overcomes the obstruction of back water. The breast wheel is not only less injured by floods, but the retarding force is overcome with greater ease, and the wheel works in a greater depth of back water.

Component parts of Water Wheels.—Vertical water wheels consist essentially of a main axis resting on masonry foundations, and together with arms and braces forming the means of support for the machine. Chambers for the reception of the water constructed of shrouding, sole-plate, and buckets. A pentrough with sluice for laying on the water, and a tail-race for conveying it away; and an internal or external geared spur wheel and pinion for transmitting the power. These parts we shall treat of successively, before describing the modifications of the vertical wheel.

The main axis is a large and heavy cast-iron shaft carried upon plummer blocks bolted to the masonry foundations of the
wheel-house. It sustains the weight of all the moving parts of
the wheel, and in some cases the power is taken from it, when
it is subjected to a force of torsion. It is usually cast with
deep ribs or wings, calculated to resist the tensile
and compressive strain to
which they are alternately
subjected as the wheel
revolves. A section and
elevation of the main
axis of a water wheel, 20
feet in diameter and 22
feet wide, are shown in
figs. 100 and 101.* A A is
one half the main axis
with its four deep ribs.
The part e is the journal
on which the wheel re-
volves, and d is left square
for the convenience of
fixing a screw-jack should
the wheel require rais-
ing. B B B are the re-
cesses for the radical arms
of 2\$$\frac{1}{2}$$-inch round iron
fixed by the keys f f ;
g g the corresponding re-
cesses for the braces which pass diagonally across the wheel
and alternate with the arms; c c are the key beds on the main
axis for fixing the main centre. It is difficult to estimate the
strain on this shaft when the wheel is on the suspension
principle, although the work it has to perform is trifling com-
pared with what it would have to sustain in the event of the
power being taken from the axle. In the latter case the wheel
has to sustain not only the weight of the wheel and the water
in the buckets, but also the force of torsion, as the power is
transmitted from the periphery through the arms and axle to
the main gearing of the mill.

* The wheel is shown in Plate IV. Fig. 110 is also an enlarged detail drawing
of this wheel.
ON THE CONSTRUCTION OF WATER WHEELS.

The following table exhibits the dimensions of the journals, which for high and low breast wheels, where the depth of the buckets is nearly the same, I have found effective, and is a summary of my own practice in this respect for the last forty years:—

<table>
<thead>
<tr>
<th>Diameter of Wheels in feet</th>
<th>Diameter of Journal for a Wheel</th>
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<tbody>
<tr>
<td></td>
<td>5 ft. broad</td>
</tr>
<tr>
<td>15</td>
<td>6</td>
</tr>
<tr>
<td>18</td>
<td>6(\frac{1}{2})</td>
</tr>
<tr>
<td>20</td>
<td>7</td>
</tr>
<tr>
<td>25</td>
<td>7(\frac{1}{2})</td>
</tr>
<tr>
<td>30</td>
<td>8</td>
</tr>
<tr>
<td>40</td>
<td>8(\frac{1}{2})</td>
</tr>
<tr>
<td>50</td>
<td>9(\frac{1}{2})</td>
</tr>
</tbody>
</table>

The lengths of the bearings are usually equal to one and a half diameters of the journal.

Tredgold's rule for the diameter of water-wheel journals is that

\[ d = \frac{1}{9} (l \times w)^{\frac{1}{3}} \]  \(\text{(1)}\)

where \(d\) = diameter of gudgeon in inches, \(l\) = its length in inches, and \(w\) = the maximum load placed on it in lbs.; or, supposing the power to be taken off at the loaded side and the pinion to carry the weight of water, \(w\) = half the weight of the wheel.

Example.—A wheel 18 feet in diameter and 20 feet broad weighs 34 tons; required the diameter of the gudgeon of the main axis, taking its length at 10 inches.

Here, \(d = \frac{1}{9} (10 \times 34 \times 2240)^{\frac{1}{3}} = 8\) in.

Another rule which has been proposed is—

\[ d = \frac{1}{25} \sqrt{w} \]  \(\text{(2)}\)

Example.—Taking the same wheel as before—

\[ d = \frac{1}{25} \sqrt{34 \times 2240} = 7.8\ \text{in.} \]

where the length is nearly equal to the diameter; but both these give a somewhat smaller journal than in the table above.
There exists a wide difference of principle amongst millwrights as to the mode of attaching the wheel to the axis. It may either be rigidly fixed by cast-iron arms which resist its weight, as a series of columns alternately exposed to a tensile and compressive strain, or it may be supported by tension rods on the principle now most generally practised in the construction of improved iron water-wheels. In the former case the arms are of cast-iron fixed in recesses in a cast-iron main centre, to which they are accurately fitted on chipping strips, and then bolted, as shown in fig. 102. Flat wrought-iron arms are sometimes riveted to the main centre in a somewhat similar manner.

It was reserved for Mr. T. C. Hewes, of Manchester, to introduce an entirely new system in the construction of water wheels, in which the wheels, attached to the axis by light wrought-iron rods, are supported simply by suspension. I am informed that a wheel on this principle in Ireland was actually constructed with chains, with which, however, from the pliancy of the links, there was some difficulty. But the principle on which this wheel was constructed was as sound in theory as economical in practice, and is due originally, it is said, to the suggestion of Mr. William Strutt, and was carried out fifty years ago by Mr. Hewes, whilst at the same time Mr. Henry Strutt applied the principle to cart wheels, some of which, thus put together, were for a long time in use. Mr. Hewes employed round bars of malleable iron in place of the chains, and this arrangement has kept its ground to the present time, as the most effective and perfect that has yet been introduced.

In the earlier construction of suspension wheels the arms and braces were attached to the
centre by screws and nuts, as shown in fig. 103. The arms \( c c \) passed through the rim \( b b \), and the braces \( e e \), are set diagonally in the angle of the rim. This arrangement, although convenient for tightening up the arms and braces, was liable to many objections; the nuts were subject to become loose from the vibration in working, so as to endanger the wheel, and to create a difficulty in keeping it truly circular in form. To obviate this, in 1824, I substituted gibs and cotters, on the same principle as those which secure the piston rod of a steam engine, as shown in figs. 100 and 101: the ends of the arms are forged square, and are fixed in sockets in the cast-iron centre, and are there retained by the gibs and cotters \( ff \) in perfect security from the danger of becoming loose.

The shrouds \( a a \) consist of cast-iron plates cast in segments with curved flanges to receive the bucket plates, which are attached to them by bolts or rivets (\( dd \), fig. 104), and round the inner periphery a projecting flanch (\( b \), figs. 104 and 105) is formed for the reception of the sole plates \( c \). Fig. 104 is a side elevation, and fig. 105 a section of a large shrouding of this description 15 inches deep; \( a a \) the cast-iron segmental plate of the shroud; \( b \) the flanch to which the sole plate \( c c \) is riveted; \( dd \) the curved flanges and bucket plates; \( n \) the bucket. The segments of the shrouds are bolted together by overlap joints, \( jj \), shown also in section in fig. 106. The overlap is placed on the bucket side of the shroud to preserve a smooth face on the outside of the wheel. The arms are attached to the shrouds either by riveting, or, according to my own practice, by dovetailing into recesses cast upon the inner face of the shroud. Fig. 107* represents this arrangement in section, and fig. 108 in plan. The ends of

* Figs. 104 to 109 are enlarged details of the Catrine Wheels, Plates I. and II.
the arm $c$ are forged into a $T$ form, and are fitted into a similar shaped recess on the shroud. To retain the arms in position, it is only requisite to give to the recess and $T$-head a dovetail, as shown at $d$. The boss on the shroud must be tapered gradually down, to avoid injury in casting from unequal contraction in cooling. The arms are usually 2 to 2½ inches in diameter for almost all wheels, and the braces $1\frac{1}{2}$ to 2 inches.

To strengthen the wheel laterally, diagonal arms, called braces, are used ($g\ g\ g\ g$, figs. 100 and 101), and where the wheel is not of great width these braces pass from the main centre on one side to the shroud on the opposite side of the wheel, alternating with the radial arms and fixed in the same manner (fig. 109). Where the wheel is broad I prefer to attach the braces to a middle ring of cast-iron, riveted to the interior of the sole plates in their centre between the shroudings. This ring strengthens the wheel in an important degree, by supporting the bucket and sole plate at their weakest part, where they are liable to
yield to the weight of the water. The middle ring is cast in segments like the shrouding, and the braces are attached in the way already described. Fig. 110 shows the middle ring of a wheel 20 feet diam. and 22 feet broad.

The sole plates are of wrought-iron, ½th inch thick (No. 10 Wire Gauge), riveted together with lap-joints. The buckets are riveted throughout their whole length to the sole plate by a bend at the bottom, or in some cases by a small angle iron (k k, fig. 104). For the further support of the bucket plates, at every two feet of their length they are riveted to bucket stays forming a complete ring of
auxiliary columns round the wheel at every two feet of its breadth. These bucket stays may be of wrought-iron, turned, with two collars, and riveted through each bucket plate, as at $m$, fig. 104, or else of cast-iron, as at $s s$, fig. 111.

*The Overshot Water Wheel.*—By the overshot water wheel was originally intended that form of wheel in which the stream of water was led *over the summit* of the wheel, and thrown upon it just beyond the extremity of the vertical diameter. The water is retained upon the wheel in troughs or buckets, and by its weight continuously depresses the loaded side of the wheel, so as to create a motion of revolution. By a convenient modifi-
cation of the mode of applying the water, however, the stream was laid on to the wheel upon the same side as it approached, by reversing the direction of the spout or sluice, and for this form the name of pitch-back overshot wheel was employed. In present use the term overshot is no longer used strictly, but is arbitrarily applied to all wheels in which the water is laid on near the summit, although high-breast is perhaps a more correct and descriptive designation.

The form of the overshot wheel, as constructed about seventy to eighty years ago, is shown in fig. 112. The wheel revolves on a cast-iron shaft \( a \), with broad flanches to which the wooden arms \( b b \) are bolted, as shown in section fig. 113, with wedges between them to retain them in place. The water is brought from the dam and carried to the summit of the wheel in a wooden trough \( c c \), which is nearly horizontal, as in fig. 112, or has an inclined apron or spout over the wheel, that the water may flow with a velocity somewhat greater than that of the wheel, so as not to be struck by the back of the revolving float-boards, and thrown off the wheel. This apron is usually made to incline at an angle of about 15° with the course, and is 18 or 24 inches long. A sluice or shuttle \( d \) is generally placed at the end of the pentrough, to regulate the discharge on the wheel.

Useful Effect.—Thus provision is made for a constant supply of water falling into the buckets at the summit of the wheel, and by its weight constantly depressing the loaded side, whilst at the bottom it is discharged with the same facility as it was received. Owing to the form of the buckets, however, the water begins to be discharged at a point considerably above the bottom of the wheel, and thus escapes before it has performed all the work due to the fall. The amount of this waste may be reduced—

1. By adopting a curvilinear form of bucket.

* In earlier wheels, in which the main axis is of wood instead of iron, the principal arms are usually placed in parallel pairs extending across the main axis to the shrouding on either side.
2. By only partially filling the buckets.

3. By a close-fitting breast to retain the water on the wheel. But when decreased as far as possible, this waste is still an important item in the performance of the wheel, and hence the useful effect secured is never equal to the work of the water due to the space through which it falls. The fraction expressing the percentage of useful effect derived from a given quantity of power expended by the water is called the efficiency of the machine, and is found by the formula—

\[ m = \frac{100 \, \nu}{\psi} = \frac{100 \, w \, h}{w \, h} \]

\[ \nu = \frac{m \, w \, h}{100} \]

where \( m \) is the efficiency of the machine per cent.; \( \nu \) the work of the water employed per minute, or the weight \( w \) of the water in pounds multiplied by the fall \( h \) in feet, measured from the surface of the water in the pentroutch to that in the tailrace; \( \psi \) the useful effect of the machine, or the pressure \( p \) in pounds moved by the working point of the machine, multiplied by \( h \), the space in feet through which this point is moved per minute, or the number of pounds raised one foot high by the machine per minute. In ordinary overshot water wheels, the useful effect amounts to about 60 per cent. of the power; or a supply of 12 cubic feet of water per second will give one-horse power for every foot of fall. In the improved iron high-breast wheels, as I have been in the habit of constructing them, the efficiency amounts to 75 per cent., in which case 10.8 cubic feet of water per second will give one-horse power per foot of fall. This is about a maximum effect for water machines, and hence the improved high-breast wheel may be considered as nearly perfect as a water machine.

The waste of water from spilling may to a certain extent be reduced by decreasing the opening of the buckets, but with the disadvantage of at the same time increasing the difficulty of the exit of the water at the bottom of the wheel, and of its entrance at the summit. The waste may be further lessened in an important degree by increasing the breadth of the wheel and the capacity of the buckets, but in general it is not advisable that the buckets should ever be more than two-thirds
filled with the average supply of water. The buckets then reach a much lower position before they begin to discharge than when they have been nearly filled. The third means of preventing the spilling of the water is by a curved breast fitting closely to the wheel, as shown in fig. 112, $g g$, and serving, when accurately fitted, to retain the water on the buckets. With low falls this breast is of considerable importance, and secures a considerable increase of efficiency. But with large wheels for high falls, with small openings in the buckets, it is of no value, and does not compensate for its cost when the buckets are made of the best form, so as to retain the water as long as possible upon the wheel; and in these cases the breast is invariably dispensed with.

The Pitch-back Wheel.—The most important modification of the old overshot wheel is known as the pitch-back wheel, in which the course of the current of water is reversed in the pentrough, and laid on the wheel from the same side at which it approaches. In old wheels it was essential, as the wheel generally worked more or less frequently in back water, that the tail-race should always lie in the same direction as the revolution of the wheel. Hence, when the position of the waste water culvert was fixed by other circumstances, it often happened that the millwright was driven to the use of the pitch-back wheel to meet the conditions of the case, and the advantages of this form of wheel were thus forced on his notice. It was perceived that by increasing the diameter of the wheel the water might be laid on at a distance from the summit, and it was shown theoretically that a larger useful effect would be secured by laying it on at about 25° to 30° from the summit than if it took the water over the top. And in this way, when the introduction of iron gave sufficient facility for the construction of wheels of large diameter, the high-breast wheel was adopted, and has maintained its ground to the present time as one of the most perfect and economical machines.

Direction of Tail-race.—It is no longer necessary that the flow of the tail-water should be in the direction of the wheel’s revolution. On the contrary, I frequently take it in the opposite direction or at the side, according as the circumstances of the case determine the position of the wheel and the point of discharge. The old plan of setting
the wheel parallel with the stream is no longer requisite provided proper care is taken to give a sufficient outlet to the water. To effect that object it is essential to sink the bottom of the tail-race two or two and a half feet beneath the bottom of the wheel, and that depth should be continued to the river, so as to form the tail-race into a canal with the water flowing gently and with a comparatively slow motion from the wheel. In this arrangement the bottom of the wheel, when standing in an ordinary condition of the river, is 8 or 9 inches above the water in the tail-race, so that its motion cannot be impeded, and there is left ample space for the rise occasioned by the continuous discharge from the buckets during the working of the wheel. To show how immaterial is the direction of the tail-race, I may add that I have in some cases formed the tail-race into an underground tunnel, in the shape of an inverted syphon. Fig. 114 shows this arrangement as adopted for a mill in 1832, to secure an increase of fall: A shows the wheel and wheel-house, in which originally the wheel was 24 feet in diameter, the fall 22 feet, and the tail-
water conveyed direct into the river Eagley, at b. When replacing this wheel by a new one, it was found that by taking advantage of a bend in the river, and conveying the tail-water to c, an increase of about 6 feet of fall could be obtained. Hence a wheel 32 feet in diameter was adopted, with a fall of 28 feet; and for the tail-race a tunnel d d was constructed, nearly a quarter of a mile long, and passing under the bed of the river at b, so as to meet the stream on the other side of the field at c. The substratum being composed of hard rock and shale, afforded every facility for the drifting of the tunnel, and when complete, the flow of water through it was so exceedingly sensitive, that only a few gallons falling from the wheel into the trumpet mouth at a, immediately caused a perceptible discharge into the river at c, at a distance already stated, of nearly a quarter of a mile. The perfect success of this arrangement caused its adoption in other cases, where the conditions were favourable for carrying it out.

The Catrine High-breast Wheels.—Plates I. and II. illustrate the construction of the improved iron high-breast wheel as applied at the Catrine Works in Ayrshire, between the years 1825 and 1827, on a fall of forty-eight feet. Taking into consideration the height of the fall, these wheels, both as regards their power and the solidity of their construction, are even at the present day among the best and most effective structures of the kind in existence. They have now been at work upwards of thirty years, during which time they have required little or no repairs, and they remain nearly as perfect as when they were erected.

It was originally intended to erect four of these wheels at the Catrine Works, but only two have been constructed. Preparations were made, however, for receiving two others in the event of an enlargement of the reservoirs in the hill districts, and more power being required for the mills. This extension has not as yet been wanted, as these two wheels are working to 240 horses' power, and are sufficiently powerful, except in very dry seasons, when they are assisted by auxiliary steam-power, to turn the whole of the mills.

Plate I. is a plan of the wheel-house, showing the position of the wheels, and the arrangement of the main gearing. The
first pair of wheels is shown in section, to exhibit the main axle, arms, braces, spur segments, and pinions. The other pair are shown in plan, one exhibiting the buckets, and five rows or bucket-stays, while the pentrough, sluice, and regulating gear are shown on the other. It will be seen that the motion of each pair of wheels is transmitted through a common pinion shaft, and thence by another pinion and spur-wheel, by which the velocity is increased to the first motion shaft of one mill, whilst between the two pairs of wheels there is the first motion shaft of another mill geared into the preceding shaft by a pair of large bevel wheels.

Plate II. is an elevation of the wheel-house, with the masonry for supporting the wheels, tail-race, tunnel, &c. The right half of the wheel is shown in section, and the left half in elevation, and there is a section of the pentrough, sluice, and plates, to guide the water into the buckets.

The following are the references to the different parts of the wheel:—

- A, main axis.
  - a a a, arms.
  - b b b, braces.
  - e, pentrough.
  - c, sluice with racks.
  - f, pinion connected with governor.
  - d, joints of segments.
  - e, tunnel running through the wheel-house, and acting as the tail-race.
  - d, pinion gearing into internal segmental spur-wheel on shrouds.
  - e, wheel on the same axis as d, and communicating the power to the pinion f on the first motion shaft.
  - g, galleries to obtain access to the pentrough and other parts of the wheel.

The water is brought from the reservoirs in a tunnel 10 feet in diameter, through the hill part, and thence in a conduit 12 feet wide, and 5 feet deep, arched over. The reservoirs cover 120 Scotch acres, of an average depth of 8 or 10 feet, giving storage room for a large supply of water; and the sill of the reservoir sluice, from which the aqueduct bottom is carried
ON THE CONSTRUCTION OF WATER WHEELS.

level to the pentrough, is 16 inches above the lowest overflow of the sluice on the wheel; hence in dry seasons the water may be drawn off to within 16 inches of the bottom of the lade. At the same time the pentrough is made of a depth of 6 feet, in order that in seasons of plentiful supply the water may be drawn off at the highest level, and the entire fall, as far as possible, rendered effective.

The total supply of water requisite to work the mills when the wheels were started was about 60 tons or 2,150 cubic feet per minute, the wheels revolving at a circumferential velocity of 4 feet a second, or 182 buckets passing each sluice per minute. This gives

\[
\frac{2,150}{182 \times 2} = 5.9 \text{ ft. or 6 cubic feet of water nearly for each bucket of the wheels. The whole capacity of each bucket is } 17\frac{1}{4} \text{ cubic feet; hence, when thus working the buckets were just one-third filled.}
\]

When working to their full power of 240 horses, however, the fall being 48 feet, this pair of wheels would require,

\[
\frac{100 \times 33,000 \times 240}{75 \times 2,240 \times 48} = 98.2 \text{ tons of water per minute,}
\]

if we suppose the useful effect to be 75 per cent. of the water power expended. Now if we take the circumferential velocity at 5 feet per second, at which the wheel should then run, this would give 7.7 cubic feet of water per bucket, or

\[
\frac{7.7}{17.25} = \frac{10}{22}
\]

or one-half nearly, as the ratio of the quantity of water in the buckets to their capacity.

Between these limits these water wheels act effectively and economically.

The wheels are 50 feet in diameter, 10 feet 6 inches wide inside the bucket, and 15 inches deep on the shroud; the buckets are 120 in number, and have an opening of 6 inches; the internal spur segments are 48 feet 6 inches diameter, 3\(\frac{1}{4}\) inches in pitch, 15 inches broad, and have 560 teeth. The pinions are the same width and pitch, and are 5 feet 6 inches in diameter. The intermediate wheel between the pair of segment pinions is 18 feet 3\(\frac{1}{4}\) inches in diameter, 16 inches broad, and 3\(\frac{1}{4}\) inches pitch; and the large bevil-
wheels are 7 feet in diameter, 3½ inches pitch, and 18 inches broad on the cog, so as to be of sufficient strength to convey, if necessary, the united power of the four water wheels.

When viewed from the entrance, the two wheels already completed have a very imposing effect, from their elevation on stone piers. And as the whole of the cisterns, sluices, winding apparatus, galleries, &c., are considerably elevated, they are conveniently approached in every part. Under the wheels there is a capacious tunnel, terminating at a considerable distance down the river and conveying away the tail-water from the wheels.

**Table of Speed.**

| Water wheel 50 ft. 0 in. = 1.5 revolutions = 4 ft. per second. |
|-----------------|-----------------|
| Segments, 48 ft. 6 in. and 1.5 into wheel 5 ft. 6 in. = 13.3 of shaft. |
| Wheels A, 18 ft. 3½ in. and 13.3 into pinion 5 ft. 6 in. = 44 of main shaft to mill. |
| Wheels B, 7 ft. 0 in. and 44 into wheel 7 ft. 0 in. = 44 of shaft to new mill. |
| Wheels S, 5 ft. 9 in. and 44 into wheel 4 ft. 0 in. = 63 of upright in new mill. |

The journals of the main axes of the water wheels and of the pinion shafts are 14 inches in diameter. The first motion shafts are 13½ inches in diameter, and of an average length between the couplings of 19 feet.

The maximum fall may be estimated at 48 feet 9 inches. The distance from the bottom of the wheel to the floor of the tail-race is 3 feet 6 inches, the average depth of tail-water 2 feet, and the distance from the floor of the tail-race to the level of the water in the reservoirs is 50 feet 9 inches.

I have been more particular in describing these wheels, as they are the first erected upon the principle of concentration and combined action. In former cases it had been the custom to erect the wheels near where the work was required, so that it was not unusual to have three or four wheels at a short distance from each other, working independently. This was the case at the Catrine Works before the large wheels were erected. It was found desirable, however, in extending the works, to have the whole power concentrated in one wheel-house, with a uniform fall, so as to simplify the transmission of the power to the different parts of the mills. This was effected in the manner already described with great success, and the result
has been a continuous and efficient supply of power from 1827 to the present time.

Immediately following the erection of the Catrine wheels, those of Deanston, belonging to the same proprietary, were commenced. The Deanston Works were designed upon a much larger scale than even those at Catrine, as it was intended to erect eight powerful water wheels instead of four, as in the

works in Ayrshire. The Deanston Works were erected with two water wheels in the bottom room of the factory about the year 1780, and came into the hands of their present proprietors about 1798 or 1800. After the completion of the alterations in Ayrshire, a similar concentration of the power was desired for Perthshire, and I was requested to prepare both for a renewal of the old wheels and the erection of new ones on a larger and more comprehensive scale. In obedience to these instructions, an entirely new site was selected for the water power, close to
the old mills on the River Teith, and provision made for an increased fall, and an improved application of the water power.

The new wheels as then designed were eight in number, and were placed together in a rectangular building adjoining the old mill, but arranged to afford power to an entirely new establishment surrounding the wheel-house, according to the annexed plan (fig. 115), in which the centre building A is the wheel-house, and the buildings B B B B, surrounding it on all four sides, and three stories in height, contained the machinery driven by the wheels. From this design it will be seen how the power, amounting to 800 horses, was given out on each side by the shafting a a a a, radiating from the centre of the wheel-house, at right angles to the mills on every side. Another shaft was extended in an underground tunnel to the old mill, where it still gives motion to the machinery in that portion of the works.

It is much to be regretted that this design was never carried out in its integrity; but the late Mr. James Smith, so well known as the inventor of the subsoil plough and many other ingenious contrivances, altered the plans after having raised one side of the new mill to a height of one story, when unfortunately it was abandoned for a much less convenient and less perfect structure.

As respects the water wheels, the first two were erected by myself—then in partnership with my much respected friend, Mr. James Lillie—and the last two by Mr. Smith, who, with the Cotton Mills, has since carried on considerable engineering works. The remainder have never been erected. There were, however, several novelties in the arrangement of these wheels which it may be desirable to describe at greater length. The River Teith is the principal feeder, and falls into the Forth about a mile above Stirling. The supply in ordinary seasons is about 260 cubic feet per second, and for many months in the year more than double that quantity. The original fall was about 18 feet; but by the erection of a weir higher up the stream, and the construction of a canal three-quarters of a mile long, it was increased to 33 feet, so as to afford, except in very dry seasons, nearly 800 available horses' power. Of late years this has been increased by a copious supply from Loch Vennaquar, the surface of which has been raised at the cost of the Corporation of Glasgow, as a
compensation for the water taken from Loch Katrine, which falls into the Teith for consumption in the city. From Loch Vennaquar, therefore, there is a continuous supply at all seasons.

The augmentation of the fall from 18 to 33 feet nearly doubled the power for the mills, and also the supply of water which was conveyed direct from the weir to the new wheels in the rectangular building. The water flowed into a wrought-iron pentrough \(A\), fig. 116, supported on iron columns, and delivered the water into the wheels on each side. The wheels were 36 feet in diameter, and of the same construction as those at Catrine. Those on one side of the pentrough, \(d\ d\ d\ d\), gave off their power by an internal spur gearing, and those on the other, \(e\ e\ e\ e\), by an external spur gearing on the shrouds of the water wheels; the shafts carrying the pinions, \(b\ b\), gearing into the water wheel segments, carried also a spur-wheel, \(f\ f\), 18 feet diameter, gearing into a common pinion \(g\). This last pinion was on the central shaft, \(a\ a\), passing along the centre of the wheel-house, and giving off motion to the shafts \(a\ a\) by the bevel wheels \(k\), at the centre of the wheel-house (fig. 117).

Water wheel, 4\:1526 ft. circumferential velocity = 2\:203 revolutions.

<table>
<thead>
<tr>
<th>Ft.</th>
<th>Rev.</th>
<th>Ft. in.</th>
<th>Rev.</th>
</tr>
</thead>
<tbody>
<tr>
<td>33</td>
<td>8(\frac{1}{2})</td>
<td>2:203 into 6</td>
<td>pinion = 13:59 cross shaft.</td>
</tr>
<tr>
<td>Wheels</td>
<td>18</td>
<td>6</td>
<td>pinion = 45:3 of main shaft to mill.</td>
</tr>
</tbody>
</table>

It will be observed that these high-breast wheels have the
peculiar advantage of permitting the use of a sliding or folding sluice, for the admission of the water, which can be adjusted to a very variable fall. So that, at whatever height the water may stand, the velocity at which it enters the wheel will be the same, because it falls over the top of the adjusted sluice. But with this advantage they are apt to become liable to the defect of admitting the water with too much difficulty, a defect which was remedied by the principle of ventilation, which I first introduced in the year 1828, under the following circumstances:—

Ventilation of Water Wheels.— Shortly after the construction of the water wheels for the Catrine and Deanston Works, a breast wheel was erected for Mr. Andrew Brown of Linwood, near Paisley. In this it was observed, that when the wheel was loaded in flood waters, each of the buckets acted as a water blast, and forced the water and spray to a height of 6 or 8 feet above the orifice at which it entered. This was complained of as a great defect, and in order to remedy it openings were cut in the sole-plates, and small interior buckets attached, inside the sole, as shown at b, fig. 111. The air in the bucket made its escape through the openings α, α, and passed upwards as shown by the arrow, permitting the free reception of the water from the pentrough. The buckets were thus effectually cleared of air as they were filling, and during obstruction from back-water in the tail-race the same facilities were offered for its re-admission, and the free discharge of the water from the rising buckets. The effect produced by this alteration would scarcely be credited, as, in consequence of the freedom with which the wheel received and parted with its water, an increase of power of nearly one-third was obtained, and the wheel, which remains as then altered, continues, in all states of the river, to perform its duties satisfactorily.

This difficulty in the admission of the water had often been noticed by the early millwrights, and where it interfered with the working of the wheel, their remedy was to bore holes for the escape of the air in the sole-plate or the start of each bucket. Thus, in his 'Mechanical Philosophy,' Dr. Robison gives a similar instance to that of Mr. Brown; a wheel 14 feet in diameter and 12 feet wide was working in three feet of back-water and labouring prodigiously; three holes, each one inch
diameter, were made in each bucket, when the wheel ceased to labour, and its power was increased one-fourth. The objection to holes in the sole-plate or buckets is a certain spilling of the water over the interior of the wheel, which cannot be avoided. But it must be remembered that air being 800 times rarer than water will escape through a hole at least thirty times faster with

Fig. 117.

the same pressure. Hence, the area for the escape of the air may be made very much smaller than the opening of the bucket.

The amount of power gained, and the beneficial effects produced upon Mr. Brown's wheel, induced the adoption of the ventilating principle as a permanent modification of construction. The first wheel thus designed was erected at Wilmslow in Cheshire, and was started in 1828. It was identically the same with that shown in Plate III., and it was closely followed by a further improvement, as shown in Plate IV.
Close-bucketed wheels labour under great disadvantages when receiving the water through the same orifice at which the air escapes. When, as is frequently the case, the water is discharged upon the wheel in a sheet of greater depth than the opening between two buckets, the air is thus suddenly condensed in the bucket, and re-acting by its elastic force throws back the water upon the orifice of the cistern, and thus allows the buckets to pass imperfectly filled. A similar obstruction occurred whenever the wheel worked in backwater, the water being lifted in the rising buckets, the mouths of which being under water the entrance of air was effectually prevented; and the deeper the backwater the more completely they filled with water and the greater became the difficulty in discharging. Many millwrights to remedy this were in the habit of boring holes in the sole near the start of the bucket, and of narrowing the spout or sluice so as to leave room on each side of the buckets for the escape of the air, means which to some extent remedied the evil of the spilling and sputtering of the water, but in most cases occasioned considerable waste of power, from the water being driven through the openings and falling over the interior of the wheel.

Other remedies have been attempted, such as circular tubes and boxes attached to the sole-plates; but these plans have been generally unsuccessful, owing to the complexity of their structure and the inadequate manner in which they attained the object contemplated. In fact, in wheels of this description it has been found more satisfactory to submit to acknowledged defects, than to incur the trouble and expense of partial and imperfect remedies. In the ventilated wheels about to be described, the perfect escape of the air is effected by very simple means, and great success has attended their application in situations where interruptions frequently arise from excess of backwater or a deficiency of supply.

Low-breast ventilated Wheel.—Plate III. represents a front and side view of a water wheel with ventilated buckets. Portions of the shrouding and segments are removed in order to show a section of the buckets, and the position in which they receive the water.

A is the axle or ribbed shaft, supporting the two main axes, C C, from which the wheel is suspended; B B are the projecting
sockets into which the ends of the malleable arms \(a\ a\) and the
diagonal braces \(b\ b\) are keyed. The arms are 2 inches, and the
braces \(1\frac{1}{2}\) inches in diameter. \(d\) represents the buckets, with
the shuttle which regulates the admission of the water, and
which is made to slide downwards. \(e\) the termination of the
stone breast, and \(n\) the tail-race. This wheel, it will be seen, is
arranged as a low-breast.

The principle of the construction of the buckets is more
clearly shown on an enlarged scale in fig. 3, Plate III., the sole-
plate being abandoned and the bucket plates bent round and
prolonged upwards so as to overlap one another, leaving an
opening, indicated by the arrows, for the escape of the inclosed
air. The bucket plates are connected together by tubular
ferules, or stays, through which a rivet is passed, and riveted
on each side.

The wheel should always, as in this plate, be placed above the
tail-water, and not, as in the older forms of wheels (fig. 112), be
carried down to the level of the tail-race floor; and the breast
of wood, iron, or stone, but usually the latter, which is of so
much importance for low falls in retaining the water on the
wheel, should break off about ten inches from the extremity of
a vertical diameter of the wheel. In fact, the benefits of this
form of breast and tail-race are so great, they should be strictly
carried out where it is desirable to make effective use of the
fall.

In high-breast wheels of 25 feet in diameter, and upwards,
the breast is not required, as the buckets having narrower
openings, and their lips extended nearer to the back of the fol-
lowing buckets, retain the water longer on the wheel. In this
case the loss from spilling constitutes too small a percentage of
the power to compensate for the expense of a lofty and close-
fitting breast. In some cases the breasts have been composed
of iron and wood, but in the best constructed they are of ma-
sory, and allow little or no space between them and the wheels.
It is, however, necessary to be cautious that extraneous matters
do not in that case gain admission to the buckets, as by jamming
between the buckets and the curb they might cause disaster.

The preceding statements, so far as relates to the method of
ventilation, have been principally confined to the form of
bucket and description of water wheel suitable for low falls. It
will now be necessary to describe the best form of breast wheels for high falls, or falls of from one-half to three-fourths of the diameter of the wheel.

High-breast ventilated Wheel.—A water wheel of this kind, constructed for T. Ainsworth, Esq., of Cleator, near Whitehaven, is represented in Plate IV. It is 20 feet in diameter, 22 feet wide inside the bucket, and 22 inches deep on the shroud. It has a close riveted sole, composed of No. 10 wire gauge iron plate, and the buckets are ventilated from one to the other, as shown on a larger scale in fig. 3. The fall is 17 feet, and the water is discharged upon the wheel by a circular shuttle, $A$, which is raised and lowered by a governor as circumstances require. By this arrangement the whole height of fall is rendered available, and the water in dry seasons may be drawn off three or four feet, in order to afford time for the dam to fill in the periods during which the mill is stopped.

The power is taken from each side by two pinions working into the internal spur segments $B B$, and these again give motion to shafts and wheels at $C C$, which communicate with the machinery of two different mills, at some distance from each other.

Arrangement of Gearing.—The position of the pinion, or the point where it gears into the spur segments on the water wheel, whether internal or external, is of importance in every water wheel, but pre-eminently so in those constructed on the suspension principle, which are indifferently prepared to resist the torsive strain to which they would be subjected if the power were taken from the unloaded arc of the wheel. Water wheels of this construction, with malleable iron rods only two inches in diameter for their support, could not resist the strain, but would twist round upon the axle, and destroy the wheel.

It is necessary, therefore, in every case, to take the power from the loaded side of the wheel, as near the circumference as possible, in order to throw the weight of the water directly upon the pinion without transmitting it through a larger arc of the wheel than is absolutely necessary. For this purpose the spur pinion should be below the centre of gravity of the water on the wheel, and therefore more or less below the extremity of the horizontal diameter.

In the old water wheels, where the power was generally taken
from the axle, the whole of the force passed through the arms to the point, and afterwards by a pit-wheel by some multiplier of speed to the machinery of the mill. In the improved wheels this is no longer the case: the arms, braces, and axle have only to sustain the weight of the wheel, and to keep it in shape, and the power being taken from the circumference, considerable complexity is avoided, and the requisite speed far more easily obtained.

*Speed of Water Wheels.*—I have usually made breast wheels for high and low falls, with a velocity between 4 and 6 feet per second at the periphery, and between these limits water wheels may be worked with economy. But for a minimum velocity I have taken 3 feet 6 inches per second, for falls of from 40 to 45 feet, and for a maximum velocity, 7 feet per second, for falls of 5 or 6 feet. The higher velocities, namely, from 5 to 6 feet per second, are now very generally adopted for the best constructed wheels, not indeed on the score of economy in the expenditure of water, but for the purpose of obtaining more easily the requisite speed under the variable conditions of supply. In this climate, where the atmosphere is so much charged with moisture, the rivers, for eight months in the year, generally afford an ample supply of water. It is for this reason that an increased velocity is given to the wheel, in order to increase the power in average conditions of supply, so as to work off the surplus rather than adapt the wheel to the minimum expenditure. It would, however, be advantageous to increase the capacity of the wheel, and work at a velocity of 4 feet, or at most 4 feet 6 inches per second.

*Area of opening of Bucket.*—The width of the opening of the bucket varies according to the point at which the water is laid on. I have made them with openings as low as 4 inches wide and as much as 20 inches, the first being for very high-breast and the latter for undershot wheels, but ordinarily the width is from 5½ to 8 inches for high-breast and from 9 to 12 inches for low-breast wheels. In this matter the millwright must exercise his own judgment, taking into account, 1st, the quantity of water to be delivered upon the wheel; 2nd, the position on the circumference at which the water is to be delivered, a wider opening being necessary for low-breast than for high; and 3rd, he must consider whether the circumstances of
the case in any degree limit the width of the wheel. The width of the opening must be measured perpendicularly to the direction in which the water enters the wheel; thus, in fig. 104, \( x \) is the width of opening.

For high falls, the best proportion of the area of opening of the bucket, that is, the width multiplied by the length between the shrouds, is found to be such that 5 square feet of sectional area of opening is allowed for 25 cubic feet capacity in the bucket. But in breast wheels which receive the water at a height of not more than 10 degrees above the horizontal diameter, 8 square feet should be allowed for the same capacity. With these proportions the depth of the shrouding is assumed to be about 2 or \( 2\frac{1}{3} \) times the width of the opening.

The distance of the buckets apart, measured upon the external periphery of the wheel, I have been accustomed to make from 1 foot to 1 foot 6 inches, low-breast being somewhat further apart in general than high-breast. This proportion fixes the number of buckets in the wheel according to the following table:

<table>
<thead>
<tr>
<th>No. of Buckets</th>
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<tbody>
<tr>
<td>For wheels 10 feet diameter, from 20 to 30</td>
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<tr>
<td>20</td>
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<td>170</td>
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<td>180</td>
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</table>

In setting out the curve of the water wheel bucket in breast wheels, a line \( a \ b \) may be drawn cutting the external periphery of the shroud at the point and in the direction in which it is intended that the water shall strike the wheel after passing the guide plates of the pen-trough sluice. If we then measure a distance \( c \) equal to the distance of the buckets apart, and from the centre \( e \) draw the radius \( d \ c \), the line \( a \ b \) will be nearly the direction of the lip of the bucket and \( e d \) the direction of its start, and the curve must be drawn connecting these lines according to the judgment of the millwright, making some allowance for the velocity of the wheel.
ON THE CONSTRUCTION OF WATER WHEELS.

*The Shuttle.*—The shuttle of these wheels requires a slight notice. The front of the pentrough is of cast iron, in the form of an arc closely fitting the periphery of the wheel, with an opening extending from side to side for the passage of the water to the buckets. This opening is made of such a breadth and is placed in such a position that when the water in the pentrough is highest it will flow upon the wheel near the top, and when the water is lowest it will still be able to enter the buckets near the bottom. This opening is then fitted with inclined guide plates, arranged so as to prevent the water in entering striking against the sole plate or the back of the succeeding bucket. Over the guide plates is a door, or closely fitting sluice, which slides up or down, according to the height of the water in the pentrough, so as to admit a thin sheet of water flowing over its upper edge through the guide plates into the buckets of the wheel. By this arrangement it will be seen that the water is always drawn off at its highest level and the fall economised to the utmost extent. Racks are fitted to the back of the sluice with pinions, by which its position is altered, and the quantity of water flowing on the wheel adjusted.

In the Catrine wheel, Plates I. and II., the pentrough consists of cast-iron plates bolted together and resting on beams supported on one side by the wall of the wheel-house and on the other on columns.

Figs. 119 and 120 represent the water-wheel governor, a very ingenious arrangement, similar in principle to that of the steam-engine, but adapted in its details to a different purpose. It consists of two heavy balls which in revolving take a position further apart or nearer together, according to the velocity at which they are driven. These balls are swung upon the vertical revolving shaft s s supported in the strong cast iron framing A A A. Two cast iron brackets B B on either side of the frame, and bolted to it, support between them a bridge C C, passing over the driving shaft and clutch box, on which the shaft s s rests in a foot step. This vertical shaft is driven by the bevel wheels F and G, the former of which is keyed on the driving shaft b, which is hollow, to allow the shaft a a connected with the gearing of the sluice to pass through it. A third bevel wheel H, is also placed on a hollow shaft, and is driven by the
bevel wheel $c$, revolving of course in an opposite direction to the first wheel $f$.

The governor balls with the radial arms and slotted arcs $f f$ are of the construction usual in steam-engines, but the links $l l$ carry a brass slide $c c$, so that, as the governor balls diverge, this slide is drawn up along the vertical shaft, and as they approach it falls. On the slide is fixed the eccentric cam $d$, shown also in fig. 122 as seen in plan. This cam of course revolves simultaneously with the slide, balls, and vertical shaft $s s$. Attached to the bracket $b$ on one side of the framing is a bent lever $g g g$ carrying at its upper extremity a fork $e e$, and near the bottom a similar fork placed vertically, $h$, fig. 121. The upper fork is moved by the revolving eccentric $d$, the lower fork moves a clutch box which slides backwards and forwards on the shaft $a a$, and engaging alternately with the bevel wheels $n$ and $f$. When the motion of the wheel becomes too slow the balls fall and bring the cam $d$ in contact with a knee of iron $m$ in the upper fork $e e$; this causes the clutch $d d$ to be thrown into gear with the bevel wheel $n$, and the clutch being keyed so as to slide on the shaft $a a$, causes that also to revolve and the sluice or shuttle to be lowered. On the contrary, when the motion of the wheel is too rapid, the balls diverge, the cam $d$ is raised and strikes the upper knee $m$; the clutch is then thrown into gear with $f$; the shaft $a a$ revolves in the opposite direction and causes the shuttle to be raised. At other
times, when the motion does not require adjustment, the clutch is disengaged from both wheels and the whole of the winding apparatus is stationary.

This arrangement of governor is exceedingly compact and effective, and a great improvement on the original condition in which I first found it, with rollers and reversing pulleys. It is free from the objection to which those governors are open which directly bring the sluice gearing into operation and retain it so by their momentum.

As examples of the speed at which this part of the machinery is worked, I subjoin a few examples that are working successfully:—

Governor shaft, . . . 36 revolutions per minute.
Rack shaft, from 0.0314 to 0.058 revolutions per minute.

There is usually a worm on the shaft \( a a \), working into a wheel on a cross shaft; on the cross shaft a second worm working into a wheel on the rack shaft; and a small pinion 8 inches in diameter on the rack shaft gears into the rack upon the sluice. This rack should be jointed to the sluice at the middle, and should be of such a length that the rack shaft and pinion can be placed out of water above the pentrough. But the details of the gearing and shafting by which the motion of the governor is transmitted to the sluice vary with the position of the governor and the circumstances of each particular locality, and they must therefore be left to the millwright’s own judgment. Only it is important to observe that the motion of the sluice should in every case be slow, as in the above examples, or the acceleration or retardation in the supply of water will cause an irregular motion first faster and then slower in the wheel, conditions inadmissible where machinery is employed.

In designing a water wheel the first important consideration is the height of the fall; this taken in conjunction with the intended outlay will fix the diameter of the wheel. We must next determine the form of bucket as already detailed. Then the quantity of water per second in cubic feet must be ascertained, and this will determine the necessary capacity of the bucket and the consequent breadth of the wheel. Here we have to consider also, 1st, that the bucket is not to be more than one-third or one-half filled; and, 2nd, the rate of revolution of
### TABLE OF PROPORTIONS OF WATER WHEELS

<table>
<thead>
<tr>
<th>Diameter of shrouds Ft. in.</th>
<th>Fall Ft. in.</th>
<th>Depth of shrouds in inches</th>
<th>No. of buckets</th>
<th>Opening in buckets in inches</th>
<th>Speed of periphery per second Ft. in.</th>
<th>Diameter of segments Ft. in.</th>
<th>No. of Gogs</th>
<th>Pitch in inches</th>
<th>Breadth in inches</th>
<th>Remarks</th>
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On the construction of water wheels.
the wheel which determines the number of buckets passing the shuttle per second. (p. 140.)

Suppose a wheel, having 5 feet peripheral velocity per second, supplied with 3,000 cubic feet of water per minute, and the breadth of which has to be determined so that the buckets shall be only one-half filled:—

Let depth of shroud = . . . 14 inches
distance between buckets = . . 14 inches
section of water in bucket when full,
at the pentrough = . . . 144 sq. ins.

Here five buckets pass the sluice per second, and each must contain \( \frac{3,000}{5 \times 60} = 10 \) cubic feet of water per second; but they are to be only one-half filled when containing this quantity of water, hence their capacity must be 20 cubic feet. Their sectional area is 1 square foot, and hence 20 feet is the breadth necessary for the wheel.

The table on pp. 148, 149, of the proportions of water wheels which I have constructed, may afford aid to the engineer and millwright designing wheels, in their adaptation to different heights of falls, quantity of water, &c.
CHAPTER IV.

ON THE UNDERSHOT WATER WHEEL.

Before the introduction of iron, undershot water wheels were frequently employed, and were in almost every instance constructed with straight radial floats, as in the annexed sketch, the water being discharged against the float boards, as it rushed with considerable velocity underneath the shuttle. This was the invariable practice down to Smeaton's time even, the prin-

ciple being to employ the impulse of the fluid stream, and not its gravity or weight. Indeed, there appeared to be an impression that this was the more effective and economical mode of application, and probably arose out of the circumstances of the original employment of water as a moving power. The earliest wheels of which we read are undershot wheels placed
between two boats in a flowing stream, and driven by its impulse, and in Smeaton's own time the works for the supply of water to London obtained their power from some magnificent examples of precisely similar wheels, placed in the tidal stream rushing between the clumsy piers of the old London Bridge. In the old time it was no doubt an advantage to have the prime-mover working at a considerable velocity, and an overshot wheel will not do this effectively. Hence wheels were sometimes built of the form shown in fig. 124, the water being carried down from the top of the fall so as to strike the radial floats of the wheel at a very high velocity. Such a wheel is described in Smeaton's reports.

The earliest great advance in the perfecting of the water wheel was effected mainly by Smeaton, and we owe to him the first experimental inquiries on the effect and proper velocity and proportions of water wheels. In all the various applications of water, experimental researches have hitherto been the principal means of advance, and in no department has more labour and talent been expended in such inquiries; the result is, that our hydraulic machinery of the present day is as perfect, and yields as high a proportion of the power to the actual fall of water, as we can ever hope to obtain.

In my own practice I have been accustomed to employ water even for very low falls, solely by gravity, using the arrangement already described, as a low breast wheel, when treating of ventilation, and which is shown in detail in Plate III. This wheel is 16 feet in diameter, 17 feet 6 inches between the shrouds, and is adapted to a fall varying from 5 to 8 feet, according to the condition of the river. The water flows into the wheel at its highest level, over a sliding sluice of precisely the same construction as in high breast wheels; it is retained in the buckets to the bottom of the fall, by the cast-iron and stone breast fitting accurately to the edge of the buckets. The advantages of this construction are manifest, as the water expends its full force on the wheel from the very top of the fall, the
buckets being well ventilated, and having a curvature adapted to the position in which they receive the water. By these means, a greatly increased duty is obtained as compared with the wheels with radial floats acted upon by impulse or gravity, or by both. Besides, with this form of wheel, the spider or suspension principle of construction may be adopted, and the power taken off at once from an internal segmental spur-wheel, placed on one of the shrouds, and a high velocity at once obtained, independently of multiplying gear. The advantages of this form of construction in iron wheels are very great, and, when combined with an economical application of the water, they form a machine probably as effective as any which can be employed for falls of not less than five feet.

Radial float wheels, however, constructed of wood are still in use, and the most important directions in respect to these appear to be to make the depth of the floats large, as compared with the thickness of the lamina of water which strikes them; to place the sluice as close as practicable to the floats; to contract somewhat the aperture of the sluice, and to expand the tail-race immediately beyond the vertical plane passing through the axis, to allow the water escaping from the floats to diffuse itself in the tail-race, and pass freely away. These directions, with the following practical formula for fixing the diameter of the wheel, we have from the dissertation on water wheels in the Engineer and Machinist's Assistant.

Let \( u = \) the velocity of the extremity of the floats; \( N \) the number of turns desired per minute; \( h = \) fall in feet. Assume \( u = 2.4 \sqrt{h} \) for a maximum effect, then the diameter expressed in terms of the velocity and height of fall will be

\[
19.1 \times \frac{2.4 \sqrt{h}}{N} = \frac{46}{N} \sqrt{h} \nearly.
\]

Thus supposing the height of fall \( h = 4 \) feet; number of turns required per minute \( N = 8 \); then the diameter \( = \frac{46}{8} \sqrt{4} = 11.25 \) feet nearly.

Twelve to twenty-five feet is the usual range of diameter for undershot wheels, and the same writer considers 12 to 16 feet to be the most effective; in my own practice, I have found from 14 to 18 feet perform the best duty. Feathering, or inclining the floats, does not appear to increase the useful effect.
The number of floats is usually equal to \( \frac{4}{3} d + 12 \), where \( d \) is the diameter in feet. The thickness of the vein of fluid striking the floats may be from 6 to 9 inches, and the depth of the floats from 18 inches to 2 feet.

M. Poncelet, one of the first authorities on Hydraulic machines, and the first writer on Turbines, has contrived a very important modification of the undershot wheel, which has been used on the Continent with very good effect. A series of experiments led him to the conclusion that the floats should be curved instead of plane, and he deduced that for these wheels the velocity which gives a maximum effect was equal to 0·55 the velocity of the current, whilst it may vary from 0·5 to 0·6. He found the dynamic effect to vary from 50 to 60 per cent. of that of the water, being better for small falls with large openings at the bottom of the flood gate, and less for deep falls with small openings.

For describing the curve of Poncelet's floats, let \( c e \) be the external circumference, and \( a r \) the radius of the wheel; take \( a b = \frac{1}{2} \) to \( \frac{1}{4} \) the fall, and draw the inner circumference of the shrouding; let the water first strike the bucket at the point \( a \) and in the direction \( d a \), draw \( a e \) perpendicular to \( d a \), so that the angle \( e a r \) will be from 24° to 28°. Take on \( a e, f g = \frac{1}{6} a f \), and from centre \( g \), with radius \( g a \), describe the curve of the float.

Fig. 126 represents a good example of Poncelet's wheel. The width of the opening should be contracted somewhat towards the wheel so as to assume the form of the fluid vein, and the bottom may be at first inclined \( \frac{1}{10} \) to \( \frac{1}{12} \) to give the water a greater impetus on the wheel, but over a breadth of 18 or 20 inches at the extremity it should be made to a curve very accurately fitting the periphery of the wheel.

So also the tail-race may be expanded in width and depth to keep the wheel clear of backwater. The buckets are made of
wrought iron of the requisite curve, riveted to the shrouds on each side, and the sole plate is altogether dispensed with; as no resistance is opposed by the air, the buckets are made more numerous than in breast or undershot wheels, and as the wheel carries no weight of water, it may be made comparatively light.
For the number of buckets for wheels of from 10 to 20 feet in diameter, we may take

\[ n = \frac{8}{5} d + 16 \]

Thus for a wheel 15 feet in diameter,

\[ n = \frac{8 \times 15}{5} + 16 = 40 \]

The wheel shown in the figure is 16 feet 8 inches in diameter, and 30 feet wide, and is driven by a fall 6 feet 6 inches high, yielding 20,000 cubic feet per minute. With a circumferential velocity of 11 or 12 feet per second, it afforded 140 horse-power.

This wheel gives a useful effect of 50 to 60 per cent. of the water power employed when well constructed, and may be used with advantage for falls not greater than about 6 feet. Above this the low breast wheel is certainly more advantageous and costs less.

Poncelet made some experiments on wheels of this class, with the friction break. The wheel was 11 feet diameter, 28 inches wide, and with 30 floats. He found the efficiency equal to 52 per cent. when the ratio of the velocity of the wheel to the water was 0.52. Morin has also experimented on these wheels, and for falls of from 3 to 4½ feet, with sluice openings of 6, 8, 10, and 11 inches, he found the efficiency 52, 57, 60, and 62 per cent. respectively.*

* In a conversation with General Poncelet on this subject I found that the wheel which bears his name gives a duty of nearly 60 per cent. of the water employed. This is about the same as my own wheel with ventilated buckets for low falls, where the sole is entirely dispensed with. There is, however, this difference, namely, that in the Poncelet wheel the water is discharged upon the floats from under the sluice, whereas, in that of the ventilated wheel, it is discharged into buckets over the sluice from the upper surface of the fall.
CHAPTER V.

ON TURBINES.

It will be impossible in the present work to enter into details on the theory and construction of the immense variety of prime-movers known under the name of turbines, the development of the principles of which we owe chiefly to continental mathematicians. Two varieties of horizontal wheels or turbines have long been employed on the Continent, which, although ill-devised and ineffective, yet presented evident advantages in their small size, cheapness, and simplicity of construction. These are known in France as roues à cuves and rouets volants, the former being a small wheel revolving on a vertical axis, and having inclined curved vanes or buckets arranged radially. It is placed in a pit so that the water passing vertically through it should act by pressure and reaction on the buckets. The rouet volant differs from this in having the water applied to the wheel at a small part only of the periphery, so as to drive the wheel by impulse. These wheels of from 3 to 5 feet in diameter with nine to twelve buckets are usually made of cast iron, and fixed upon a lever foot bridge, so that they can be slightly raised or depressed. The running millstone is fixed on the upper extremity of the vertical axis, so as to obviate the use of any gearing or belting. In regard to efficiency, the roues à cuves yield about 27 per cent. and the rouets volants about 30 to 40 per cent. of the water used.

General Poncelet was the first to demonstrate the principle and superior advantages of the turbine, and in 1827 M. Fourneyron recalled public attention in France very forcibly to the construction of the horizontal wheels by a turbine very happily conceived and executed. For this invention he received in 1833 a prize of 6,000 francs; and the principles of his machine
have been investigated, and its superiority proved, by the ablest continental experimenters on hydraulics. In its present form it is equal in efficiency to the best hydraulic machines, and in many circumstances is very advantageously employed. Since then the manufacture of these turbines in countries where water power is much depended upon has assumed considerable importance, and very numerous modifications of its form and construction have been adopted.

1. Turbines in which the water passes vertically through the wheel.

Wheels of this class are composed of two annular cylinders, the upper fixed and the lower revolving on a vertical axis. The upper is fitted with guides to direct the water most effectively against similar curved vanes or buckets, turned in the opposite direction, in the lower wheel. The water passes from the reservoir or cistern placed over the upper cylinder, vertically downwards, acting on the revolving wheel by pressure as it glides over the surface of the vanes.

Burdin about 1826 invented a turbine of this description (turbine à évacuation alternative), the efficiency of which was as much as 67 per cent. of the water power expended.

Fig. 127 represents Feu Jonval’s turbine (known also as the Koechlin turbine). The fixed wheel is shown at A A, the revolving wheel at B B. The wheels consist of cast-iron rims, having wrought-iron guides grooved and riveted to them. The running wheel is keyed on the shaft C C, which is supported on a step D, firmly fixed by screws on the cast-iron bridge attached to the
cylinder forming the tail-race. The regulation of the water is
affected partly by a valve resembling the throttle-valve of a
steam-engine and placed beneath the wheel, or in some cases
by a sluice at the opening of the conduit into the tail-race.
This method, when much variation of power is required, reduces
the efficiency of the wheel, but it has the merit of great sim-
plicity and facility of construction. In the construction repre-
sented the vane carries outside the cylinder in which it is placed
a wheel, acted on by a worm from a hand-wheel placed at any
convenient point above the upper cistern. There are also em-
ployed movable divisions by which part of the inner periphery
of the revolving wheel is enclosed, and the water passes through
a narrower annular aperture on the external periphery. This
arrangement is said to have operated effectively in America, so
that a wheel giving 60 H. P. in wet seasons can work at 40
H. P. in dry seasons, without losing more than 15 or 16 per
cent. of its efficiency.

These wheels are placed in an air-tight cylinder, for low falls
at a depth of 4 to 6 feet below the surface, and for high falls
at a distance not exceeding 30 feet above the level of the water
in the tail-race, when lowest; so that in the upper part of the
fall the water acts by pressure, in the part below the wheel by
suction; hence, there is no inconvenience from backwater be-
yond the inevitable reduction of fall, and the waste water may,
if necessary, be conveyed in an air-tight pipe to any convenient
point of discharge, only taking care that its mouth be under
water. In case of breakdown the wheel is very easily ren-
dered accessible. These wheels are said to yield 75 per cent.
of the power expended on falls above 12 feet.

Fig. 128 represents part of a similar turbine by M. Fromont,
which received the Council Medal at the Great Exhibition of
1851. It differs from the last in the method of regulating the
water, and is known as M. Fontaine Baron's turbine. A number
of sluices \( s \) are suspended in the fixed wheel by wrought-
iron rods, and are raised or lowered simultaneously by means of
wheel-work, so as to open or contract the orifices for the passage
of the water. In awarding a medal to this turbine, the jury
made the following remarks on its merits:—1st. It occupies a
small space; 2nd. Turning very rapidly, it may, when used for
grinding flour, be made to communicate the motion directly to the millstones; 3rd. It works equally well under great and small falls of water; 4th. It yields, when properly constructed, and with the supply of water for which it was constructed, a useful effect of 68 to 70 per cent., being an efficiency as high as any other hydraulic machine; 5th. The same wheel may be made to work at very different velocities, without materially altering its useful effect.'—Reports of Juries.

In designing a wheel of this description, we must take a distance $a\ b$ equal to the distance between the floats, or $6.29 \times$ radius. Take the angle $a\ b\ c = 15^\circ$ to $20^\circ$, and draw $a\ c$ perpendicular to $c\ b$. Lay off $d\ c\ f$ equal to $\frac{\delta + \beta}{2}$, where $\delta$ is the angle $a\ b\ c$, and $\beta$ is taken arbitrarily equal to $100^\circ$ to $110^\circ$. Bisect $c\ f$ in $e$, and through $e$ draw $g\ d$ perpendicular to $c\ f$, and cutting $c\ d$ in $d$. From $d$ with radius $d\ c$, or $d\ f$, draw the arc to which $c\ b$ will be a tangent. For the guides, take the angle $f\ h\ k = a$, so that

$$\cot a = \cot \beta + \frac{1}{\sin \delta}$$

draw $f\ m$ perpendicular to $h\ k$, cutting the top of the guide
ON TURBINES. 161

wheel \( n o \) in \( n \); from \( n \) draw an arc touching \( h k \). These directions are from Weisbach.

In America the Koechlin turbine has been experimented upon by the Franklin Institute, with the following results:—The turbine experimented upon is intended to afford 7 horse-power under a fall of 10 feet. It is \( 21\frac{1}{2} \) inches in diameter, \( 3\frac{1}{2} \) inches deep, and intended to make 190 revolutions per minute, giving \( 63\frac{1}{2} \) revolutions of a horizontal shaft to which it is geared 3 to 1. To this shaft was attached a Prony dynanometer, whose lever was 7·96 feet long, giving 50 feet circumference.

Experiment No. 1.—The discharge over a waste board in the tail-race gave the following data for calculating the discharge:—

\[ L = \text{width of waste board} = 3·83 \text{ feet, } h = \text{depth of water on it, } 0·74. \]

Then \( q = 383 \times 3·83 \times 0·74 \times \frac{64}{\sqrt{64} \times 0·74} = 7·468 \text{ cubic feet per second.} \]

Hence the theoretical power = \( 7·468 \times 62·5 \times 9·34 \times 60 = 261,537 \) foot-pounds per minute, = 7·92 horses-power.

It was found that at 63 revolutions per minute of the horizontal shaft 63 lbs. balanced the lever. Hence the power developed by the wheel was \( 63 \times 63 \times 50 = 198,450 \text{ lbs.} = 6·014 \text{ horses-power.} \)

Experiment 2.—The gates from the head-race were so far closed as to reduce the head one foot, and maintain it at that level during the experiment. The depth of water on the waste board was \( 8\frac{1}{2} \) inches, and the fall 8·41 feet. \( \therefore q = 0·39 \times 3·83 \times 0·677 \times \frac{64}{\sqrt{64} \times 0·677} = 6·66 \text{ cubic feet per second.} \)

Hence theoretical power = \( 6·66 \times 62·5 \times 8·41 \times 60 = 210,000 \) foot-pounds per minute = 6·36 horses-power.

It was found that 63 lbs. balanced the lever at 49 revolutions per minute of the shaft. Hence the power developed by the wheel was \( 49 \times 63 \times 50 = 164,350 \text{ lbs.} = 4·98 \text{ horses-power.} \)

The coefficients are then for No. 1, \( \frac{6·014}{7·92} = 0·76. \)

The coefficients are then for No. 2, \( \frac{4·98}{6·66} = 0·78. \)

And making allowance for leakage round the waste board the experimenters conclude that the wheel yielded 75 per cent. of the power expended.
Another experiment on a 60 horse-power turbine gave the following results:

Effective power . 56·30  
Theoretical power 63·92  

0·88.

Perhaps this very large coefficient is not quite reliable.

2. Turbines in which the water flows horizontally and outwards.

In turbines of this class the revolving wheel is placed outside of the fixed wheel, so that the water directed by guide plates on the inner wheel strikes the curved vanes of the outer wheel, and forces them round by pressure and reaction. The water is regulated by a cylindrical sluice fitting between the fixed and movable wheels.

M. Fourneyron's turbine is the chief example of this class. Its advantages, as stated in M. Poncelet's Report to the Academy of Sciences at Paris, are the high velocity at which it may be worked without reducing its useful effect, its small size, and, lastly, its capability of working equally well under backwater. From the experiments of M. Morin, the coefficient of useful effect appears to range from 0·60 to 0·80. On the other hand, it has to the full the defects of this class of machines, requiring the utmost nicety of design and execution, and being very susceptible to injury from small bodies carried into it by the water. It requires for its successful application both a large acquaintance with the principles of its construction and a considerable experience of its use: hence it will be unnecessary to do more in this place than select for illustration one of the most successful instances of their application.

Fig. 130 represents a vertical section, and fig. 131 a plan, of the celebrated turbine erected under M. Fourneyron's direction at St. Blazien, for a fall of 354 feet. This small wheel, of only about 26 inches diameter, is employed in driving the machinery of a spinning factory of 8,000 throttle-spindles, with the necessary preparing apparatus. In comparison with the work it has to perform, it is therefore of a size altogether unique.

The wheel consists of a cast-iron concave plate $t t$, keyed on the main axis $a a$; on this is fixed the annular wheel $s s$, con-
sisting of an upper and lower plate of wrought iron, in which are fixed the 36 curved diaphragms seen in the plan, fig. 131. Opposite each of these curved plates on the outer revolving wheel there is a similar guide on the inner fixed wheel v v, which is carried on a massive cast iron plate attached to the hollow tube b b, in which is placed the main axis. This plate not only sustains the guide plates, but takes off from the main axis the weight of the water, and thus reduces the friction on the footstep. The cylinder c c slides up and down in the larger water cistern, and forms a circular sluice between the revolving and fixed wheel, by which, within certain limits, the
discharge of water and velocity of the turbine can be regulated. This sluice is raised or lowered by 4 rods, \( d d \), which are screwed above into the eyes of 4 pinions (not shown). These pinions all gear into one larger wheel, and in this way the four rods may be raised or lowered simultaneously. The supply of water is brought to the cistern by a pipe \( g \) of 16\( \frac{1}{2} \) inches diameter, and 1,200 feet in length. The spindle works on a steel pivot in a footstep adjusted by gibs and cotters \( e \). This turbine makes from 2,200 to 2,300 revolutions per minute.

Another form of turbine, in which the flow is horizontally outwards, has been made to some extent in this country by Messrs. Whitelaw and Stirrat, and is sometimes called the Scotch turbine or reaction wheel. It is precisely on the principle of Barker's mill, and works by reaction. The principal improvement effected by Mr. Whitelaw is the form of the arms, which are curved in an Archimedean spiral. Fig. 132 shows the method of striking these curves, the centre line of the arm being first
drawn and half the breadth set off on each side of it, so that the capacity of the arm increases from the extremity towards the centre in the inverse ratio of the velocity at each point. Fig. 133 shows the arrangement of this wheel, the water being brought in a pipe A, curved at the bottom, so as to enter the reaction wheel on the under side. The wheel is firmly stayed to prevent its rising from the upward pressure of the water, and carries directly the vertical first motion shaft. The most effective velocity at the extremity of the arms is said to be nearly

\[ v = \sqrt{2gh} \quad (1), \]

where \( v \) = velocity in feet per second, \( h \) = head of water in feet, and \( g \) is the accelerating force of gravity = 32.19.

The following are the rules which Mr. Whitelaw gives for proportioning this machine:

Let \( q \) be the number of cubic feet of water supplied per minute.

\( h \), the height of the fall or head of water.

\( e \), the useful work in units of horse-power.

\[ e = \frac{qh}{696.73} \quad (1). \]

Then for two properly formed jets:

Width of each discharging orifice = \( w_1 = \sqrt{\frac{135e}{1000h\sqrt{h}}} \)

Width of each arm of machine = 4 \( w_1 = w_2 \).

Diameter of machine = \( d = 50w_1 \).

Diameter of central opening = 10 \( w_1 \).

Number of revolutions in a minute = \( \frac{149.4338\sqrt{h}}{d} \).

In experiments with models the wheel is said to have realised from 74 to 77.8 per cent. of the available power.
3. **Turbines in which the water flows horizontally inwards; vortex wheels.**

We owe the invention of this class of turbines to one of my own pupils, Mr. James Thomson, C. E., of Belfast, and probably no turbines are more efficient or capable of more general application to every variety of fall than the vortex wheels which he has constructed. For this reason, and also because from their recent introduction they are less known than the varieties which have been longer in use, we shall illustrate them rather more fully with the aid of working drawings, supplied by Messrs. Williamson and Brothers of Kendal, who, we believe, have at present erected all which are employed in this country.

The peculiarity of these vortex wheels consists in the arrangement of the fixed guide blades on the outside of a circular chamber in which is placed the revolving wheel, so that the water flowing inwards strikes the curved plates of the revolving wheel tangentially, and leaves the wheel at the centre at a minimum velocity; the whirlpool created in the wheel chamber giving to this description of turbine its designation of vortex wheel.

Fig. 134 shows the general form of the guides and passages of a vortex wheel; \( a a \) are the fixed guides, four in number, which direct the water tangentially into the passages of the wheel \( b b \); after having done its work in these, the water leaves the wheel at the open passage at the centre \( c \); \( s \) is the vertical shaft carrying the wheel and communicating its motion to the mill. The chamber in which the guide blades \( a a \) are fixed forms part of the supply chamber, and the supply of water to the wheel may be regulated by altering the position of the guide blades, and thus diminishing or increasing the area of opening between them. For this purpose the guide blades are fixed on
gudgeons $d$ $d$, near their extremities, and are connected by levers and links, so that they may be shifted simultaneously by a spindle. The inner radius of the wheel is usually half the external radius, and the obliquity of the inner ends of the vanes 20° to 30°.

The general principles of these turbines Mr. Thomson thus explained at the meeting of the British Association in 1852:—

' The velocity of the circumference is made the same as that of the entering water, and thus there is no impact between the water and the wheel; but, on the contrary, the water enters the radiating conduits of the wheel gently, that is to say, with scarcely any motion in relation to their mouths. In order to attain the equalisation of these velocities, it is necessary that the circumference of the wheel should move with the velocity which a heavy body would attain in falling through a vertical space equal to half the vertical fall of water, or, in other words, with a velocity due to half the fall, and that the orifices through which the water is injected into the wheel chamber should be conjointly of such area that when all the water required is flowing through them it may also have a velocity due to half the fall. Thus one-half only of the fall is employed in producing velocity in the water, and therefore the other half still remains acting on the water in the wheel chamber at the circumference of the wheel in the condition of fluid pressure. Now, with the velocity already assigned to the wheel, it is found that this fluid pressure is exactly that which is requisite to overcome the centrifugal force of the water in the wheel, and to bring the water to a state of rest at its exit, the mechanical work due to both halves of the fall being transferred to the wheel during the combined action of the moving water and the moving wheel. In the foregoing statements, the effects of fluid friction, and of some other modifying influences, are, for simplicity, left out of consideration; but in the practical application of the principles, the skill and judgment of the designer must be exercised in taking all such elements as far as possible into account. To aid in this some practical rules, to which the author (Mr. Thomson) as yet closely adheres, were made out by him previously to the date of his patent. These are to be found in the specification of the patent, published in the Mechanics' Magazine for January 18 and January 25, 1851.'
Fig. 135.
Elevation.
Mr. Thomson claims for his wheel the peculiar advantages—
(1) That the injection passages are large and well formed. (2) That it permits the employment of a most advantageous mode of regulating the power, by contracting the areas of the injection passages, without reducing the efficiency of the machine. (3) That the maximum velocity of the water in the wheel does not exceed that due to half the fall. (4) That the centrifugal action of the water tends to regulate the velocity of the wheels under a varying load.

In his paper, Mr. Thomson describes a vortex for a fall of 37 feet, and for an average supply of 540 cubic feet per minute, yielding 28 effective horse-power. The speed, 355 revolutions per minute; diameter, 22½ inches; and extreme diameter of case, 4 feet 8 inches; also a low-pressure vortex for a fall of 7 feet, for an average supply of 2,460 cubic feet per minute, and yielding 24 horse-power, at 48 revolutions per minute. Another he has constructed for a fall of 100 feet, and a fourth of large size, calculated for working at 150 horse-power, on a fall of 14 feet, and through a considerable part of the year submerged under 7 feet of backwater. These data will sufficiently show the capabilities of this machine, and its adaptation under great varieties of circumstances.
Figs. 135 and 136 exhibit an elevation and plan of a high-pressure vortex wheel, constructed by Messrs. Williamson and Brothers of Kendal. It is of 5 horse-power, on a 30 feet fall, and consumes 118 cubic feet per minute. The water is conveyed to the wheel in the 9-inch pipe \( \Lambda \), at a velocity of 4.4 feet per second. \( \Sigma \) is the supply chamber, or wheel case, fixed on masonry in the tail-race \( \xi \), from which the water passes away by the tunnel \( \eta \). In the drawing the tunnel is shown closed, as is occasionally necessary, for access to the wheel or other purposes. \( \pi \) is a platform just above the ordinary level of the water; \( \sigma \) \( \sigma \) is the first motion shaft, to which the wheel is attached, and which is supported on the footstep at \( \sigma \), and by pedestals attached to the supply pipe \( \Lambda \). 

Fig. 137 shows the wheel case in section. \( \Pi \) \( \Pi \) is the supply chamber or guide blade chamber, cast in parts and bolted together as shown; \( \omicron \), the wheel itself, about ten inches in diameter, and composed of wrought-iron plates with wrought-iron curved vanes; \( \pi \pi \) the four guide blades, in this wheel fixed and let into grooves cast in the cover and bottom of the chamber; \( \xi \xi \), four bolts tying the cover and bottom of the supply chamber together to strengthen it against pressure; \( \lambda \) the supply pipe as before, and \( \xi \xi \) the openings in the centre of the wheel.
for the escape of the waste water after it has done its work on the wheel. The joint between the wheel and its case is made by means of the accurately fitting annular parts $L L$, adjusted for the wheel to run without friction by bolts $n n$ in the upper piece. $s s$ is the first motion shaft resting on a lignum vitae pivot firmly fixed in the footbridge $c$, which is bolted on below the supply chamber, the height of the pivot as it wears being adjusted by the screw $l l$. The pivot is lubricated by the water in which it works spread over it by a radial groove. In other cases Mr. Thomson makes the shaft to terminate in an inverted cup containing a concave brass disc working on a fixed steel pivot, with a radial groove for spreading the water. He does not consider the lubrication with oil so essential as other engineers insist, and believes the cases in which turbine pivots have been rapidly destroyed to be attributed to the absence of
a proper provision for the escape of the air between the rubbing surfaces. Fig. 138 represents a half-plan and half-horizontal section of the same wheel, the same letters of reference being used as in fig. 137.

Fig. 139 exhibits the arrangement, in sectional elevation, of a low-pressure vortex wheel with its pentrough and tail-race. This wheel is of 34 horse-power, with an effective fall of 14 feet 3 inches, and a supply of 1,680 cubic feet per minute. The wheel is 46 inches in diameter, and makes 94 revolutions per minute. A A are the four supply pipes, 2 feet in diameter, so that the water in them has a velocity of about 2·3 feet per second. B is the square supply chamber, C C the tail-race, and D D the conduit and pentrough. The water as it arrives passes through a perforated metal strainer E E, to prevent the choking of the narrow passages of the wheel by floating leaves, &c. Over the four supply pipes A A is fixed a circular cast-iron plate G G, with four holes corresponding in one position with the trumpet
mouths of the supply pipes. On the edge of this plate is a rack into which the pinion $g$ gears, so that by moving the worm and wheel $h$ the sluice plate $a a$ may be revolved and the entrance for the admission of the water to the wheel more or less closed or opened. This is an effective and inexpensive means of regulating the power of the wheel, where the supply of water is abundant, and it is not necessary to economise its expenditure to the utmost extent. $s s$ is the first motion shaft, and $t t$ the bevel wheels by which it gives off the power of the wheel to the mill. $k$ is the foothbridge, carrying a step which can be raised by the lever $l l$ as it wears away. Fig. 140 exhibits a half-plan and half-section of the wheel and supply chamber. $a a$, as before, supply pipes, $w$ the wheel itself, $g g g$
fixed guide blades, the regulation of the wheel being effected by the sluice as before described. The first motion shaft, L central opening for the escape of the water, M wheel cover, forming at its inner periphery a close and accurate joint with the revolving wheel.

Another plan which has been adopted with these wheels for regulating the speed, when they are applied to high falls, is to bring the supply pipe when near the wheel into a horizontal direction, fitting to it an ordinary sluice such as is used in high-pressure mains. A 10 horse-power turbine, on a fall of 80 feet, has been erected on this principle by Messrs. Williamson and Brothers in Yorkshire. The wheel is only 13 inches in diameter, and consumes 90 cubic feet of water per minute, which is brought a distance of 340 yards, in a 9-inch pipe, the pentrough and strainer being placed at the upper end, and the sluice at the bottom close to the wheel.

But beyond question the most economical arrangement for regulating the expenditure of water, although somewhat more complicated in its details, is the adjustment of the guide blades themselves in the manner already alluded to. Fig. 141 shows a plan of a turbine, arranged with movable guide blades. A A two supply pipes; B wheel cover; C C C C bell cranks connected together by links. The whole of these bell cranks are worked by a vertical spindle D, and worm and wheel in the mill; they carry in the supply chamber links shown by the dotted lines, by which the guide blades g g g g, movable on centres at h h h h, can be opened or closed.

These turbines yield 75 per cent. of the power expended, and are therefore as efficient as the
best water wheels or turbines. They work equally well under backwater, and, if it be necessary, they can be placed at any height less than 30 feet above the water in the tail-race, the lower part of the fall being made to do its work on the wheel by suction in pipes descending from the central discharge orifice, and terminating in the water of the tail-race.

In America, turbines of various kinds have come into extensive use, and some erected there are of unprecedentedly large size. The better forms have been copied, in their main features, from European machines already described, with some variation in the constructive details. Thus Mr. Boyd has introduced a diffuser, or annular mouth-piece, round the outer or revolving wheel of the Fourneyron turbine, instead of permitting the water to escape into the free space of the tail-water. He has also, to avoid the difficulties arising from the rapid wear of the

footstep working under water in large turbines, suspended them from above, instead of supporting them below. This he accomplishes by the peculiar form of bearing shown in fig. 142. The top of the main vertical shaft of the turbine c is cut so as to form a series of bearing surfaces; these fit into corresponding grooves in the metal of the suspension box α, which is supported, as shown in the elevation, by gimbals. The height of the shaft can be accurately adjusted by screws, so that the weight of the turbine may rest on the collars in the suspension shaft, and the lower bearing beneath the water serve merely to retain the shaft in its place. By lining the suspension box α
with a soft metal, principally tin, melted and poured in with the necks in place, sufficient accuracy can be attained to prevent any undue strain on particular collars. This form of bearing is said to have been successfully employed, and to obviate the difficulties of oiling beneath the water.

Efficiency of Turbines.—It may be useful to revert here for a moment to the experiments which have been made upon different forms of turbine to ascertain their relative efficiency. In all these machines, the useful work rendered is less than the entire force of the fall of water which acts upon them by the loss of work expended in overcoming the friction and inertia of the machine, together with the loss from the *vis viva* expended in shocks and impact and passing away in the water of the tail-race, and from other causes in special cases. The fraction which expresses the ratio of the total work expended by the water to the useful work returned by the machine is the *efficiency* of the machine. Commonly we express this ratio in a percentage, taking the work of the fall as 100, and calling the work accomplished useful effect or return.

For the turbines of Fontaine and Jonval, in which the flow is vertical, a return of 70 to 72 per cent. was obtained by M. Morin; 67 per cent. by MM. Alcau and Grouvelle; 74·5 per cent. by MM. Hulze, Borneman, and Bruckman.

The turbine of Fourneyron yields, according to M. Morin, 74 per cent.; but 64½ according to MM. Redtenbacher and Marozeau; M. Fourneyron has obtained results varying from 65 to 80 per cent. according to the fall and immersion of the turbine. The turbine of St. Blazier is said to yield from 70 to 75 per cent.

The turbine of Poncelet, in which the water is laid on tangentially, yields from 65 to 75 per cent.; according to M. Hulze, 70 per cent.

The turbine of Cadiat, with an outward flow like that of Fourneyron, but regulated by an exterior circular sluice, gave 65 per cent. to M. Redtenbacher.

The reaction wheel of Whitelaw and Stirrat has yielded in experiments with models 70 to 78 per cent.

Mr. Thomson's vortex wheel yields, according to his experiments, 75 per cent.
ON TURBINES.

All these returns appear to approximate closely to the duty performed by water wheels; probably not so high as that given by a well-constructed iron water wheel, but the difference is inconsiderable. Smeaton's experiments gave, on his overshot wheels, as much as 76 per cent., and the results obtained from experiments on the breast-wheel, with ventilated buckets on a large scale, gave nearly 78 per cent. of the actual power of the water employed.

Certain advantages, it must be admitted, are obtained by the turbine in certain localities under favourable conditions; but it is doubtful whether they are equal, either on the score of expense or ultimate efficiency, to well-constructed water wheels. In some situations favourable for their reception they are doubtless preferable in effecting a reduction of the original cost, but taking into account the conveyance of the water in pipes and other charges, it will be found as a general rule that the difference is not considerable, and that a well-constructed water wheel of 50 years' duration is an effective and excellent substitute for the turbine.

Since the first edition of this work another improved turbine, by Mr. Schiele, has been introduced, of which the following is a description.

Schiele's turbine (patent of 1863) is constructed for the purpose of regulating and adjusting the supply of water to the amount of power required, and so to proportion the parts as to maintain uniformity of speed and economy in the free use of the water; to float the turbines partially in the water so as to reduce the friction on the footsteps; also to allow the dams or reservoirs to be run empty towards closing or stopping time; and to prevent the entrance of leaves or other floating substances into the working parts. This turbine, moreover, combines the advantage of being perfectly self-acting, and working up to nearly a maximum effect. In addition to the above it is stated by the constructors that, exclusive of its simplicity and comparative cheapness, the tangential entrance of the water and its radial delivery is effected with facility, and that it works freely in back water under the varied conditions of the height of the fall, as it is increased or diminished, without change of velocity when the supply is sufficiently abundant, admitting of a
wide range of speed without sensibly diminishing its useful
effect.

These turbines are so constructed as to admit the water on
the top of the tube at a, fig. 142, when the sluice in the
watercourse is fully opened and fixed in that position. The
tube a leads the water into the tubular foundation plate b,
from whence it rises into the circular tube c, surrounding the
spirally formed cast-iron guide-blades d, which project higher
than the ring or tube c. The base or inner guide for the
water is formed by a cone, which diminishes the area of the
passages uniformly, so that if an outer ring closes the lower
projecting half of the guides, their interior area would be
diminished one-half, and so on with any other fractional
dimination of the area. The water passing through is not de-
levered direct but sideways round the spiral openings, each
extending from one-quarter to sometimes one-half the circum-
ference, and rising to a greater height than is usual in turbines,
whereby an almost tangential direction is given to the water,
thus preventing shocks, and enabling strong cast-iron wings
to be used for the turbine wheel f. These wings, where they
face the guides d are partly cylindrical, having a sharp cutting
edge forward to cut to pieces any obstructions. The wings e
also taper in their curved form to a fine edge. This construction
allows of a considerable reduction in the number of wings,
whereby the passages of the turbines are made sufficiently large
in most cases so that strainers, with rods three to four inches
apart, are quite sufficient to prevent the entrance of materials
interfering with the safe working of the turbine. Should sticks
enter between the wheel and guides, they are immediately cut
off by the sharp edges of the wings e and the spiral guides d,
which form a scissor-like action and divide them. If this should
fail by too great a quantity having entered at once, then
turning the turbine partly round backwards, will clear and open
the passages; or the lifting out of the wheel, sliding on its
spindle to above the surface of the water, may be accomplished
with great facility and expedition, when the obstruction may be
removed by flushing the water through the guides. The wheel
is now dropped down again into its place on the coupling,
and secured in that position by a wedge above the water level, &c.
For clearing obstructions out of the hollow foundation plate \( b \), a flushgate \( g \) is occasionally opened. Should ice come down with the water in too large quantities, another strainer is placed before the water entrance to the guide \( d \), and an occasional flushing out is required. The wings \( e \) above mentioned are cast to a disk \( f \), which is fixed to the spindle by resting on a coupling plate \( i \), provided with pins which enter through the disk \( f \). A wedge \( k \) holds the disk or turbine wheel \( f \) down to the plate \( i \). The pivot on which the spindle turns is shown by dotted lines. It is made to the antifriction curve and is supplied with oil by the tube \( l \). The water passages between the wings \( e \) are adjustable in their heights by a disk \( m \) cut out for the passage of the wings \( e \). A casing \( n \) of the form of a double ring is connected to the under side of the disk \( m \), covering those portions of the wings which are not at that moment in use. The inner ring, which slides up and down between the wings \( e \), and the guides \( d \), adjusts the areas of the latter in the same proportion as the disk \( m \) adjusts the wheel passages, thus maintaining the requirements of a good turbine for varying powers. The sliding of \( m \) and \( n \) up and down is accomplished by means of bolts passing through the wings \( e \), and fixed to the cover \( o \) over the wheel \( f \). The cover \( o \) fits over the cylindrical portion of the wheel and allows of a constant leakage. It has a central pipe \( s \), fixed to and opening into it, which sliding on the spindle by its upper end, gives the rising and falling motion of \( o \), \( m \), and \( n \), a secure guiding. In order to lift \( o \), and by it \( m \) and \( n \), it is only necessary to admit water into the central pipe, which, when rising therein, produces a great pressure upwards, owing to the large surface of \( o \). No sudden overstroke of this adjustment can happen, as the column of water would at once diminish and check the moving force. The pressure between the disks \( m \) and \( f \), produced by the force or fall of the water, tends to counteract this useful effect, but the circular velocity of the water under the cover \( o \) balances it, and to such an extent, that at any sudden start of the turbine—caused by a considerable portion of the load being suddenly taken off—the cover \( o \) rises at once, not waiting for the regulating supply of the water. The speed of the turbine is
maintained by a ball governor regulating the supply under the cover o. The height of the water level is maintained by the float p, adjusting the turbine, when the governor would allow too much water to pass the turbine. This is more particularly useful where turbines run in connection with steam engines which supply by their governor the remainder of the power required when the water supply is insufficient. The pressure produced under the central portion of the disk f takes away the greater portion of the weight resting on the footstep of the spindle. The float p, when set out of action as a float, may be held in such a position as will allow the turbine to consume larger quantities of water, giving correspondingly greater power so as to run reservoirs or rivers empty before the completion of the day's work. The water issuing from other turbines generally indicates a separation of currents—not a compact water-mass—in a direction not radial to the wheel. This turbine, having the two disks f and m projecting considerably beyond the tips of the wings e, and the inclination of the wings being nearer the tangential direction than in otherwise constructed turbines, the issuing water is much more compact and efficient in its uniform and almost radial flow on leaving the wheel; a great variation of speed is thus admissible before such unfavourable angles of discharged water are caused as would materially influence the useful effect obtained.

4. Water Pressure Engines.

In the water pressure engine the power obtained from the pressure of a column of water is employed in generating a reciprocating instead of a rotatory motion. Engines of this description have long been employed in the mining districts of the Continent, but in England their use appears to date from 1765, when a single-acting water pressure engine was erected for draining a mine in Northumberland by Mr. Westgarth.

For the most successful application of these engines, as regards efficiency, it is necessary that the motion of the water should be slow, and as far as possible without shock. Three to six strokes per minute, or a velocity for the piston of one foot per second, is
about the ordinary speed. The stroke also should be long, and therefore 'the most advantageous use to which a water pressure engine can be put is the pumping of water, to which slow motion and a long stroke are well adapted, because they are favourable to efficiency, not only in the engine but in the pump which it works.'—Rankine.

The valves now usually employed in these engines are solid pistons working in the supply pipe, with leather or metal packings. Figs. 143 and 144 showing the valves for a single-acting engine will sufficiently indicate the principle. A A is the supply pipe, B B the entrance to the cylinder, and C C the eduction pipe. When the cylinder is being filled, fig. 144, the valve D is below the entrance and closes the eduction pipe. When, however, the cylinder is emptying, fig. 143, the valve is raised and then closes the supply pipe. Deep notches are cut in these valves in order that they may very gradually open and close the passages to prevent shock.

These valves are usually worked by a small water pressure engine, acting in the reverse direction to the general engine, and worked from it by tappets. Fig. 145 shows such an arrangement, from the single-acting engine of M. Junker.

In this drawing C represents the upper edge of the main cylinder, s the supply pipe, d the port connecting the main cylinder with the valve chest, g the discharge pipe: E is the valve, which when above d, as in fig. 145, permits the water to escape from the cylinder, and when below d, closes the discharge pipe and opens a passage from the supply pipe. The area of the valve E is made less than that of the piston F, with which it is connected by a rigid rod. Hence the pressure of the water between E and F tends to raise them both. The upper side of F is provided with a trunk working in a stuffing box in the top of the valve cylinder. The use of this is to diminish the effective area of the upper side of the piston F,
so that it shall not be more than is requisite to enable the water when admitted through the port \( i \) to overcome the upward tendency of the piston together with the friction of the piston and valve.

\[ \text{Fig. 145.} \]

\( H \) is the supply pipe, and \( M \) the discharge pipe of the auxiliary engine for working the valves; \( K \) is the valve of this engine which regulates the admission and discharge of the water through the port \( i \), precisely in the same manner as the valve \( E \) regulates the admission and discharge from the main cylinder; \( l \) is a plunger of the same size as \( K \), that the pressure between them may be equalised and not tend to move \( K \) upwards or downwards. The rod to which \( k \) and \( l \) are fixed is connected by means of a train of levers and link-work with a lever carrying the crutch \( r \). This is alternately raised and depressed by a tappet rod carried by the piston in the main cylinder \( c \).

Suppose now the piston valve \( E \) is raised, and the water discharging from the main cylinder, as shown in fig. 145. When the main piston approaches the bottom of its stroke, the upper tappet strikes the lower hook on \( r \) and depresses it, along with the auxiliary valve \( k \). This admits water from \( s \) through \( H \) and \( i \) to the upper side of the counter piston \( r \), so as to depress it along with the valve \( E \). The valve \( E \) then closes the discharge pipe, and admits water from \( s \) to the main cylinder; the piston rises, and near the termination of its stroke strikes the upper hook on \( r \), and raises the auxiliary valve \( k \). This allows the water to discharge from the upper side of \( r \), and then the surplus pressure on its lower side lifts it with \( E \), and the operation is repeated.*

* The description of this valve is abridged from Mr. Rankine's and Prof. Weisbach's Treatises.
Fig. 146 exhibits an elevation of a single-acting water pressure engine, which I erected some years since in Derbyshire for the purpose of raising water from the Alport lead mines. It does not widely differ in its action from that of M. Junker just described. \( C \) is the main cylinder, and \( P \) its piston or plunger. \( S \) the supply pipe, and \( D \) the discharge pipe, connected with the valve apparatus \( E \). \( F \) is the cataract or auxiliary engine for working the valves. The piston \( P \) is connected with the sway beam \( B \), which at its other extremity is attached to the oscillating connecting rod \( A \), which is fixed on a pivot or joint at its lower extremity. By this arrangement the piston is permitted to rise vertically, and the spear rod of the pumps \( Z \) is also nearly vertical in its movement. A heavy balance weight \( W \) is attached at the opposite end of the sway beam to balance the pump rods at the other, so that the piston should fall in the cylinder \( C \) at an appropriate velocity, and without shock.

Mr. Joseph Glynn erected a similar engine at the same mines in 1842. This engine was of larger size, namely, with a 50-inch cylinder, and 10 feet stroke. The head of water is 132 feet, and lifts a plunger rod 42 inches in diameter, affording a power of about 150 horses when working at its greatest velocity.

Hydraulic engines of this description are not the most effective even for pumping water, as the motion is exceedingly slow, and the friction of the water and the organic parts of the engine absorbs a considerable amount of the power employed. To remedy this evil it is found desirable in some cases, wherever the fall is not too high, to introduce the water-wheel with cranks and spear rods, communicating a reciprocating motion to the pumps in the shaft of the mine.

In mountainous countries, where high hills descending from great elevations are found, the reciprocating engine is probably the best application for draining purposes, as the motion is conveyed direct from the main cylinder to the pumps, and that, probably, at the smallest outlay of capital, when a supply of water is at hand.

It is otherwise when large supplies of water on low falls are present. Then the water-wheel, with its machinery, is
the most effective and the most economical application of the power.

Fig. 146.

The recent introduction of the turbine may, however, effect a change in this class of machinery, as it is admirably adapted to
high falls, and may be advantageously employed at a moderate cost. The great objection to its use in this form is the great velocity it attains on high falls, and the consequent reduction which would be requisite to work pumps at 10 to 12 strokes per minute, when the machine itself is moving at the rate of 400 to 500 revolutions per minute. This appears to be the only drawback, and it is not improbable that the simple cylinder here described may, under certain conditions, be best adapted to meet all the requirements of raising water from deep mines with the aid of convenient streams on high falls.
CHAPTER VI.

ON THE PROPERTIES OF STEAM.

Before considering the application of the steam engine as a prime-mover, it may be interesting to know something of the properties of steam by which it is moved, in regard to pressure, temperature, and density, as ascertained by various philosophers since the days of Newcomen and Watt. Of late years a great change has gradually taken place in the system of working the steam engine. At the time of the introduction of the double-acting engine of Watt, the makers of engines never dreamed of employing steam at a greater pressure than 10 lbs. on the square inch, and up to 1840 that was the maximum pressure at which steam engines were worked, with the exception of a few constructed on Wolf’s principle of double cylinders, where the steam is first admitted to the piston of the smaller cylinder at a pressure of 30 to 40 lbs. per square inch, and after having performed its office there, is allowed to expand into the second cylinder of three or four times greater capacity, and thus to unite its force with that of the small cylinder, as it moved from one extremity of the stroke to the other. To work this description of engine with high-pressure steam, it was necessary to proportion the strength of the parts of the engine as well as the boiler to a much greater extent of pressure than in the double-acting engine of Watt. Hence it was soon found that the waggon form for the latter, as employed by Watt, was not calculated to resist a pressure exceeding 10 or 12 lbs. per square inch without the introduction of numerous wrought-iron stays to retain it in form. To raise steam for the compound engine such a boiler was wholly inadequate, and a series of small boilers, with hemispherical ends, were introduced in its stead wherever steam of high-pressure was required.
ON THE PROPERTIES OF STEAM.

The single pumping engines of Watt, and the compound engines of Wolf, employed at the mines in Cornwall, gave, however, extraordinary results as regards the work accomplished for the quantity of coal consumed, which was less than half the quantity used in the rotative engines employed in mills. It was also asserted that the double cylinder engine in use on the Continent (but chiefly made in this country) was performing a more satisfactory duty than could possibly be attained by the single cylinder low-pressure engine.

These assertions, often repeated, and the returns of Cornish engines, published from year to year, led to a close inquiry into the subject, first in my own works at Manchester, and subsequently before the British Association for the Advancement of Science, where the whole question was ably discussed, and ultimately led to a better system of working in factory engines, with a saving of one-half the fuel formerly consumed in effecting the same quantity of work. In these investigations it was found that the compound engine had no advantage over the single cylinder engine, as constructed by Watt, when worked at the same pressure of steam and the same rate of expansion; that is, a single cylinder engine, with properly constructed valves, having the power of cutting off the steam at any point of the stroke, is quite as effective, and more simple in construction, than the double cylinder engine. It is true, that at first the double cylinder engine had an advantage over the single cylinder engine in its greater uniformity of motion, but this is no longer the case, as an increase of the velocity of the piston from 240 to 320 and 360 feet per minute effectually remedies that evil, and increases the power of the engine in the ratio of the increase of speed.

Thus it will be seen that a great change has come over the system of employing steam; the pressure is quadrupled in factory engines, and more than doubled in marine engines. Every engine of recent construction is provided with boilers of great resisting powers, and on an average cuts off the steam in the cylinder at one-fourth, and at other times one-fifth or one-sixth of the stroke, the steam acting by expansion alone during the remaining three-fourths, four-fifths, or five-sixths, as the case may be. This system is found to be of great value, as the
quantity of fuel consumed does about double the amount of work which could be got out of it on the low-pressure principle.

The important results already obtained by a judicious system of working steam expansively, has given a powerful stimulus to the extension of our commerce and manufactures, and the question naturally arises, whether or no we have attained the full benefit from the introduction of the methods of working now employed, or whether we may not reap a still greater advantage from progressing in the same direction and using steam of higher pressure, expanded to still greater lengths than has yet been attained in our present practice. This is a question which remains for solution, and it appears most desirable that we should ascertain by direct experiments to what extent of pressure and expansive action we may safely venture with perfect security to the boilers and the working parts of the engines. Assuming for a moment that an increased pressure, accompanied by increased expansion, would in the same proportion increase the economy of working, we have then to consider the capabilities of our vessels for resisting those pressures. And lastly, the observation of the action of steam in expanding has led many to expect still further advantage from the use of superheated or gaseous steam. To make sure progress in either of the directions here indicated two things are necessary: we must cultivate a more intimate acquaintance with the resisting powers of materials, and the strength of vessels of different forms, before we can assure ourselves of success; and we must attain increased and increasing knowledge of the properties of the agent we employ under the various conditions of expansion and superheating. In regard to the first of these requisites a steady progress has been made, and experimental inquiries have been extensively carried on in regard to the resisting powers of vessels and the causes of their failure, and the difficulty of constructing boilers to resist very high pressures has been greatly diminished. Our knowledge of steam has also rapidly increased, and many of the necessary questions relating to its properties have been for ever set at rest by the recent and classical labours of Regnault, carried on at the instance and with the assistance of the French Government. The questions of the density and law of expansion of steam, however, still require solution.
ON THE PROPERTIES OF STEAM.

They have been investigated, from a theoretical point of view, with considerable success, by Mr. Rankine of Glasgow. The experimental inquiry I have undertaken in conjunction with my friend Mr. Tate, and a part of the results, comprising experiments up to a pressure of 60 lbs. per square inch, will appear in the Transactions of the Royal Society. We are now preparing to enter on the more arduous and dangerous task of ascertaining the density, volume, &c., at much higher pressures. The accumulation of facts on this subject, bearing directly upon the application of steam, cannot be otherwise than acceptable to the general reader, and I shall, therefore, without further preface, insert such an abstract as bears directly on the subject under consideration:

General Laws of Vaporisation.

When a liquid is heated in any vessel, its temperature progressively rises up to a certain point, at which it becomes perfectly stationary. At that point the heat continuously absorbed becomes latent, or is no longer registered by the thermometer; ebullition commences, and vapour, of a bulk enormously greater than that of the liquid from which it is formed, rises in bubbles and fills the vessel. In this condition the temperature of the liquid is perfectly constant; no urging of the fire will cause it to rise; the heat, absorbed continuously, expands itself in effecting that change in the state of aggregation of the liquid which we know as vaporisation.

This remarkable constancy in the temperature of liquids undergoing vaporisation in open vessels has long been known and applied to the graduation of thermometers. The point at which a liquid boils in an open vessel is called its boiling point. The following table gives the boiling points of some of the more important liquids:

<table>
<thead>
<tr>
<th>Liquid</th>
<th>Boiling Point Fahr.</th>
<th>Authority</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>212°0</td>
<td>Kopp</td>
</tr>
<tr>
<td>Ether</td>
<td>94°8</td>
<td>Pierre</td>
</tr>
<tr>
<td>Alcohol</td>
<td>173°1</td>
<td>Marignac</td>
</tr>
<tr>
<td>Sulphuric Acid</td>
<td>640°0</td>
<td>Regnault</td>
</tr>
<tr>
<td>Mercury</td>
<td>662°0</td>
<td></td>
</tr>
</tbody>
</table>

We have said that the boiling point of a liquid is constant when in an open vessel, that is, when subject to atmospheric
pressure. If we change the pressure the temperature of ebullition changes also. Thus, if we place a vessel of hot but not boiling water under the receiver of an air-pump, and rapidly exhaust the air, the liquid will after some time begin to boil, and we may notice that the lower its temperature the more perfect must we make the vacuum before ebullition commences. Or again, if water be subject to pressure greater than that of the atmosphere, its temperature must be raised higher than 212° before it will boil. Experiment, therefore, shows that the boiling point, constant at the same pressure, varies at different pressures, rising higher as the pressure increases, and vice versa.

Strictly speaking, the pressure of the atmosphere is not always the same; it varies within narrow limits from day to day; it decreases as we ascend higher into it, and hence there will be a small but corresponding variation in the boiling point at different times and places. This last fact has afforded the means of measuring the altitude of mountains, by determining the difference of the boiling point at their base and their summit. Measuring the atmospheric pressure by the column it supports in the barometer, we may draw up the following table of the relation of the boiling point to the height of the barometer column and the altitude of the observer, assuming that the barometer stands at 29.922 inches, and water boils at 212° Fahr. at the level of the sea.

<table>
<thead>
<tr>
<th>Height of Barometer in inches</th>
<th>Altitude in feet</th>
<th>Boiling Point of Water Fahr.</th>
<th>Height of Barometer in inches</th>
<th>Altitude in feet</th>
<th>Boiling Point of Water Fahr.</th>
</tr>
</thead>
<tbody>
<tr>
<td>29.922</td>
<td>0</td>
<td>212.0</td>
<td>25.988</td>
<td>3,926</td>
<td>204.9</td>
</tr>
<tr>
<td>29.906</td>
<td>462</td>
<td>211.1</td>
<td>25.468</td>
<td>4,460</td>
<td>204.0</td>
</tr>
<tr>
<td>28.774</td>
<td>933</td>
<td>210.0</td>
<td>26.014</td>
<td>5,000</td>
<td>203.0</td>
</tr>
<tr>
<td>28.659</td>
<td>1,411</td>
<td>209.3</td>
<td>24.046</td>
<td>6,111</td>
<td>201.2</td>
</tr>
<tr>
<td>27.846</td>
<td>1,897</td>
<td>208.5</td>
<td>23.454</td>
<td>7,268</td>
<td>200.0</td>
</tr>
<tr>
<td>27.348</td>
<td>2,392</td>
<td>207.6</td>
<td>18.992</td>
<td>18.700</td>
<td>190.0</td>
</tr>
<tr>
<td>26.852</td>
<td>2,895</td>
<td>206.7</td>
<td>15.135</td>
<td>18.000</td>
<td>180.0</td>
</tr>
<tr>
<td>26.372</td>
<td>3,407</td>
<td>205.8</td>
<td>12.145</td>
<td>26,000</td>
<td>170.0</td>
</tr>
</tbody>
</table>

But, besides pressure, certain other circumstances exercise a slight but sensible influence on the boiling point. In a glass
vessel the boiling point of water is about 2° higher than in a metal one, owing apparently to some adhesion between the glass and the liquid. Dr. Miller states that, if the glass be varnished with shellac, the temperature of the water may be raised to 221° in the open air, when a sudden burst of steam will take place, during which the temperature falls to 212°. From a similar cause the presence of salts in solutions raises the boiling point in some cases considerably. A saturated solution of common salt boils at 227° Fahr., and a saturated solution of chloride of calcium, which has an enormous affinity for water, does not boil at a less temperature than 355° Fahr.

There is yet one other remarkable condition of evaporation which should be noticed here. If water be dropped upon a clean metallic surface heated sufficiently high, instead of entering into ebullition it assumes a globular form, and rolls about very slowly and quietly evaporates. This condition, known as the spheroidal state, has been investigated by M. Boutigny. He finds that the temperature of the liquid globule never rises so high as its boiling point, being indeed usually 5° to 10° below it; that the temperature of the plate necessary to cause the spheroidal state varies with different liquids, and depends in part on the conducting power of the plate; and he considers the temperature of the spheroid to be constant, being for water 205°-7, for alcohol 167°-9, and for ether 93°-6.

If, whilst the spheroid is rolling upon the metal plate, the temperature of the plate is allowed to fall below a certain temperature (340° for water), the spheroid breaks, and is suddenly dispersed in vapour.

The temperature of the vapour rising from a liquid is necessarily identical with that of the liquid from which it rises, except in those cases in which the boiling point has been affected by adhesion, when the vapour at once adjusts itself to the normal temperature at that pressure.

So long as vapour is in contact with the liquid from which it has been formed, its temperature continues the same as that of the liquid, for if it be heated it takes up fresh liquid, and the temperature falls from the absorption of the heat rendered latent, until the normal temperature of the boiling point is regained.
The Vaporisation of Water and the Formation of Steam.

The temperature at which water boils is therefore constant at each pressure, and in consequence the temperature of the steam itself, when in contact with water, is constant at each pressure. The relation between the temperature and pressure of steam has been ascertained by experiment.

When in contact with the water producing it, steam is at the maximum density consistent with that temperature and pressure, and is then called saturated steam, or vaporous steam, and its temperature is called the maximum temperature of saturation at the given pressure. Usually when the pressure of steam is spoken of, the pressure of saturated steam is intended.

When isolated from the water producing it and heated, the steam expands, and decreases in density if the pressure be constant, or if the volume be constant it increases in pressure; it is then called variously anhydrous, gaseous, or superheated steam. The rate of expansion of superheated steam must be determined by experiment.

By the density of steam we mean the relative weight of a unit of volume. The specific volume of the steam is the reciprocal of the density, or the ratio of the volume of the steam to that of the volume of water which produced it. The density of saturated steam is constant at each temperature, and must be determined by experiment.

The latent heat of evaporation of steam is the quantity of heat which disappears in effecting the conversion of the water into vapour, or which reappears in the condensation of the steam. The latent heat of evaporation added to the sensible heat, or heat required to raise the temperature of the water up to the temperature of ebullition, is called the total heat of the steam.

The Relation between the Pressure and Temperature of Saturated Steam.

Probably the earliest experiments on this subject were made by Watt,* who tells us that when inventing the separate con-

* Muirhead's Life of Watt, p. 76.
densation he made some trials (in 1774) from which he constructed a curve, of which the ordinates represented the pressures, and the abscissæ the temperatures of the steam, and thus enabled him to calculate the one from the other at sight, with sufficient accuracy for his purposes. Watt first surmised that the elastic force or pressure of the steam increased in a geometric progression for temperatures increasing in an arithmetical progression.

Robison* made experiments upon the same subject at elevated temperatures, ascertaining the temperature at which the steam began to blow off from a safety valve loaded with weights, a proceeding susceptible of little accuracy. Dalton,† however, was more successful in devising an accurate method. He employed a barometer carefully purged of air, into which he introduced a small quantity of water. The barometer was surrounded by an outer water bath, by which the vapour in its chamber was heated to various temperatures. The mercury in the barometer tube adjusted itself so as to be in equilibrium at each temperature between the pressure of the atmosphere on the outside and the pressure of the vapour within, and the column fell as the temperature rose to an extent which is an exact measure of the pressure of the vapour within. The difference of height of an ordinary barometer and the barometer containing the water gives directly the pressure of the steam, so that by a series of careful measurements of a humid barometer and an ordinary dry barometer, the pressures corresponding to various temperatures may be observed.

This method, under various modifications, has been frequently employed, both for water and other liquids, at pressures which are less than that of the atmosphere. The chief difficulty is to maintain the liquid in the bath, by which the barometer is


PART I.
heated, at a uniform temperature, and to prevent it from dividing into strata unequally heated. To obviate this, the temperature may be observed at various depths and the arithmetical mean taken, or the length of the barometer may be decreased as the temperature rises. Or a barometer with two limbs may be employed, as in the researches of Dr. Ure; or, lastly, the varying temperature of the atmosphere may be substituted for that of the liquid bath, as in the experiments of Kaemtz,* intended to supply data for meteorological purposes, which extended over a period of two years, and ranged from $-15^\circ$ to $+80^\circ$ Fahr.

Dr. Ure's† modification enables the experiments to be carried to pressures higher than that of the atmosphere. The space in the barometer tube occupied by the vapour need never be large, and the increase of elastic force is measured by the quantity of mercury which must be added to a second limb of the barometer in order to maintain the quicksilver in the first at a constant level. Thus, in fig. 148, $a b c$ is the bent barometer tube for experiments above the atmospheric pressure, the shorter limb being enclosed in a glass vessel, which can be filled with oil and heated progressively to any required temperature. Fine rings of platinum wire are firmly fixed round the tubes at the level $d d$, and as the temperature rises the mercury in the limb in the bath is maintained at this level by adding mercury in the other limb, when the column $d e$, supported by the steam, measures its elastic force.

Dalton, whose experiments were, on the whole, accurate, inferred from the results which he obtained with water and alcohol, that the tension of all vapours was equal at temperatures equally distant from their boiling points under atmospheric pressure. This law, which has since borne his name, has not

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† Phil. Trans., 1818, p. 338.
been confirmed by experiments on a larger number of liquids. For many liquids, however, it is nearly true, at small distances above the boiling point. Thus:

<table>
<thead>
<tr>
<th>Degrees from the boiling point</th>
<th>Elasticity in inches of Mercury</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fahrenheit</td>
<td>Water</td>
</tr>
<tr>
<td>+ 30</td>
<td>62.90</td>
</tr>
<tr>
<td>+ 20</td>
<td>44.06</td>
</tr>
<tr>
<td>+ 10</td>
<td>36.47</td>
</tr>
<tr>
<td>0</td>
<td>30.00</td>
</tr>
<tr>
<td>− 10</td>
<td>24.50</td>
</tr>
</tbody>
</table>

In the above table the boiling point of water is 212°, of alcohol 173°, and of ether 104°.

The following table gives a few of Dalton’s results for comparison with those of other experimenters which will be given presently.

**Table II.—Elastic Force of the Vapour of Water, according to Dalton.**

<table>
<thead>
<tr>
<th>Temperature (Fahr.)</th>
<th>Elastic Force of Vapour In Inches Mercury</th>
<th>In lbs. per square inch</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.086</td>
<td>0.033</td>
</tr>
<tr>
<td>10</td>
<td>0.980</td>
<td>0.945</td>
</tr>
<tr>
<td>20</td>
<td>1.129</td>
<td>1.064</td>
</tr>
<tr>
<td>40</td>
<td>2.233</td>
<td>2.131</td>
</tr>
<tr>
<td>60</td>
<td>5.24</td>
<td>5.262</td>
</tr>
<tr>
<td>80</td>
<td>10.00</td>
<td>9.500</td>
</tr>
<tr>
<td>100</td>
<td>18.86</td>
<td>9.93</td>
</tr>
<tr>
<td>150</td>
<td>7.42</td>
<td>7.71</td>
</tr>
<tr>
<td>212</td>
<td>30.00</td>
<td>15.00</td>
</tr>
</tbody>
</table>

In 1823 the French Government, then legislating on the subject of steam, and requiring some further knowledge of its properties, intrusted to the French Academy the conduct of some important experiments on this subject. The Academy appointed a Commission, consisting of MM. Prony, Arago, Girard, and Dulong, to investigate the subject, and their report was published in the Memoirs of the Academy for 1831.* The experiments detailed in this Report were made chiefly by MM. Dulong and Arago, by a new method, and with all the care and accuracy which was possible in the state of science at the time. They were also on a scale which is only possible where

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private effort is seconded by the munificence of the Government.

Their apparatus consisted of, 1st, a boiler to generate the steam, 2nd, a manometer to measure the pressure.

The pressure, which extended to twenty-four atmospheres, was in fact measured by the column of mercury it would support in an open glass tube, but as the length of tube necessary for this purpose rendered it very inconvenient, they employed an intermediate measurer, consisting of a closed air manometer, graduated by experiment with the open mercury column. At the centre of the tower of the ancient church of St. Geneviève they erected a firmly supported wooden column, to which they attached the glass tubes containing the mercury column. These tubes, thirteen in number, were each 6½ feet in length, so that the mercury column for the graduation of the manometer could be as much as 86 feet in height, corresponding to a pressure of thirty atmospheres, or 450 lbs. per square inch. This column was adjusted precisely vertical, and communicated with a cistern containing 100 lbs. of mercury. The manometer, which consisted of a carefully dried glass tube, closed at the upper extremity, and 67 inches long, communicated with the same cistern, and was maintained at a uniform temperature by a stream of water circulating round it. The height of its mercury was read by means of a vernier, similar to that of a standard barometer. It is easy to see how, by means of a force pump, the pressure in the cistern of mercury could be increased at pleasure, and how the pressure could be registered by reading off simultaneously the height of the mercury in the open tube and its corresponding level in the manometer. When the value of the divisions of the manometer had been thus determined up to twenty-seven atmospheres, it became an instrument for measuring pressure of as great accuracy and delicacy as could be desired.

The boiler for generating the steam was of a capacity of 17·6 gallons, to ensure a uniform temperature, and communicated with the manometer by a tube filled with water, cooled by a refrigeratory apparatus. The temperature was measured by means of mercurial thermometers, placed in thin metal tubes, containing mercury, to protect them from pressure.
ON THE PROPERTIES OF STEAM.

The boiler being charged, and a convenient quantity of fuel introduced into the furnace, the temperature was allowed to rise until it nearly attained a maximum. A series of readings were then taken simultaneously from the manometer and four thermometers, until the temperature passed its maximum, and began sensibly to decrease. The readings at the maximum were alone retained for calculation. Fresh fuel was then added, and a second experiment obtained.

The method, carried out with the skill for which MM. Arago and Dulong have earned so high a reputation, possesses most of the essentials of complete accuracy. Its chief defect, as M. Regnault has pointed out, lies in this, that when the pressure and temperature are changing, however slowly, it is impossible to be absolutely certain that the thermometers have followed that change with the necessary rapidity, and that they do really register the temperature at the time the observation is made. There is in these experiments one other source of possible error, namely, the use of the mercurial thermometer, which, in the higher parts of its scale does not possess the accuracy necessary in experiments of this nature. Be this as it may, these experiments are of high value and permanent importance. The results obtained in thirty experiments are given in Table IV. on next page.

Next to the experiments of the French Academy, the most important experiments on the relation of temperature and pressure of steam were those of the Franklin Institute in America. They differed considerably from those of the French physicists, and are probably less reliable. The following table gives an abstract of the results:

<table>
<thead>
<tr>
<th>Pressure in Atmospheres</th>
<th>Temperature in degrees Fahr.</th>
<th>Pressure in Atmospheres</th>
<th>Temperature in degrees Fahr.</th>
<th>Pressure in Atmospheres</th>
<th>Temperature in degrees Fahr.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>212</td>
<td>4½</td>
<td>298·5</td>
<td>8</td>
<td>335</td>
</tr>
<tr>
<td>1½</td>
<td>235</td>
<td>5</td>
<td>304·5</td>
<td>9½</td>
<td>340½</td>
</tr>
<tr>
<td>2</td>
<td>250</td>
<td>6½</td>
<td>310</td>
<td>9½</td>
<td>345</td>
</tr>
<tr>
<td>2½</td>
<td>264</td>
<td>6</td>
<td>315·5</td>
<td>9½</td>
<td>349</td>
</tr>
<tr>
<td>3</td>
<td>275</td>
<td>6½</td>
<td>321</td>
<td>10</td>
<td>352½</td>
</tr>
<tr>
<td>3½</td>
<td>284</td>
<td>7½</td>
<td>326</td>
<td>10½</td>
<td>356½</td>
</tr>
<tr>
<td>4</td>
<td>291·6</td>
<td>8½</td>
<td>331</td>
<td>11½</td>
<td>360</td>
</tr>
<tr>
<td>No. of Experiment</td>
<td>Temperature observed Cent.</td>
<td>Mean Temperature reduced to Fahr. scale</td>
<td>Elastic force of Steam in Metres of Mercury, at 0° C.</td>
<td>Elastic force in Inches of Mercury.</td>
<td>Elastic force in Atmospheres of 29.92 inches</td>
</tr>
<tr>
<td>------------------</td>
<td>---------------------------</td>
<td>----------------------------------------</td>
<td>---------------------------------</td>
<td>-----------------</td>
<td>---------------------------------</td>
</tr>
<tr>
<td>Small Thermometer</td>
<td>Large Thermometer</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>127.97</td>
<td>123.3</td>
<td>258.99</td>
<td>1.62916</td>
<td>64.141</td>
</tr>
<tr>
<td>2</td>
<td>132.58</td>
<td>132.82</td>
<td>270.86</td>
<td>2.1767</td>
<td>85.698</td>
</tr>
<tr>
<td>3</td>
<td>132.64</td>
<td>133.3</td>
<td>271.84</td>
<td>2.1816</td>
<td>85.891</td>
</tr>
<tr>
<td>4</td>
<td>137.70</td>
<td>138.3</td>
<td>280.40</td>
<td>2.5386</td>
<td>99.947</td>
</tr>
<tr>
<td>5</td>
<td>149.54</td>
<td>149.7</td>
<td>301.31</td>
<td>3.4759</td>
<td>133.85</td>
</tr>
<tr>
<td>6</td>
<td>151.87</td>
<td>151.9</td>
<td>305.38</td>
<td>3.6688</td>
<td>145.15</td>
</tr>
<tr>
<td>7</td>
<td>153.64</td>
<td>153.7</td>
<td>308.60</td>
<td>3.881</td>
<td>152.80</td>
</tr>
<tr>
<td>8</td>
<td>163.00</td>
<td>163.4</td>
<td>316.76</td>
<td>4.9353</td>
<td>194.42</td>
</tr>
<tr>
<td>9</td>
<td>168.40</td>
<td>168.5</td>
<td>335.21</td>
<td>5.6054</td>
<td>220.09</td>
</tr>
<tr>
<td>10</td>
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<td>386.61</td>
<td>8.8995</td>
<td>342.81</td>
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<td>188.5</td>
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<td>220.8</td>
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<td>224.15</td>
<td>435.22</td>
<td>18.1894</td>
<td>716.13</td>
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</table>

The experiments of Arago and Dulong give a temperature of 358°-88 Fahr. for a pressure of ten atmospheres, or 6°-38 higher than that of the American Institute. This notable difference, too great to be merely accidental, Regnault, whose experience in the matter entitles him to speak with certainty, attributes to the use of mercurial thermometers, which, although agreeing perfectly between 32° and 212°, often present at elevated temperatures a difference of many degrees. Regnault's own experiments give 356.54 on the air-thermometer as the temperature at the pressure of ten atmospheres, which is 2°-34 lower than the French Academy, and 4° higher than the Franklin Institute. As at this temperature the mercurial thermometer gives higher
indications than the air thermometer, MM. Arago and Dulong’s experiments appear the most reliable.

The uncertainty arising from the discordance of the numerical results of the different physicists who had studied this question, and especially the difference above noted, called for a new investigation.

The experiments of M. Regnault on the reliability of the various instruments employed in measuring temperature, led him to the conclusion that at elevated temperatures the indications of different mercurial thermometers were too variable to be trusted, unless they were made of the same description of glass, and that even in that case they require reduction to the absolute temperature of the air thermometer. The following table gives some of the results obtained:

<table>
<thead>
<tr>
<th>Temperature by the Air Thermometer</th>
<th>Temperatures by Mercurial Thermometers</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>Crystal of Chotai-le-Bol</td>
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<tr>
<td>100°</td>
<td>100°</td>
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<td>150</td>
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<td>300</td>
<td>305-72</td>
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<td>350</td>
<td>360-50</td>
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</tbody>
</table>

The above numbers are in Centigrade degrees. They show for the thermometer of ordinary glass, when its indications are reduced to Fahrenheit’s scale, the following divergences from the true temperature shown by the air thermometer:

<table>
<thead>
<tr>
<th>Temperature by Air Thermometer</th>
<th>Temperature by Mercurial Thermometer</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fahrenheit:</td>
<td>Fahrenheit:</td>
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<tr>
<td>302</td>
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<tr>
<td>392</td>
<td>391-46</td>
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<tr>
<td>482</td>
<td>482-09</td>
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<tr>
<td>572</td>
<td>573-94</td>
</tr>
<tr>
<td>662</td>
<td>669-20</td>
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</tbody>
</table>

To M. Regnault the French Government committed, on the proposition of M. Legrand, the task of carrying on a series of experiments to determine, with the greatest precision, the
principal laws and numerical data which enter into the calculation of the duty of steam engines, and supplied the funds for fulfilling its attentions on a scale such as would have been impossible in any private enterprise. The papers, which were the result of this munificence, are amongst the most important in the recent history of science. They cover a large ground, and possess a precision and completeness before scarcely ever attained in researches of this kind.

In relation to the steam engine, the most important questions which M. Regnault has set himself to solve, are—1st. The elastic force of the vapour of water, both at pressures lower than that of the atmosphere, and at high pressures, up to 400 lbs. per square inch. 2nd. The latent heat of the vapour of water through a similar range of temperature and pressure. 3rd. The specific heat of liquid water. The laws of the density and expansion of steam, it will be observed, Regnault did not touch, but, on the subjects above named, his researches are not likely to be superseded in accuracy or extent.

To ascertain the relation of temperature and volume of steam at low temperatures, Regnault adopted the plan of employing two barometers, placed side by side, under precisely similar circumstances, into one of which was introduced a portion of water perfectly freed from air. The upper part of these barometers was surrounded by a large bath of water, maintained by agitation at a constant temperature. The difference of level of the mercury in the humid and dry barometers gave directly the elasticity of the steam at the temperature of the bath.

Fig. 149 shows one of the forms of apparatus employed. The two barometers, $eg$, $ok$, were plunged in the same cistern $v$, and maintained vertical against a firm board. In the form shown, the moist barometer $eg$ communicated with a glass globe $\lambda$, of a capacity of 80 cubic inches, and exhausted of air by means of an air-pump, after which the tube $l$ was hermetically sealed. The tension of the air remaining was accurately ascertained, and did not exceed 1 to 2 millimetres. The bath of galvanised iron $vv$ was of a capacity of about 2,746 cubic inches; over a rectangular opening opposite the barometers the plate of glass $zg$ was fixed, and through this the readings were taken, after the error arising from refraction had been determined. By means of a lamp placed underneath, a constant temperature
could be maintained in this bath as long as was necessary to take a series of readings. When these were complete, water was withdrawn from the bath and replaced by boiling water; then, when a constant temperature was again arrived at, a new series of readings could be obtained.

These methods answered with perfect accuracy up to about

150° Fahr.; above this the tendency of the water to separate into strata of unequal temperature began to manifest itself so as to introduce errors into the experiments. Regnault, therefore, had recourse to the plan of observing the temperature at which water boils at determined pressures. This was the proceeding adopted by Arago and Dulong, but with a new precaution.
Those physicists were, by the method they adopted, compelled to regulate their experiments by the condition of their fire, so that it was impossible to maintain a constant temperature for any great length of time. By adding to their apparatus a large vessel containing air and acting as an artificial atmosphere, together with some large air-pumps, by which the pressure on the water could be predetermined and maintained perfectly constant, Regnault, in fact, obtained means for regulating his experiments altogether independently of the furnace, for the temperature of ebullition, we have already seen, is perfectly constant under a constant pressure. The conditions were identically those of water boiling in air.

Fig. 150 shows the larger of the two forms of apparatus employed in the experiments on the elasticity of steam at high temperatures.

It consists of a boiler, condensing tube, artificial atmosphere, mercurial manometer, and an air-pump. The boiler B is of red copper, of 13.7 inches diameter, and 123 pints capacity. The cover carries two tubes, in which were placed mercurial thermometers protected from pressure, and a third for an air thermometer. The boiler was strengthened by iron rings bolted round it. The refrigerator A A of a copper tube 5 feet long, communicating with the boiler, surrounded by a larger tube, was arranged so that a continuous stream of cold water
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flowed into the funnel $f$, and away by the siphon $s$. The reservoir of air forming the artificial atmosphere for maintaining a constant pressure was formed of a cylinder $c$, of 62 gallons capacity, and riveted and brazed so as to be perfectly air-tight. The manometer for ascertaining the pressure consisted of an open mercurial column in every instance, than which no more perfect instrument, or one more free from corrections depending on theoretical calculations, could be devised. The indications are of equal sensitiveness at all pressures, instead of continually decreasing in value, as in the ordinary compressed air-gauge employed by Arago and Dulong.

This manometer is not shown in the sketch, but it consisted of a cistern of mercury with a pipe attached having four openings; one of these was usually closed; the other three were for the attachment of glass tubes to contain the mercury columns in the various experiments in which this apparatus was employed. The column open to the atmosphere consisted of ten to twenty-two glass tubes, nearly 10 feet long and $\frac{1}{10}$ inch bore. These were carefully connected together to form a column perfectly vertical, and from 40 to 80 or more feet in height, as required, being supported against a vertical wall. Up to fifteen atmospheres the levels were taken by two cathetometers; for higher pressures the glass tube itself was graduated into millimetres.

The air-pump for maintaining the artificial atmosphere in the large cylinder $c$, consisted of three single-acting cylinders, each discharging 42 cubic inches per stroke.

To measure the temperature two mercurial thermometers $t t$, perfectly accordant, and an air thermometer, were employed; the latter consisting of a thin glass cylinder of about 1\,17 inch diameter, and 11\,7 inches long. This communicated by the capillary tube $e e$ with the manometer $g h$. The capacity of the air thermometer, its temperature, and the pressure, were therefore known, and with the corrections which M. Regnault applied, he considers that it indicated sensibly $\frac{1}{10}$th of a degree.

It will be evident how, with this apparatus, a continuous and energetic ebullition was maintained in the boiler $b$, under any pressure at which the observer wished to determine the temperature of the steam. Condensation went on at the same time
with a corresponding rapidity in the cooling apparatus \( R R \); the pressure being maintained constant by the air-pump, the thermometers would in time become identical in temperature with the steam in the boiler \( R \); simultaneous observations at this period of the thermometers and the manometer gave the relation of temperature and pressure which was required.

We have now described all the principal methods by which it has been sought to determine, experimentally, the relation of the pressure and temperature of saturated steam. It is necessary that we should next consider how they may be expressed in a formula suitable for calculation.

The law to which Watt was led, and which is usually known as Dalton's, from the care with which he verified it, so far as his experiments went, is that which, in general terms, most nearly expresses this relation; it is, that the elastic force of vapours increases in a geometrical progression, for a series of temperatures increasing in an arithmetical progression, and many of the formulæ which have been constructed to express the results of experiments have been based upon it. Strictly speaking, it is, however, only an approximate expression of the true law.

One of the earliest and best of the formulæ which have been proposed, is that first applied to steam by M. Prony, of the form

\[ f = a t^4 + b t^3 + c t^2 + \ldots \quad (1) \]

where \( f \) is the elastic force and \( t \) the temperature. The other quantities are constants derived from experiment. This formula is accurate, but requires a large amount of calculation.

Dr. Young proposes the formula

\[ f = (a + b t)^m \quad (2) \]

which has been the basis of several formulæ employed for interpolation by physicists. Thus MM. Arago and Dulong give from their own experiments the following constants:

\[ e = (1 + 0.7153 \tau)^9 \quad (3) \]

where \( e \) expresses the elasticity in atmospheres of 29.922 inches of mercury; \( \tau \) the temperature in Centigrade degrees reckoned from 100°, positive above that point and negative below, taking for unity an interval of 100°. For pressures greater than one atmosphere this formula is satisfactory, but it deviates greatly
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from experiment at lower pressures. At the same time it has a great simplicity.

The formula proposed by the Franklin Institute was of the same kind, the constants being

$$ e = (0.00333 \tau + 1)^6 \ldots (4) $$

where $e$ is the pressure in atmospheres of 30 inches of mercury, and $\tau$ the excess of the temperature above $212^\circ$ in Fahrenheit. This formula also does not apply below atmospheric pressure with accuracy. For calculation we may write it

$$ \log e = 6 \log \{0.00333 (t - 212^\circ) + 1\} \ldots (5) $$

and for calculating the temperature from the pressure,

$$ = \sqrt[6]{\frac{e - 1}{0.00333}} + t 212 \ldots (6) $$

Another form of expression was given by M. Biot in 1844, viz.

$$ \log r = a + b e^t + c e^t \ldots (7) $$

The constants for this formula M. Regnault has calculated from the following values, obtained from the graphic curve, which represented his experiments:

- $t_0 = 0^\circ$, $r_0 = 4.60$ mm.
- $t_1 = 25$, $r_1 = 23.55$
- $t_2 = 50$, $r_2 = 91.98$
- $t_3 = 75$, $r_3 = 288.50$
- $t_4 = 100$, $r_4 = 760.00$

whence he deduced

$$ \log a = 0.006865036 $$
$$ \log b = 1.9967249 $$
$$ \log c = 0.6116485 $$
$$ a = +4.7384380 $$

where the third term $c e^t$ is negative. Between $0^\circ$ and $100^\circ$ Centigrade, this expresses M. Regnault's results with very great exactness. Above this temperature, it gives results which become sensibly different from those of experiment.

For temperatures between $100^\circ$ and $230^\circ$ Centigrade, M. Regnault obtained the following values for the constants in M. Biot's formula:
For the Air Thermometer
\[
\log a = 1.997412127
\]
\[
\log k = 0.007590697
\]
\[
\log b = 0.4121470
\]
\[
\log c = 3.744891
\]
\[
a = 5.4585895
\]

For the Mercurial Thermometer
\[
\log a = 1.997443007
\]
\[
\log k = 0.01182377
\]
\[
\log b = 0.4163766
\]
\[
\log c = 4.9731198
\]
\[
a = 5.4882878
\]

Where in the formula the second term is negative, and
\[
\log \tau = a - 2 \quad a^2 + \quad c^2 \quad ... \quad (8)
\]
\[
a = \tau - 100^\circ
\]

which gives the relation of temperature in Centigrade degrees and pressure in millimetres. The mercurial thermometer was constructed of crystal of Choisi-le-Roi.

Mr. Rankine, in 1849, urged some theoretical objections to the formulæ employed by M. Regnault, and proposed the following:—
\[
\log p = 8.2591 - 3.43642 - 5.59873 - \frac{b}{c} - \frac{1}{2} \frac{b^2}{c^2} \quad ... \quad (9)
\]
\[
\tau = 1 + \sqrt{\left(\frac{8.2591 - 3.43642 + b^2}{c^2}\right)} - \frac{b}{2c} \quad ... \quad (10)
\]

when \(\tau = \tau + 461^\circ\cdot2\) Fahr.

The constants for this formula are—
\[
\begin{align*}
A &= 8.2591 \\
\log b &= 3.43642 \\
\log c &= 5.59873 \\
\frac{b}{2c} &= 0.003441 \\
\frac{b^2}{4c^2} &= 0.00001184
\end{align*}
\]

\[
\text{giving } p \text{ in lbs. per square foot.}
\]

\[
\begin{align*}
A &= 6.4095 \text{ giving } p \text{ in inches of mercury.} \\
A &= 6.1007 \text{ giving } p \text{ in lbs. per square inch.}
\end{align*}
\]

For accuracy this formula leaves little to be desired, but it requires considerable calculation, especially for finding the temperature from the pressure. Where so great accuracy is not required, the following simple formula gives results that may be relied upon for practical purposes over a large range of the scale:—
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\[ \log p = \frac{5(t - 212)}{t + 367} \ldots \text{(11)} \]
\[ t = \frac{2895}{5 - \log p} - 367 \ldots \text{(12)} \]

which gives the pressure \( p \) in atmospheres of 29.922 inches of mercury or 14.7 lbs. per square inch.

**Example 1.** For instance, let \( t \) be given = 230° Fahr.,

then \( \log p = \frac{5 \times 18}{597} = 0.15075 = \log 1.415 \).

At 230° Fah. therefore the pressure is 1.415 atmosphere = 1.415 \times 29.922 = 42.339 inches of mercury = 1.415 \times 14.7 = 20.8 lbs. per square inch, or 20.8 - 14.7 = 6.1 lbs. above the atmospheric pressure.

**Example 2.** Again, let \( p = 691 \) atmosphere

\[ \frac{2895}{5 - 1.8395} - 367 = \]
\[ \frac{2895}{5.1605} - 367 = 193.99 \text{ Fahr.} \]

**Example 3.** We may also calculate the case given in Example (1) by Mr. Rankine's formula; here \( t = t + 461.2 = 230° + 461.2 = 691.2 \).

\[ \log b = 3.43642 \]
\[ - \log t = 2.83960 = 0.59682 = \log 3.9521 \]
\[ \log c = 5.59873 \]
\[ - 2 \log t = 5.67921 = 1.91952 = \log 0.8308 \]
\[ 4.7829 \]

For lbs. per square inch 6.1007 - 4.7829 = 1.3178 = \log 20.79 lbs.

For inches of mercury 6.4095 - 4.7829 = 1.6266 = \log 42.33 inches.

These results are almost identical with those given by the preceding formula.

The following table may serve as a guide in the use of these formulæ, showing how far they are accurate, and within what limits on the scale they may be used with safety:
### Table V.—Of the Pressure and Corresponding Temperature of Saturated Steam, obtained from the Tables of M. Regnault by Interpolation and Reduction to English Measures.

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<tr>
<th></th>
<th></th>
<th></th>
<th></th>
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<td>52</td>
<td>283.32</td>
<td>200</td>
<td>381.8</td>
</tr>
<tr>
<td>22</td>
<td>233.08</td>
<td>2.45</td>
<td>53</td>
<td>284.53</td>
<td>210</td>
<td>386.0</td>
</tr>
<tr>
<td>23</td>
<td>235.43</td>
<td>2.32</td>
<td>54</td>
<td>285.73</td>
<td>220</td>
<td>389.9</td>
</tr>
<tr>
<td>24</td>
<td>237.75</td>
<td>2.25</td>
<td>55</td>
<td>286.90</td>
<td>230</td>
<td>393.8</td>
</tr>
<tr>
<td>25</td>
<td>240.00</td>
<td>2.16</td>
<td>56</td>
<td>288.05</td>
<td>240</td>
<td>397.5</td>
</tr>
<tr>
<td>26</td>
<td>242.16</td>
<td>2.10</td>
<td>57</td>
<td>289.19</td>
<td>250</td>
<td>401.0</td>
</tr>
<tr>
<td>27</td>
<td>244.26</td>
<td>2.04</td>
<td>58</td>
<td>290.31</td>
<td>260</td>
<td>404.5</td>
</tr>
<tr>
<td>28</td>
<td>246.32</td>
<td>1.98</td>
<td>59</td>
<td>291.42</td>
<td>270</td>
<td>407.9</td>
</tr>
<tr>
<td>29</td>
<td>248.30</td>
<td>1.93</td>
<td>60</td>
<td>292.51</td>
<td>280</td>
<td>411.2</td>
</tr>
<tr>
<td>30</td>
<td>250.23</td>
<td>1.86</td>
<td>65</td>
<td>297.77</td>
<td>290</td>
<td>414.4</td>
</tr>
<tr>
<td>31</td>
<td>252.09</td>
<td>1.86</td>
<td>70</td>
<td>302.71</td>
<td>300</td>
<td>417.5</td>
</tr>
</tbody>
</table>
On the Relation of Temperature and Density of Saturated Steam.

Notwithstanding the very numerous experimental researches on the relation of pressure and temperature of steam, the relation of temperature and density, which is equally important in the calculations of the steam-engine, has, till recently, been examined by theoretical investigations alone. By the method of Dumas, it was found that, in becoming vapour, a cubic unit of water expanded to 1,669 cubic units of steam, and from this single datum the density and volume at all other temperatures has been calculated, on the assumption that steam follows the same laws of expansion and contraction, under the influence of temperature and pressure, as a perfect gas.

The gaseous laws, or the laws of the relation of volume, pressure, and temperature of a perfect gas may be enumerated as follows:—

1. Mariotte’s or Boyle’s law; the pressure or elasticity is inversely as the volume when the temperature remains the same. That is, if a volume of gas of 10 cubic feet, under a pressure of 15 lbs. per square inch, be subjected to a pressure of 30 lbs. per square inch, the volume will be diminished to 5 cubic feet; or, on the other hand, if the pressure be decreased to 7½ lbs. per square inch, the volume will increase to 20 cubic feet. Expressed in a formula, putting \( p \) for the pressure when the volume is \( v \), \( p_1 \) the pressure when the volume is \( v_1 \)—

\[
\frac{p}{p_1} = \frac{v_1}{v} \ldots (13).
\]

2. Gay-Lussac’s or Dalton’s law; the expansion of a given weight of an elastic fluid under a constant pressure is \( \frac{459 + t}{459} \)th part of its volume at 0° Fahr. for every degree of increase of temperature. Expressed in a formula this law is—

\[
\frac{v}{v_1} = \frac{459 + t}{459 + t} \ldots (14).
\]
Hence, also, if the volume be constant,
\[
\frac{P}{P_1} = \frac{459 + t}{459 + t_1} \ldots (15).
\]
and combining the two formulae
\[
\frac{v \times P}{v_1 \times P_1} = \frac{459 + t}{459 + t_1} \ldots (16).
\]
that is, the product of the volume and pressure at one temperature, is to that product at another temperature as the temperature in the first case to the temperature in the second, the temperatures being counted from the absolute zero, or a temperature of $-459^\circ$ Fahr.

Now we have seen, that it has been determined experimentally for steam that when $t_1 = 212^\circ$ Fahr., $P_1 = 14.7$ and $v_1 = 1669$, and if we assume that steam is strictly gaseous, these data suffice for calculating the volume or density of the same weight of steam at any other temperature and pressure; substituting in (16) we get
\[
v = 1669 \times 14.7 \times \frac{459 + t}{71 \times P} = 36.5 \frac{459 + t}{P} \ldots (17).
\]
Thus, if we take from the preceding table of the relation of temperature and pressure the corresponding numbers, and substitute them for $t$ and $P$ in the above formula, we shall get the theoretical volume at that temperature and pressure. Thus from Table V, we have $t = 281^\circ$ when $P = 50$ lbs., then
\[
v = 36.5 \frac{459 + 281}{50} = 540
\]
that is, a volume of 1,669 cubic feet at $212^\circ$, would be reduced to 540 at $281^\circ$, and of course the density increased in the inverse ratio.

From this well-known formula all the tables of the density of steam, with one recent exception, have been deduced, on which calculations of the duty of the steam-engine have been founded.

Although experimentalists have for some time questioned the
truth of this theoretical formula, yet, up to a recent time, no reliable direct experiments had been made to test its truth. Yet a few years since Dr. Joule and Professor Thomson announced, as the result of the application of the dynamical theory of heat, that for temperatures above 212° Fahr. there would prove to be a considerable deviation from the gaseous laws in the case of steam. In 1855, Professor Rankine gave a theoretical formula for the density of steam, confirmatory of Professor Thomson’s views.* This formula deduces the volume from the latent heat, and is of the form

$$v - v' = \frac{H}{L} \ldots (17)$$

where $L$ is the latent heat of evaporation per cubic foot, in foot pounds of energy, and $H$ the latent heat of evaporation of one pound of steam in units of energy, and $v - v'$ is the increase of volume of one pound of the fluid in evaporating. As we have as yet not considered the subject of latent heat, we may express Professor Rankine’s formula in another form, as giving the volume from the pressure and temperature. It is then

$$v = \frac{773 \{1091.7 - 7(t - 32)\} \times (t + 461.2)^2 + 1}{23028 \frac{v'}{P} \{b(t + 461.2) + 2c\}}$$

where $v'$ is the specific volume of the steam, $v'$ the volume of one pound of water at the temperature $t$; $P$ the pressure of the steam at $t$ temperature in pounds on the square foot; log $b = 3.43642$; log $c = 5.59873$.

About the same time Mr. Tate made some experiments with ether, which led him to the conclusion that, at pressures somewhat above the atmospheric, the vapour of this substance does not follow the gaseous laws. These experiments led to a comprehensive series of researches, undertaken by Mr. Tate in conjunction with myself, to ascertain the density of saturated steam at all pressures, by a new and original method.

The general features of our method of ascertaining the density of steam, consist in vaporising a known weight of water in a

* Proc. Roy. Soc. Edinb. 1855. These views have been further developed by Mr. Rankine in his Manual of the Steam Engine and other Prime-Movers, in which are given full tables of the density of steam, agreeing well with the experimental results about to be detailed.
large glass globe—with a stem—of known capacity and devoid of air, and observing the exact temperature at which the whole of the water is just vaporised. Then, knowing the weight, volume, and temperature of the steam, its specific gravity may be calculated. In order to pursue this method with safety and with the requisite amount of accuracy, the following peculiarities of construction of the apparatus were adopted:

First, in order to secure the thin globe from bursting, and at the same time to have it uniformly heated, it is placed in a strong closed copper steam bath, having a thermometer and pressure gauge attached, and a strong glass tube, closed at its exterior extremity, for receiving the stem of the globe. By this arrangement the glass globe is secured from bursting, for whatever may be the elasticity of the steam, the internal pressure in the globe is balanced by the external pressure in the steam bath.

Second, when a given weight of water is vaporised in a closed vessel devoid of air, the steam is said to be in a state of saturation so long as any portion of the liquid remains in the vessel. But after all the water is vaporised, heat being still applied, the steam becomes superheated, or heated beyond the temperature just requisite for vaporising all the water. By way of distinction we call this point the maximum temperature of saturation. Now as we have to find by observation the temperature of the steam exactly at the point when the whole of the water is vaporised, the determination of this with sufficient accuracy and delicacy has hitherto formed the great practical difficulty attending experimental researches on the density of vapours. We have overcome this difficulty by using what may be called a saturation gauge, the form of which varies according to circumstances, but the principle on which it is constructed may be illustrated as follows:

Imagine two globes A, B, fig. 151, connected by a bent tube containing mercury, and immersed in a large bath of liquid to secure uniformity of temperature; suppose these globes devoid of air but containing weighed portions of water, say twenty grains in A and thirty in B. If heat be now applied to the liquid bath so as to increase progressively the temperature of the globes, this weighed portion of water will gradually pass into steam, and the elastic force in each globe will increase in a ratio
ON THE PROPERTIES OF STEAM.

Fig. 161.

corresponding with the temperature, but without in the least affecting the uniformity of level of the mercury columns \( c \) and \( d \), because the pressure on each side will be the same. But when the whole of the water in globe \( A \) has been evaporated, this equality of pressure will no longer exist, and the column \( c \) will rise. The pressure in \( b \) increases in the ratio for saturated steam, whilst that in \( A \) increases in the much smaller ratio of superheated steam, and hence the difference of level of the columns. The instant at which the columns begin to rise on one side and fall on the other, is the point at which the whole of the water in \( A \) is converted into steam; and the temperature then noted is the maximum temperature of saturation. The following theoretical table gives approximately the rise of the mercury column at several temperatures:

<table>
<thead>
<tr>
<th>Saturated Steam</th>
<th>Increments of Pressure for 1° Fahr.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pressure</td>
<td>Temperature</td>
</tr>
<tr>
<td>At 4 lbs. and 152°</td>
<td>175</td>
</tr>
<tr>
<td>7</td>
<td>175</td>
</tr>
<tr>
<td>15</td>
<td>213</td>
</tr>
<tr>
<td>20</td>
<td>228</td>
</tr>
<tr>
<td>61</td>
<td>295</td>
</tr>
<tr>
<td>74</td>
<td>308</td>
</tr>
</tbody>
</table>

The increments of pressure in this table are measured in inches of mercury. Their difference shows the rise of the mercury column on the one side on which expansion from superheating is taking place. That is, the columns would diverge from the level 0.210 inch at 152° F., 0.56 inch at 213°, 2.02 inches at 308°, and so on.

For reasons which will hereafter be obvious, it was found impossible to determine the instant at which the whole of the water in the globe was vaporised and the columns diverged. The cohesion of the glass to the last particles of water, the foggy condition of the steam, and other causes, rendered it necessary to superheat the steam a few degrees, and then having very
carefully determined the difference of level of the columns, to estimate from these data the maximum temperature of saturation.

In fig. 152 is shown a sectional elevation of the apparatus employed in these researches for pressures varying from 15 lbs. to 70 lbs. on the square inch, or from one to five atmospheres. A is the glass globe of measured capacity for the reception of the weighed portion of water, drawn out into a stem about 32 inches long. The average size of the globes was 5½ inches diameter or 75 cubic inches capacity; the stems were ⅜ to ⅞ inch bore. B B is the copper boiler or steam bath in which the globe was heated uniformly throughout. The copper bath is prolonged by a strong glass tube o o, 1½ inch in diameter, and closed at the bottom; the tube is fixed to the boiler by a stuffing box, its upper part being trumpet-mouthed to prevent its being forced out by the pressure. The joint in the stuffing box was made by a ring of vulcanised india-rubber, which at the temperatures required in this series of experiments, answered its purpose perfectly. To heat this outer glass tube, which was peculiarly liable to explode, and, in fact, on two occasions did so, an outer oil bath a a was used, made of blown glass, twenty inches long, and resting in a sand bath, l l. This bath was supported on a tripod. The copper bath was heated by a coil of gas jets e e; and the oil bath by a large wire gauge lamp h. protected from draughts by a muffle k k. The temperature thus obtained and distributed uniformly throughout the glass tube and steam bath by convection, was measured by a thermometer in the
oil bath, and another \( t \), exposed naked on the steam bath, and fixed in a stuffing box. Opposite the thermometer is a stopcock \( p \), and on the top of the boiler a pressure gauge, for roughly indicating the pressure in the boiler. The copper boiler replaced the globe \( b \) in the diagram, fig. 151. The two mercury columns, the outer in the tube \( o o \), and the inner in the stem of the globe \( i \), separate the vapour and water in the steam bath from that in the globe, and form the saturation gauge to which reference has been made. So long as the steam in the globe \( a \) remains in a state of saturation, the inner column remains stationary at a point a little above the level of the outer column, so as to balance the column of water in the steam bath \( b \). But when in raising the temperature the whole of the water in \( a \) is evaporated, and the steam begins to superheat, then the pressure of the steam in \( a \) no longer balances that of the steam in \( b \), and the columns diverge: the difference of level forming a measure of the expansion of the steam. It was found in practice a matter of the utmost importance that the observer should not, in these experiments, trust to the unaided eye to determine the point at which the columns began to diverge, but that a careful series of measurements of the difference of level of the columns should be made, not only near the saturation point, but also at various temperatures of superheating; thus affording data for determining the law of expansion near the saturation point, and for estimating the maximum temperature of saturation from a point at which the error from the cohesion between the water and the glass, and the error from the retention of portions of water in the steam itself, might both be eliminated. It was also found advisable to take these readings of the levels of the columns, rather in a descending than in an ascending series of temperatures.

To read the column levels with rapidity and facility, seeing that they could not be approached within six or \( \text{Fig. 153.} \) eight inches, a simple form of cathetometer was devised, sufficiently accurate for the purpose. It consisted of a telescope with cross wires sliding on a vertical graduated iron stem, and carrying a vernier for reading off the levels to the one-hundredth of an inch.
The steps in the process for determining the specific gravity of steam by this apparatus were as follows:

A glass globule of a size to contain, as nearly as might be, the required quantity of water for vaporisation, was selected from a series (fig. 153). These globules had open stems, and after being filled with water were immersed hot in a cup of mercury, so that, in cooling, the mercury should rise into and fill the capillary stem. The weight of the water introduced was easily ascertained by deducting from the weight after filling the weight of the dry cup, globule, and mercury. In this state the cup of mercury was transferred, and the globule passed into the large globe, in which a Torricellian vacuum had been previously formed.

To form the Torricellian vacuum, the globe, dried and filled with warm mercury, was heated on a sand bath until the mercury boiled; the stem was then filled with dry mercury, and the globe inverted, with its stem inserted in a basin of mercury. The globule was then introduced into the stem, and allowed to ascend into the globe. In order to transfer the globe from the basin to its place in the steam bath, a cup k, fig. 154, filled with mercury was suspended from the stem by an india-rubber strap, a platinum wire being inserted between the cup and globe stem to ensure free passage for the mercury. The cover of the boiler b b being then taken off, and the outer tube o o dried and partially filled with dry mercury, the globe was raised and inserted into its place, resting on a tripod in the boiler. The cover was then fixed with a flax and red lead joint, and the cock p connected with an air pump. Exhaustion was effected, so that the columns in the globe stem and outer tube stood
nearly level; the air pump was then removed and a portion of water allowed to enter through the cock. The gas lights were then kindled; and until the water attained the boiling point, the columns were maintained level by means of the air pump, to prevent the possible entrance of water into the globe. After boiling for a time the cock *p* was closed, and the process of vaporisation went on simultaneously in the bath and globe, the temperature being kept sufficiently high in the oil baths *a a* to maintain the water in the outer tube in a state of ebullition. The temperature of the baths is slowly and uniformly raised, until the temperature of the vapour in the globe is considerably above the maximum temperature of saturation. After having been maintained for a considerable period at this temperature, the levels of the columns were observed; then the temperature being allowed to sink some degrees, the operation was repeated, and the temperature again reduced; and so on until the columns became stationary, indicating saturated steam in the globe as well as on the boiler. A series of readings was taken at each temperature, to make sure that the globe had attained a uniformity of temperature. At the same time the levels of some file marks on the stem were taken, by which the capacity of the globe in each position of the mercury column could be determined. All the elements were thus obtained for calculating the density of the steam.

Let *w* be put for the weight of distilled water at $39°\cdot1$ Fahr., filling the globe to the point at which the mercury columns stood at the maximum temperature of saturation. Let *w* be the weight of water vaporised; *v* the specific volume of the steam, or the number of times the volume of steam exceeds the volume of the water from which it is raised; then:

$$v = \frac{w}{w} \ldots (19).$$

By at once superheating the steam in the globe, and then slowly reducing the temperature until the maximum temperature of saturation is reached, we secure the following advantages:—The cohesion of the water to the surface of the glass being overcome, that force, it may be presumed, cannot be regained until the glass again becomes wet, which can only occur on condensation, that is, by the reduction of the temperature below that
which corresponds to the maximum temperature of saturation. Moreover, the observation of the columns at different temperatures of superheating, not only supplies us with data for ascertaining the maximum temperature of saturation, but also for determining the law of expansion of superheated steam near the saturation point.

The following table gives the temperature of saturation deduced from the experiments with the above apparatus from the two highest temperatures of superheating attained in each case. Where the lower of these temperatures is manifestly within the limits of imperfect expansion, the reduction from higher temperature only has been retained.

**Table VI.—Results of Experiments on the Density of Steam at Pressures of from 15 to 70 lbs. per square inch.**

<table>
<thead>
<tr>
<th>No. of Experiment</th>
<th>Maximum Temperature of Saturation, Fahr.</th>
<th>Pressure of Steam in Inches of Mercury</th>
<th>Specific Volume of the Steam</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>242·89 242·90</td>
<td>53·60 53·63</td>
<td>943·1</td>
</tr>
<tr>
<td>2</td>
<td>244·90 244·82</td>
<td>55·60 55·44</td>
<td>908·0</td>
</tr>
<tr>
<td>3</td>
<td>245·42 246·22</td>
<td>56·06 56·89</td>
<td>899·5</td>
</tr>
<tr>
<td>4</td>
<td>255·62 255·50</td>
<td>66·70 66·84</td>
<td>759·4</td>
</tr>
<tr>
<td>5</td>
<td>262·30 263·14</td>
<td>76·26 76·20</td>
<td>649·2</td>
</tr>
<tr>
<td>6</td>
<td>267·35 267·21</td>
<td>81·71 81·53</td>
<td>635·3</td>
</tr>
<tr>
<td>7</td>
<td>267·08 269·20</td>
<td>81·36 84·20</td>
<td>605·7</td>
</tr>
<tr>
<td>8</td>
<td>269·24 269·20</td>
<td>84·36 84·20</td>
<td>605·7</td>
</tr>
<tr>
<td>9</td>
<td>274·76 274·76</td>
<td>92·29 92·29</td>
<td>584·4</td>
</tr>
<tr>
<td>10</td>
<td>273·30</td>
<td>90·08</td>
<td>543·2</td>
</tr>
<tr>
<td>11</td>
<td>279·42</td>
<td>99·68</td>
<td>515·0</td>
</tr>
<tr>
<td>12</td>
<td>282·50 282·58</td>
<td>104·48 104·54</td>
<td>497·2</td>
</tr>
<tr>
<td>13</td>
<td>287·49 287·25</td>
<td>112·82 112·78</td>
<td>468·3</td>
</tr>
<tr>
<td>14</td>
<td>287·00 287·25</td>
<td>112·76</td>
<td>433·1</td>
</tr>
<tr>
<td></td>
<td>288·25</td>
<td>114·25</td>
<td>449·8</td>
</tr>
</tbody>
</table>

A similar series of experiments was obtained at pressures less than 15 lbs. per square inch, but in this case the saturation gauge was abandoned. The stem of the globe was immersed at the bottom into a cistern of mercury open to the atmosphere; in other respects the method of the experiment was precisely the same. The water was introduced, the globe heated; and as
vaporisation went on, the mercury column descended in proportion to the increase of the elasticity of the vapour. Simultaneous readings of a barometer were taken; and by deducting from the height of the mercurial column in the barometer the height of that in the globe stem, we obtain the elasticity of the vapour in the globe for the corresponding temperature. So long as the vapour in the globe was in a condition of saturation, its elasticity thus found corresponded with that in M. Regnault's tables. When it became superheated, the ratio of increase of elasticity was very greatly reduced, and the column became almost stationary. The superheating was carried in these experiments to twenty or thirty degrees above the saturation point. The principle of the experiments was therefore entirely unchanged, the only alteration being that the elasticity of the saturated steam was obtained from previous experiments, and that of superheated steam observed, and the difference of level of saturated and superheated steam obtained by subtracting the one from the other, instead of being directly observed.

The following table gives the results obtained in this series of experiments reduced on the same principle as the last:—

<table>
<thead>
<tr>
<th>No. of Experiment</th>
<th>Maximum Temperature of Saturation, Fahr.</th>
<th>Pressure of Steam in Inches of Mercury</th>
<th>Specific Volume of the Steam</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>138·85 \ 138·70 \ 136·77</td>
<td>5·36 \ 5·34 \ 5·35</td>
<td>8275·3</td>
</tr>
<tr>
<td>2</td>
<td>155·38 \ 155·28 \ 159·35</td>
<td>8·64 \ 8·61 \ 9·45</td>
<td>5333·5</td>
</tr>
<tr>
<td>3</td>
<td>159·35 \ 169·36 \ 159·40</td>
<td>9·45 \ 9·45 \ 9·45</td>
<td>4920·2</td>
</tr>
<tr>
<td>4</td>
<td>170·88 \ 170·96 \ 170·92</td>
<td>12·46 \ 12·48 \ 12·47</td>
<td>3722·6</td>
</tr>
<tr>
<td>5</td>
<td>171·52 \ 171·44 \ 171·48</td>
<td>12·63 \ 12·60 \ 12·61</td>
<td>3715·1</td>
</tr>
<tr>
<td>6</td>
<td>174·92</td>
<td>13·62</td>
<td>3438·1</td>
</tr>
<tr>
<td>7</td>
<td>182·26 \ 182·34 \ 182·30</td>
<td>16·01 \ 16·02 \ 16·01</td>
<td>3051·0</td>
</tr>
<tr>
<td>8</td>
<td>188·30</td>
<td>18·36</td>
<td>2623·4</td>
</tr>
<tr>
<td>9</td>
<td>198·78</td>
<td>22·88</td>
<td>2149·5</td>
</tr>
</tbody>
</table>

These results show that the density of saturated steam at all temperatures above as well as below 212°, is invariably greater than that derived by calculation from the gaseous laws.
As we propose extending these experiments to higher pressures, it is premature to venture on any elaborate generalisation of the results we have attained. The following formulae, however, express with much exactness the relation between temperature and volume, and between pressure and volume, as indicated by our experiments.

Let \( v \) be the specific volume of saturated steam, at the pressure \( p \), measured by a column of mercury in inches; then

\[
v = 25.62 + \frac{49513}{p + 72} \quad (20)
\]

\[
p = \frac{49513}{v - 25.62} - 0.72 \quad (21).
\]

The following numbers show the agreement of these formulae with the experimental results:

<table>
<thead>
<tr>
<th>Temperature, Fah.</th>
<th>Specific Volume</th>
<th>Proportional Error of Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>By Experiment</td>
<td>By Formula</td>
</tr>
<tr>
<td>136.77</td>
<td>8275.3</td>
<td>8,183</td>
</tr>
<tr>
<td>150.23</td>
<td>5333.5</td>
<td>5,326</td>
</tr>
<tr>
<td>168.35</td>
<td>4420.2</td>
<td>4,909</td>
</tr>
<tr>
<td>179.92</td>
<td>3722.6</td>
<td>3,740</td>
</tr>
<tr>
<td>177.48</td>
<td>3715.1</td>
<td>3,478</td>
</tr>
<tr>
<td>174.92</td>
<td>3438.1</td>
<td>2,965</td>
</tr>
<tr>
<td>182.30</td>
<td>3051.0</td>
<td>2,985</td>
</tr>
<tr>
<td>188.30</td>
<td>2623.4</td>
<td>2,620</td>
</tr>
<tr>
<td>198.78</td>
<td>2149.5</td>
<td>2,124</td>
</tr>
<tr>
<td>212.90</td>
<td>943.1</td>
<td>937</td>
</tr>
<tr>
<td>244.62</td>
<td>902.0</td>
<td>905</td>
</tr>
<tr>
<td>255.23</td>
<td>892.6</td>
<td>900</td>
</tr>
<tr>
<td>255.50</td>
<td>759.4</td>
<td>758</td>
</tr>
<tr>
<td>263.14</td>
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<td>562</td>
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<td>428</td>
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<tr>
<td>288.25</td>
<td>449.6</td>
<td>456</td>
</tr>
</tbody>
</table>

We have also computed the following table from the experimental formula, which exhibits at a glance the pressure, volume, and weight of saturated steam, and will enable the reader to ascertain the necessary data for calculations at all pressures from 1 to 250 lbs. per square inch:
### General Table (VIII.) of the Relation of Pressure, Volume, and Weight of Saturated Steam Deduced from Experimental Data.

<table>
<thead>
<tr>
<th>Pressure</th>
<th>Specific Volume</th>
<th>Decrease of Specific Volume per lb. Pressure</th>
<th>Weight of a Cubic Foot of Steam</th>
</tr>
</thead>
<tbody>
<tr>
<td>In lbs. per sq. inch</td>
<td>In Inches of Mercury</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
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</tr>
<tr>
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<td>0.00692</td>
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<tr>
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<td>7276.6</td>
<td>0.00838</td>
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<tr>
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<td>5687.0</td>
<td>0.01258</td>
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<td>12.217</td>
<td>3552.6</td>
<td>0.01620</td>
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<td>14.253</td>
<td>3331.6</td>
<td>0.01874</td>
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<tr>
<td>8</td>
<td>16.289</td>
<td>2936.6</td>
<td>0.02126</td>
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<tr>
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<td>18.325</td>
<td>2625.4</td>
<td>0.02377</td>
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<td>2374.3</td>
<td>0.02630</td>
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<td>2167.4</td>
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<td>0.03131</td>
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<td>1846.7</td>
<td>0.03380</td>
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<td>28.505</td>
<td>1719.8</td>
<td>0.03630</td>
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<td>1612.6</td>
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<td>44.794</td>
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<td>69.227</td>
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<td>713.4</td>
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<td>Pressure</td>
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<td>Decrease of Specific Volume per lb. Pressure</td>
<td>Weight of a Cubic Foot of Steam</td>
</tr>
<tr>
<td>----------</td>
<td>----------------</td>
<td>---------------------------------</td>
<td>---------------------------------</td>
</tr>
<tr>
<td>In lbs. per sq. inch</td>
<td>In Inches of Mercury</td>
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<td></td>
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### ON THE PROPERTIES OF STEAM.

<table>
<thead>
<tr>
<th>Pressure</th>
<th>Decrease of Specific Volume per lb. Pressure</th>
<th>Weight of a Cubic Foot of Steam</th>
</tr>
</thead>
<tbody>
<tr>
<td>160</td>
<td>177.3</td>
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</tr>
<tr>
<td>170</td>
<td>168.3</td>
<td>0.78</td>
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<tr>
<td>180</td>
<td>160.5</td>
<td>0.72</td>
</tr>
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<td>190</td>
<td>153.3</td>
<td>0.64</td>
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<td>146.9</td>
<td>0.57</td>
</tr>
<tr>
<td>210</td>
<td>141.2</td>
<td>0.53</td>
</tr>
<tr>
<td>220</td>
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<td>0.47</td>
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<tr>
<td>230</td>
<td>131.2</td>
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<td>240</td>
<td>126.8</td>
<td>0.41</td>
</tr>
<tr>
<td>250</td>
<td>122.7</td>
<td>0.42</td>
</tr>
</tbody>
</table>

In the above table, which is probably the first calculated from direct experimental data, the third column is calculated by means of formula (20), and the last by dividing the weight of a cubic foot of water, at the temperature of 39.1° Fahr., by the specific volume of the steam, that is, by the volume to which a cubic foot of water expands when converted into steam.

It will be interesting to compare the numbers given by the above table with those which are obtained in an entirely independent manner from Mr. Rankine's formula, in which the volume is deduced from the latent heat. The following numbers show a near agreement in the results. With these has been placed at the same time a column giving the results deduced from the gaseous laws as they have hitherto been generally received.

### COMPARISON OF THE VALUES OF THE SPECIFIC VOLUME OF SATURATED STEAM, FROM THE FORMULAE OF MR. FAIRBAIRN AND MR. TAYLOR, MR. RANKINE, AND FROM THE GASEOUS LAWS.

<table>
<thead>
<tr>
<th>Temperature, Fahr.</th>
<th>Pressure in Inches of Mercury</th>
<th>Specific Volume</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>FAIRBAIRN and TAYLOR</td>
<td>RANKINE</td>
</tr>
<tr>
<td>104°</td>
<td>17207</td>
<td>19520 + 1</td>
</tr>
<tr>
<td>140</td>
<td>7553</td>
<td>7620 + 1</td>
</tr>
<tr>
<td>176</td>
<td>3397</td>
<td>3367 - 1</td>
</tr>
<tr>
<td>212</td>
<td>1641.5</td>
<td>1645 + 2</td>
</tr>
<tr>
<td>248</td>
<td>838.7</td>
<td>874 + 1</td>
</tr>
<tr>
<td>284</td>
<td>455.3</td>
<td>498 + 1</td>
</tr>
<tr>
<td>320</td>
<td>294.9</td>
<td>301 + 2</td>
</tr>
<tr>
<td>355</td>
<td>191.9</td>
<td>191 - 0.5</td>
</tr>
</tbody>
</table>
The fractions in the two last columns indicate the proportional deviation from the experimental formula. Within the limits of the experiments below the atmospheric pressure, that is, between 136° and 212°, both Mr. Rankine's and the gaseous results agree closely with our experiments. Above 212° both Mr. Rankine's and our own results deviate considerably from those obtained on the assumption of the gaseous laws, whilst at the same time the two former approximate nearly in value.

Fig. 155 represents graphically the relations which have been described in this section, the spheres representing the volume assumed by the same weight of steam at the respective pressures shown on the figure. It may also serve to show how the density increases and the volume decreases with the pressure according to the law determined by our experiments.

On the Latent Heat of Steam at different Pressures.

It has already been explained that in all changes in the state of aggregation of bodies heat becomes latent or sensible. If a body passes from the solid to the liquid, or from the liquid to the gaseous state, heat becomes latent; in the inverse process an equal amount of heat becomes sensible.

Black determined the amount of increase of heat in the water surrounding the worm of a still by the condensation of a weighed portion of steam, and found that the condensation of one pound of steam raised the temperature of an equal quantity of water 954° Fahr., an estimate which has since proved too low.

Watt investigated this subject in relation to the action of his condenser, and from his experiments concluded 'that the quantity of heat necessary to convert one pound of water at 32° into steam at any pressure is constant.' That is, that the latent heat of steam decreases as the pressure rises, by as much as the sensible heat increases, the total heat being constant. If we take the total units of heat of steam at 212° to be 1146·6, and if λ be put for the total units of heat, and λ₁ for the latent heat at any other temperature τ, then the law of Watt will be expressed by the formula—

\[ \lambda = \lambda_1 + \tau = 1146·6 \ldots (22) \]
Fig. 155.

Pressure in lbs. per square inch.

Specific Volume of the Steam.

---

1

17990

5

4560

10

2379

15

1609

20

1220

30

827

40

628

50

608

60

428

70

371

80

328

100

268

150

187

200

147

250

122

PART I.
Subsequently to Watt, in 1803, Southern made some experiments on the same subject, from which he deduced a different law, which has since borne his name. He concluded 'that the latent heat of evaporation is constant at all pressures,' and that the total quantity of heat increases as the pressure rises, by as much as the sensible temperature rises. Taking the same numbers as before, we have the latent heat at \(212^\circ = 1146^\circ - 180^\circ = 966^\circ\); then Southern's law is expressed in the formula—

\[
\lambda = 966^\circ + (\tau - 32^\circ) \ldots \ldots (23).
\]

Watt's law, from its simplicity, has generally been employed in calculations on the duty of the steam engine; it has been reserved for M. Regnault to ascertain, with the same accuracy and care as he determined the relation of temperature and pressure of steam, the true law of the relation of the latent heat and the pressure. The law he has discovered is expressed in its simplest form in the formula—

\[
\lambda = 1082 + .305 \tau, \ldots \ldots (24)
\]

which shows that the total heat \(\lambda\), incorporated in a pound of saturated steam at the temperature \(\tau\), is equal to the latent heat of evaporation of steam at \(32^\circ\) (nearly), increased by the product \(0.305 \tau\).

At \(212^\circ\) the total heat by all three formulæ will be the same, namely, 1146\(\frac{1}{2}\) units; but at \(300^\circ\) the total heat by Watt's law would still be only 1146\(\frac{1}{2}\); by Southern's it would be 1194\(\frac{1}{6}\); and by Regnault's it would be 1173\(\frac{1}{6}\).

The quantities of heat in the above paragraphs have been measured by 'units of heat:' it will be necessary to explain what is intended by the phrase. The unit of heat, or British thermal unit, is the quantity of heat which would have to be added to one pound of pure liquid water, at or near its point of maximum density, to raise its temperature \(1^\circ\) Fahrenheit. The French thermal unit is the quantity of heat necessary to raise the temperature of 1 kilogramme of water at or near its point of maximum density \(1^\circ\) Centigrade. It will be convenient to state that there are 3.96832 British thermal units in a French thermal unit, and 0.251996 French units in an English unit. (Rankine.)
The apparatus employed by Regnault to determine the latent heat of steam consisted of a boiler, condenser, artificial atmosphere and two precisely similar calorimeters. The boiler, made immensely strong, was of a capacity of 66 gallons, and was filled when required with newly-distilled water. From this a copper tube conveyed the steam to the calorimeters and condenser. This tube was surrounded by a dense stratum of steam in a jacket, which communicated with the same boiler, and terminated in a peculiarly formed cock, by which the steam could be sent to the calorimeters or condenser, as necessary. The condenser, a vessel of 13 gallons' capacity, kept cool by a stream of water, was employed merely to cause a continuous flow of steam through the apparatus, lest any portion should be cooled before entering the calorimeters. The air receiver, or artificial atmosphere, communicating with air pumps, was of the same character, and employed for the same purpose as in the experiments upon the relation of pressure and temperature, viz. to regulate the temperature of the steam in the boiler by maintaining perfectly uniform the pressure at which ebullition takes place. The calorimeters for measuring the heat disengaged were the most essential part of this apparatus, and consisted of two red copper cylinders, with thin metal covers. The worm consisted of a first bulb \( A \), of red copper, 0.078 inch in thickness, into which the steam to be condensed passed directly; the condensed water and steam thence passed into a second bulb \( B \), with a cock \( r \).
placed outside the calorimeter; the same bulb \( b \), had an upper
tubulure, by which it communicated with a copper worm. An
agitator, or fan, of two discs of fluted copper, served to blend
together the strata of water in the calorimeter during the
experiment. The same volume of water was introduced into
the calorimeters at every experiment, being measured in a
gauging vessel. The mercurial manometer and forcing pumps
were identical with those employed in the experiments on the
relation of pressure and temperature. When complete, the
apparatus was tested with a pressure of air of ten atmospheres,
and every leak perfectly closed.

For experiments at the atmospheric pressure, every part of
the apparatus exposed to condensation was covered with flannel.
The distributing cock was placed so that no steam reached the
calorimeters, and distillation was commenced and carried on
for about an hour, to secure perfect uniformity of temperature
throughout, and to expel the air. Cold water was then intro-
duced into the calorimeters, and a portion of the steam sent
through them, after a previous experiment for five minutes
had been made as to the amount of heat communicated to the
water by conduction at the joints. When sufficient condensa-
tion in the calorimeter had been effected, the cock was closed,
and the time and temperature were noted; the agitation of
the water in the calorimeter was however continued, and
observations of the rate of cooling by radiation were obtained.
The quantity of water condensed in the calorimeter was
allowed to flow out at the cock \( r \), and weighed.

It will be impossible here to enter in detail into all the de-
vices to obtain data for calculating the corrections to be applied
in each experiment for radiation, conduction, &c.; nor the for-
mulæ by which they were calculated. It is certain, however,
that these allowances have been made with very great accuracy;
in every case the theoretical formula has been checked by ex-
perimental data.

At high pressures the air pumps and artificial atmosphere
were connected with the apparatus; in other respects the ex-
periments were identical, and in this way results were obtained
up to a pressure of 14 atmospheres, or 205 lbs. per square inch.

For pressures below that of the atmosphere the forcing
pumps were replaced by the ordinary exhausting air pump,
ON THE PROPERTIES OF STEAM.

communicating with the reservoir of air. In this way experiments were obtained at pressures varying from 0·22 atmosphere to 0·64 atmosphere.

The most accurate formula for the latent heat of evaporation is Mr. Rankine’s:

\[ l = 1091.7 - 0.695 (\tau - 32) - 0.000000103 (\tau - 39.1)^3 \]

but for practical purposes the last factor may be omitted. In this way the following table of latent and total heat has been computed. The latent heat being calculated for a pound weight of steam, the units of heat required to raise the water from 32° to the boiling point are very nearly \( \tau - 32° \).

**Table IX.**

<table>
<thead>
<tr>
<th>Pressure in lbs. per sq. inch</th>
<th>Corresponding Temperature, Fahr.</th>
<th>Latent Heat of Evaporation in British Thermal Units</th>
<th>Total Heat from 32° Fahr. in British Thermal Units</th>
<th>Increment of total Heat per lb. pressure</th>
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### ON PRIME-MOVERS.

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<th>Corresponding Temperature, Fahr.</th>
<th>Latent Heat of Evaporation in British Thermal Units</th>
<th>Total Heat from 210° Fahr. in British Thermal Units</th>
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### On the Law of Expansion of Superheated Steam.

When steam is isolated from water and heated, it expands and decreases in density if the pressure be constant, or increases in pressure if the density (volume) be constant. In this state it is said to be **surcharged** or **superheated**, or, perhaps better, **gaseous steam**.

The earliest experiments on superheated steam are perhaps
those of Frost in America, which, however, do not appear to be reliable. Mr. Siemens adopted a simple apparatus not long since, with which he sought to determine the rate of expansion of steam isolated from water, and which gave a high rate of expansion, but his conclusions are not at all borne out by my own experiments, and his apparatus does not appear calculated to yield very accurate results.

We are at this time prosecuting some researches on this subject, which are not yet advanced sufficiently for publication. In the meantime some results within a small range of superheating, obtained during the experiments on the density of saturated steam, approximate so closely to what might have been expected to be the law in this case, whilst at the same time they were made with great care, that I believe they are entitled to greater confidence than any previous attempts at the determination of this question.

Mr. Rankine, in the absence of data, has taken as the basis of his calculations on superheated steam, in his recently published 'Manual of the Steam Engine,' the assumption that superheated steam follows precisely the gaseous laws in its expansion under the influence of heat; that is, that

\[
\frac{v}{v_1} = \frac{461.2 + t}{461.2 + t_1}
\]

Mr. Siemens' experiments do not at all agree with this assumption; they would give a higher rate of expansion. But, with a certain proviso, my own results accord with it very nearly, and would seem to show that superheated steam expands at the same rate as a perfect gas.

The proviso to which I allude is this,—that within a short distance of the temperature of maximum saturation, not exceeding about 20° Fahr., the rate of expansion is variable; close to the saturation point it is much higher than that of a perfect gas, but it rapidly decreases till, at a point at no great distance above the temperature of saturation, it becomes sensibly identical with that of a perfect gas. These results, however, do not extend over a sufficient range of temperature at present for us to deduce the true law, although their entirely independent
coincidence with the laws already known to physicists is some guarantee for their accuracy.

By the rate of expansion we mean here the fraction expressing the increment of volume for one degree of temperature Fahrenheit; for air this fraction is:

$$ r = \frac{1}{459 + t} $$

where $t$ is the temperature of the gas. Thus at 212° the rate of expansion of a perfect gas is $\frac{1}{671}$; at 300° it is $\frac{1}{759}$; at 400°, it is $\frac{1}{859}$; and so on at other temperatures.

Now in our experiments we may deduce the rate of expansion in a similar way, assuming it to be uniform for small increments of temperature; thus in experiment 6, in which the maximum temperature of saturation is 174°-92 Fahr., the coefficient of expansion for the steam between that temperature and 180° Fahr. is $\frac{1}{190}$, or three times that of air; whereas between 180° and 200° the coefficient is very nearly the same as that of air, being $\frac{1}{637}$ when air would be $\frac{1}{639}$; and the same rule is found in every experiment. The mean coefficient at zero of temperature from seven experiments below the atmospheric pressure, and calculated from a point several degrees above that of saturation, is $\frac{1}{438}$, whereas for air it is $\frac{1}{459}$, so that within the range of superheating obtained in these experiments the formula of expansion would be,

$$ \frac{v}{v_1} = \frac{438 + t}{438 + t_1} $$

The experiments seem to indicate that if the superheating had been carried further, the coefficient would have still more closely agreed with that which applies to incondensable gases. The following table gives the results upon which the previous generalisations have been founded, and which seem for the present the most reliable results we possess upon this subject. Before long I hope that we shall be able to lay before the
public some direct experiments upon this subject, carried to a high degree of superheating.

The following table gives the value of the coefficient of expansion for superheated steam, taken at different intervals of temperature from the maximum temperature of saturation:

**Table showing the Coefficient of Expansion of Superheated Steam.**

<table>
<thead>
<tr>
<th>No. of Exper.</th>
<th>Maximum Temperature of Suction</th>
<th>Temperatures between which the Expansion is taken</th>
<th>Coefficient of Expansion of Steam</th>
<th>Coefficient of Expansion of Air</th>
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<td>¥/η</td>
</tr>
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<td>2</td>
<td>165°-33</td>
<td>160 - 190</td>
<td>¥/η</td>
<td>¥/η</td>
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<tr>
<td>3</td>
<td>159°-36</td>
<td>159.2 - 209.9</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>5</td>
<td>171°-48</td>
<td>171.48 - 200</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>6</td>
<td>174°-92</td>
<td>174.92 - 200</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>7</td>
<td>182°-30</td>
<td>182.3 - 209.5</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>8</td>
<td>188°-30</td>
<td>188 - 211</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>9</td>
<td>255°-5</td>
<td>257 - 259</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>10</td>
<td>267°-21</td>
<td>268 - 271</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>11</td>
<td>269°-2</td>
<td>271 - 273</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>12</td>
<td>279°-42</td>
<td>283 - 285</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
<tr>
<td>13</td>
<td>292°-58</td>
<td>297 - 302</td>
<td>¥/η</td>
<td>¥/η</td>
</tr>
</tbody>
</table>

The limited extent to which the superheating is carried leaves the question of efficiency at higher temperatures unsolved. We believe we are perfectly conversant with the costly machinery that is used for this purpose on board ship and in other places, but until more reliable data have been determined by direct experiment, it would be premature to pronounce by what law the advantages assumed to result from its use are produced. We hope in entering on this inquiry to arrive at conclusions founded on the unerring principles of physical truth.
CHAPTER VII.

VARIETIES OF STATIONARY STEAM ENGINES.

The steam engine as an instrument of propulsion is at the present time of such vast importance as to sink into insignificance every other known agent as a motive power. We have already considered the best methods by which the power of water can be utilised, but the whole of the water power in Great Britain falls immeasurably short of that obtained from steam, in every department of useful art. If we were to stop for a moment to compare the amount of steam power employed in industrial operations, with that of wind or water, we should find that the latter were mere fractions in the sum; and looking forward to still further developments in its application, I have taken some pains in the preceding chapter in giving a concise account of the properties of water when converted by the agency of heat into vapour or steam. I have considered these facts of vital importance to a knowledge of its economical employment and application, and I have dwelt longer on the inquiry than I originally intended, in order that I might have an opportunity of rendering accessible the results of experiments on the density of steam, and that the subject might be clearly and distinctly understood before treating of the construction of the steam engine.

It is not my object in this treatise to follow historically the many changes and improvements which have been effected in the steam engine since it left the hands of Watt. Suffice it to observe, that there has been no change in the principles of its action, unless we are to reckon as such the recent employment of gaseous instead of saturated steam. All the other improvements, in whatever form they present themselves, are confined
to alterations of the organic parts of the engine, but have
effectively no change in the principle of action.

Taking then the condensing engine in its best and most
economical form, I shall endeavour to lay before the reader
some examples of the best and most recent construction, adapted
for mill purposes in all the conditions of manufacture to which
they are applied. In making a selection of those of medium
size, I have chosen for illustration those at Saltaire, near Bradford,
of 100 nominal horse-power each. Those engines are
the best known for mills and factories, and the description of
them will include the essential features of every other condensing
beam engine.

Stationary Beam Engines.

At Saltaire the engines required to drive the machinery con-
sist of two pairs of condensing beam engines, each engine being
of 100 nominal horse power, or collectively 400 nominal horse-
power. They are placed on either side of the principal entrance
to the mills, and are supplied with steam from boilers placed
underground, at a short distance in front of the mill.

Plate V. contains a side elevation of one of these engines,
and Plate VI. a plan of one engine-house with its pair of
engines. The general arrangement will be understood when it
is noticed that the power generated in the cylinders c, and trans-
mitted through the working beam b b, to the large spur fly-
wheel w, 24 feet in diameter, is taken direct from its circum-
ference by the pinions p p, which give it off at the required
velocity to the shafting of the mill.

The working beam b b is supported on two massive columns
c, 16 feet high, 14½ inches in least diameter, and 1½ inch thick
of metal; these columns are bolted down beneath the whole
mass of masonry supporting the engine. The heavy entable-
ment e bolted to each column, and to the columns of the adjoining
engine, is firmly fixed in the walls of the engine-house on
each side, and the spring beams a a over this and at right angles
with it are similarly attached to the cross beams b b. In this
way an exceedingly strong and rigid support is secured for the
main centre of the engine, which, resting in its pedestal a, has to
sustain the principal strain of working. The spaces between the spring beams and the walls, excepting where the main beam vibrates, are filled with ornamental perforated metal plates, forming the beam-room, approached by the staircase \( f \), for the purpose of oiling the centres, repairs, &c. The working beam receives its motion from the piston-rod \( g \), through the parallel motion \( h h \), and transmits it by the connecting-rod \( f \) and crank \( g \) to the fly-wheel \( w \).

The steam is brought from the boilers through a prolongation of the tunnel or flue in which the smoke passes to the chimney, and enters the engine-house by the pipe \( n \). Having thence been admitted to the cylinder through the valve chests \( k k \), it repasses after it has completed its work to the condenser \( n \), through the eduction pipe \( k \), in the usual way. The condenser is supplied with cold water from the river Aire, by the pipe \( k k \), which communicates with the cold-water cistern \( j \); the injector through which the water enters the condenser is in these engines 6 inches bore, but the supply of water may be diminished if necessary by the injection gear hereafter described. Beside the condenser is the air-pump for pumping out the water and the air which enters with the water into the condenser, and is worked by the rod \( l l \) from the beam through a part of the parallel motion. A pump to supply the cold-water cistern is worked by the rod \( n \), and another pump is worked by the rod \( p p \), by which part of the hot water from the condenser is pumped back again for the supply of the boilers, in proportion as the water in them is decreased by its evaporation into steam. The supply of steam to the engine is regulated by the governor \( n \) acting on the throttle valve \( q \), and thus the speed of the engine is kept uniform. A shaft \( s s \), receiving motion from a bevel wheel on the crank shaft, works the equilibrium valves in the chests \( k k \), as will be described; \( t t \) is a flooring or stage by which access is gained to the cylinder covers for oiling and cleaning. The cylinder is 50 inches in internal diameter, and has 7 feet stroke; it stands on the circular cylinder bottom \( c' \), which is firmly bolted to the masonry by the long holding down bolts \( t t \).

The length of the engine-house is 50 feet, and its breadth 24 feet. It will be seen that the two engines are combined so as
to act in concert upon the same crank-shaft and fly-wheel, the cranks being placed at right angles to each other, that when one engine is passing its top and bottom centres, and exerting least power, the other is in mid stroke and exerting its whole power upon the full leverage of the crank. In this way the action of the engines is equalised, and the motion rendered smoother than is possible with an independent engine, whilst, in case of accident to either of the pair, its fellow may be employed alone until the damage is made good.

Plate VII. exhibits a half-elevation and half-section of the valve chests, condensers, air-pumps, &c., of a pair of engines, showing the valves and the manner of working them. As before, c c are the cylinders, c' c' the cylinder bottoms, x x the upper, and x' x' the lower valve chests, fixed right over the cylinder ports and communicating by the side pipes t t'. d d is the steam pipe, h h the condensers, l l air-pumps, with their valves v v v; m the hot well into which the air-pump lifts the water accumulating in the condenser. This water passes away by the overflow pipe m; p p p are feed pumps for supplying the boilers, with an air vessel p', for equalising the pressure and preventing any sudden shocks in the pipes; u, injection cock and injeciter, the quantity of water admitted being regulated by the injection cock, worked by the hand wheel f, through the medium of the small shafts and bell cranks n n.

The valves in these engines are of a peculiar construction, being modifications of the double beat or equilibrium valve, invented by Mr. Hornblower, and generally employed in the mining engines in Cornwall, where the high price of coal has led to that rigid economy for which its engineers have long been so justly famous. Most of the appliances for using steam expansively in rotative engines (i.e. in mill engines as distinguished from pumping engines), are open to the objections,—1st, of wire-drawing the steam; 2nd, of cutting it off too slowly; and 3rd, of leaving too much space between the cut-off valve and the cylinder, whereby much steam is wasted without producing its due mechanical effect. To remedy these defects I have employed the particular arrangement of valves shown in the plate, which are applicable to all rotative engines working expansively, whether with high or low pressure steam.
The steam entering the upper steam chest $x$, through the stop valve $a$, has free access also to the lower steam chest $x'$. through the side pipe $t$; whilst the exhaust steam has also clear access to the condenser, through the other side pipe $t'$. The steam is admitted to the cylinder from the valve boxes by means of the valves $x$ and $x'$; and after having completed its work it passes through the exhaust valves $y$ and $y'$ to the condenser, these valves being opened and shut, alternately, at the right instant by an apparatus yet to be described. Each of the valves consists of two single conical valves $a$, 1 and 2, carefully secured together and accurately fitting their seats; the lower valve is slightly smaller than the upper. The steam is admitted on the upper and lower side of each of these pairs of valves and presses in opposite directions, so that the downward pressure on the upper valve is neutralised by the upward pressure on the lower, excepting that a slight preponderance is given to the former in consequence of the difference of area in the valves, in order to aid in keeping the valves firmly pressed upon their seats when released by the cams. Hence they lift with the greatest ease and expose any required opening for the admission or exit of the steam.

The mode of working these valves is very simple; a shaft $s$ (Plate V.) receives motion from the crank shaft, and imparts it by the bevel wheels $b$ to the horizontal shaft $c$; this in turn gives motion to the valve spindles $d d$, which pass continuously through bearings in the valve chests, and are supported on footsteps on the brackets $e e$. Upon each of these spindles are fixed two discs $g g$, carrying cams upon their upper surfaces, so arranged as to lift and release each valve at the proper instant of time. This is effected by a direct and simple action; the height of the cam corresponds with the lift of the valve, its length with the duration of the lift, and its position on the cam disc, which makes one revolution for every stroke, regulates the instant of time in the course of the stroke at which the valve is opened and shut. The action of the cams is transferred to the valves through the medium of friction pulleys $k k k k$, fixed upon small cross-heads, which are guided in their upward and downward motion by the brass standards in which they work. In the case of the steam valve these pulleys are capable
of adjustment by sliding them along the cross-head, towards or away from the valve spindle, so as to bring them over different parts of the cam, which is so arranged that the steam may be cut off at \( \frac{1}{3}, \frac{2}{3}, \frac{3}{4} \), or any required portion of the stroke, the remainder being effected by the expansion of the steam.

The exhaust steam requiring a full opening into the condenser, it is desirable to retain the exhaust valve fully open during the whole length of the stroke. By the present arrangement this is effected with a greater degree of certainty than by any other means hitherto proposed. The exhaust valves rise suddenly on the short inclined planes of the cams, and having allowed time for the escape of the steam through a wide passage to the condenser, they fall with equal celerity by their own weight; thus a more complete vacuum is formed under the piston than is perhaps possible to obtain by any other process.

The stop valve \( \alpha \) is a simple conical valve, worked by a lever and hand wheel \( z \), fixed by a bracket to the side of the steam chests, and is chiefly used for shutting off the steam from the engine.

The following diagrams were taken from these engines on May 4th, 1859. The engines were then working at 25 revolutions per minute, and one pair with part of the load off:—

<table>
<thead>
<tr>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diameter of cylinder</td>
<td>50 ins.</td>
</tr>
<tr>
<td>Area</td>
<td>1963.50 ins.</td>
</tr>
<tr>
<td>Speed of piston</td>
<td>350 feet per minute</td>
</tr>
<tr>
<td>Scale of diagrams</td>
<td>( \frac{1}{8} ) inch per lb. pressure</td>
</tr>
</tbody>
</table>

**Engine A.**

From this diagram we get:—

\[
\begin{align*}
\text{Mean pressure of steam} & = 7.1684 \\
\text{Deduct for friction, &c.} & = 2.0000 \\
\text{Effective pressure} & = 5.1684
\end{align*}
\]

\[\therefore \text{Actual horse-power} = 107.63.\]
Engine B.

From this diagram we get:—

Mean pressure of steam . . . = 7·3646
Deduct for friction, &c. . . . = 2·000
Effective pressure . . . = 5·3646

∴ Horses-power = 111·46.

Engine C.

From this diagram we get:—

Mean pressure of steam . . . = 13·301
Deduct for friction, &c. . . . = 2·000
Effective pressure . . . = 11·301

∴ Horses-power = 235·34.

Engine D.

From this diagram we get:—

Mean pressure of steam . . . = 12·946
Deduct for friction, &c. . . . = 2·000
Effective pressure . . . = 10·946

∴ Horses-power = 227·95.

Collectively 682·38 horses-power.

With a higher pressure of steam, or a shorter expansion, these engines will work to nearly double the above, or 1,200 horses-power.

Fig. 158 represents the cylinder, and its base, of the Saltaire engines. The cylinders are 50 inches internal diameter, with 7 feet stroke, of metal 1½ inch thick. The ports are twenty inches wide, by 6 inches deep, so as to give 1/8 the area of the piston for the admission and exit of the steam. The equilibrium valves have the upper disc 12 inches diameter, or 113 inches area, the lower disc 10½ inches diameter, or 86½ inches area, lift of steam valves 1½ inch; of exhaust valves 1½ inch. Steam pipes, 12½ inches diameter; exhaust, 13 inches; condenser, 40 inches; air pump, 33½ inches, and 3 feet 6 inches stroke. Beam 21 feet 6 inches long between the end centres, or over three times the stroke; and 3½ feet deep in the middle,
or \( \frac{3}{4} \) the length. Main centre of wrought iron 12 inches diameter in the beam and 9 inches in the bearings. Spur fly wheel 24 feet 6 inches in diameter, with 230 cogs on the rim, 14 inches broad, 4 inches pitch; the rim is in 10 segments and has a sectional area of 200 square inches.

It is now more than thirty years since it was found desirable to increase the power of the steam engines employed in manufacture, and instead of engines of from 20 to 50 nominal horse-power, as much as 100, and in some cases 200 horse-power were required to meet the demand. To keep pace with the rapid extension of our manufactures, not only was the power itself doubled, and in some cases quadrupled, but a new class of men was brought into existence as mechanical engineers, and these, with the facilities afforded by new constructions and improvements of tools, gave to the manufacture of steam engines, and machinery of every description, an impetus that in a few years produced steam engines in an accelerated ratio of ten to one.

For some years previous to the great demand for power, the mills were driven by single engines, some as much as 50 or 60 horse-power, but these had soon to give place to others of much greater force, or, what was found to answer much better, two were employed coupled together as described above. Working in pairs, they were found to afford greater uniformity of action from the cranks being placed at right angles. Again, it was found that the speed of 240 feet per minute, considered as the maximum by Watt, was insufficient with the increasing demand for power, and speeds of 320 to 350 feet per minute are now become general. In some of the old engines, however, with
such an increase of speed, the breakages became so numerous as to cause a retrograde movement, and a return to the old speed.

The increase of speed was, however, inadequate to meet the requirements for power in many cases, and the next resource was to increase the pressure of the steam. Unfortunately many of the boilers and engines were not calculated to withstand the forces to which they were thus subjected, and the result was an increase of the number of breakages and explosions to an extent that was ruinous to life and property. The ultimatum of all this was to increase the number of steam engines with an entirely new description of boiler, calculated to withstand higher pressures, and maintain the speed required to work the engine up to the required standard of power.

In the above statement I do not mean to attach blame to any person in his attempts to increase the power of the steam engine to meet the demands of the mill. On the contrary, the majority of manufacturers were against an increase of speed or pressure on account of the dangers they entailed, and the heavy responsibilities attached to them when the lives of workpeople were at stake, and it required a long series of years, in which I advocated the use of high-pressure steam, before the reluctance of the manufacturers was overcome. That is, however, now accomplished, and along with an improved principle of construction in boilers, the steam engine is no longer, when worked with steam of only one-fourth the pressure, what it used to be. To what extent the pressures may yet be carried, and how far the steam may be expanded, is a question still open for solution. But judging from what has already been done, the inference is that we have not as yet attained the maximum pressure, nor the rate of expansion calculated to afford the greatest economy in the use of steam as a source of power.

To accomplish the increase of pressure no change has taken place in the engine itself, beyond the strengthening of the parts, and the substitution of wrought iron and steel for parts which were before considered sufficiently strong of cast iron.

Where additional power was required in mills which could not be obtained by increasing the speed and pressure of the old engines, horizontal, high-pressure non-condensing engines
were sometimes introduced, and these, in the manufacturing districts, are commonly called Thrutchers. These Thrutchers have been largely employed in Staleybridge and the surrounding district, and although not of great value on the score of economy, they are, nevertheless, important as auxiliary to the larger condensing engines. They are generally attached to the main gearing or first motion wheels, and the steam, which enters their cylinder at 50 lbs. pressure, exhausts into the cylinder of the condensing engine, and is there expanded and worked over again. This system of double action would appear favourable to the expansive process, but unfortunately the distance

Fig. 159.

of the high-pressure cylinders from those of the condensing engine, and the consequent loss of heat by radiation and the retardation from friction, including the complicated nature of the connections, &c., is so great as to neutralise or destroy the economy of fuel which would otherwise have been secured.

There is, however, a considerable saving in original cost, which to a certain extent balances this drawback and renders the Thrutchers valuable as an auxiliary power. In cases where engines are overloaded, and where it is impossible for want of space to erect new engines on the first principle of construction,
the horizontal non-condensing engines are admissible, and may be used with advantage.

The annexed sketch (fig. 159) will explain the mode of connecting the horizontal high-pressure with the vertical condensing engines. At \( \alpha \alpha \) are shown a pair of 60 horse-power engines with the cylinder \( e e \) and fly-wheel \( e e \). At \( \beta \) are the double high-pressure engines with their cylinders \( c \), and their connection with the main shaft \( b b \), by a spur fly-wheel and pinion \( d d \). In this way all the four engines are united; a certain portion of the lower part of the mill being occupied with the auxiliary engines \( \beta \), and with a new set of boilers to supply the steam at the requisite pressure.

The great deficiency of power severely felt in many establishments, has been supplied in some cases by another method, without resorting to the erection of new engines, and that is by McNaughting the old ones. This process, the invention of Mr. McNaught, consists in increasing, or even nearly doubling, the power of a condensing engine by the introduction of a high-pressure cylinder attached to the same working beam, that is, provided the beam is strong enough to bear the increase of
to act in concert upon the same crank-shaft and fly-wheel, the cranks being placed at right angles to each other, that when one engine is passing its top and bottom centres, and exerting least power, the other is in mid stroke and exerting its whole power upon the full leverage of the crank. In this way the action of the engines is equalised, and the motion rendered smoother than is possible with an independent engine, whilst, in case of accident to either of the pair, its fellow may be employed alone until the damage is made good.

Plate VII. exhibits a half-elevation and half-section of the valve chests, condensers, air-pumps, &c., of a pair of engines, showing the valves and the manner of working them. As before, c c are the cylinders, c' c' the cylinder bottoms, k k the upper, and k' k' the lower valve chests, fixed right over the cylinder ports and communicating by the side pipes t t'. d d is the steam pipe, h h the condensers, l l air-pumps, with their valves v v v; m the hot well into which the air-pump lifts the water accumulating in the condenser. This water passes away by the overflow pipe m; p p p are feed pumps for supplying the boilers, with an air vessel p', for equalising the pressure and preventing any sudden shocks in the pipes; u, injection cock and injector, the quantity of water admitted being regulated by the injection cock, worked by the hand wheel f, through the medium of the small shafts and bell cranks n n.

The valves in these engines are of a peculiar construction, sing modifications of the double beat or equilibrium valve, invented by Mr. Hornblower, and generally employed in the dining engines in Cornwall, where the high price of coal has tended to that rigid economy for which its engineers have long been so justly famous. Most of the appliances for using steam expansively in rotative engines (i.e. in mill engines as distinguished from pumping engines), are open to the objections,—st, of wire-drawing the steam; 2nd, of cutting it off too lowly; and 3rd, of leaving too much space between the cutoff valve and the cylinder, whereby much steam is wasted without producing its due mechanical effect. To remedy these effects I have employed the particular arrangement of valves shown in the plate, which are applicable to all rotative engines working expansively, whether with high or low pressure steam.
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and the facility of getting to every part in case of repairs being necessary, give it a superiority over every other form, however perfect and compact. Besides, the engineers (or engine tenters, as they are called in the manufacturing districts) find there is less trouble in cleaning, and there is therefore a desire on their part to have the old construction in preference to every other. From these considerations the old Boulton and Watt form of engine, strengthened and improved by being adapted to work expansively, is now the favourite, and is likely to maintain its ground as long as steam is depended on as the source of power in mills.

In the consideration of steam as a prime-mover, it would be unjust to omit to notice the modification of Woolf, so extensively used on the Continent, where fuel is expensive, and where the greatest economy in its use has been an object of serious consideration.

For the last half century Woolf's engine has been preferred in France and other countries on the continent of Europe, and this has arisen from the fact that until the last fifteen years the single cylinder engine has been worked with low pressure steam only, without expansion. Now it is evident that the single cylinder engine worked with full steam throughout the stroke, will require a larger expenditure of fuel than another engine worked expansively. Thus the double cylinder or compound engine, in which high-pressure steam was employed, expanded through three-fourths of the stroke, appeared to effect a considerable saving of fuel; but taking both engines worked alike, with steam of the same pressure similarly expanded, as is now the case in the best single cylinder engines, there appears to be no advantage in the compound over the simple single cylinder engine. On the contrary, there is a loss in the original cost of the engine, and the complexity of the one as compared with the other. I have therefore no hesitation in recommending the single cylinder engine worked expansively, as an efficient competitor of the compound engine.

Fig. 161 is a view of the two cylinders and valve chests of a Woolf's engine. The small or high-pressure cylinder is shown at $a$, 23 inches in diameter and 6 feet stroke, and the large or low-pressure cylinder at $b$, 40 inches in diameter and 8 feet
stroke; their contents being as 1 to 4. The steam is brought from the boiler by a pipe not shown in the drawing, which admits the steam into the annular passage c c, whence it passes into a valve chest d of the ordinary construction. This valve chest communicates by the passages f and h with the two valve chests c c of the large or low-pressure cylinder b, and the exhaust steam from a passes into these, and is expanded to four
times its bulk in the larger cylinder, which has no direct communication with the boiler. The steam from the upper side of the piston of the high-pressure cylinder passes to the lower part of the larger cylinder, and in this way a simultaneous upward or downward motion of the pistons in the two cylinders is secured. After the steam has been thus expanded, and the work so economised, it passes by the pipe to the condenser.

The valves of the large cylinder are equilibrium valves, like those of the Saltaire engines, but differently moved. A reciprocating motion is given to a crank by means of an eccentric on the fly-wheel axis. This motion is communicated by a connecting rod and bell crank to the two rods which slide with freedom in a vertical direction. Upon these rods at suitable heights are fixed the arms and lifting the valves for the admission of the steam into the cylinder, and those for the exhaust. The valve of the high-pressure cylinder is similarly worked by an arm connected with the rod, not shown in the drawing.

Before closing our notice of the varieties of steam engines, we have to describe the horizontal condensing engines in which the cylinder is placed horizontally upon a cast-iron frame or bed-plate. This arrangement presents all the features of cheapness and concentration which we noticed in the high-pressure Thrutchers already described. The condensing engine, however, works to 12 lbs. or 13 lbs. under the atmospheric pressure, and thus economises part of the work of the steam which is lost in the Thrutchers, with the additional disadvantage that they work against a considerable back pressure. It is for these reasons that the high-pressure non-condensing engines are not in demand where a large amount of power is required. They are, however, simple and effective, excepting as regards economy of fuel. In some cases they are preferable to the condensing engine, and that is in small establishments and as auxiliaries to water wheels when the supply of water fluctuates, and a small engine is needed when the supply is deficient. In large establishments, and more especially where coal is dear, the high-pressure engine must give place to the condensing. The horizontal condensing engine presents some of the advantages of
both classes of engines, as it is economical as regards fuel, and at the same time is lighter, more compact, requires less space, and costs less money than a beam engine. These are its merits. Its drawbacks are the horizontal position of the cylinder, involving unequal wear of the parts, and the tendency of the cylinder to become oval.

Fig. 162 represents a horizontal condensing engine, in which \( \text{c} \) is the cylinder, \( \text{s} \) slide bars carrying the crosshead on the piston rod, from which is worked the fly-wheel \( \text{F} \) by the connecting rod \( \text{r} \), and the bell crank \( \text{b} \), by a short link. This bell crank transmits motion to the piston of the air-pump \( \text{a} \), communicating in the ordinary manner with the condenser \( \text{d} \). The working parts of the engine are firmly fixed on the iron bed-plate \( \text{A} \).

High-pressure Engines.

Engines working without condensation are now frequently employed as auxiliaries, and where the amount of power required is not large. It will not be necessary to describe here all their varieties, but they may be briefly enumerated as, 1st.
Horizontal engines, like the last described, but without the condenser; 2nd. Columnar engines, in which the action is vertical, the framing being in the form of a hollow cylindrical column; 3rd. Vertical engines, with the cylinder placed above the crank and working downwards; 4th. Oscillating engines, in which the crank is worked direct from the piston rod, and the cylinder oscillates upon trunnions near its centre, to allow of the re-
quisite vibration of the crank; 5th. Steeple engines, in which the piston rod carries a crosshead, from which the connecting rod works downwards to the crank.

One example of the best of these varieties will be sufficient for our purposes in this place. Figs. 163 and 164 represent the columnar engine, which from its simple, compact, and neat form, is probably superior to most other constructions; it combines several advantages from its vertical position, and the ease with which it is supported on two iron beams, $b b$, built into the walls of the engine-house for that purpose. In this way the necessity for heavy foundations is entirely done away with, and the boiler may be placed immediately below the engine, in order to be
close to its work, and to save space. The annexed drawings represent a front and side elevation of an engine of this description of six horses-power, but the same principle has been successfully extended to engines of thirty horses-power. The piston rod is cottered in the usual way into a crosshead, carrying blocks which slide in fixed guides on each side of the columnar framing of the engine; the connecting rod \( r r \) is attached to this crosshead, and also to the crank overhead. \( c \) is the cylinder with its valve chest, the valves being of the short \( d \) construction, worked by the eccentric \( e \) on the crank shaft. On the other side of the column, the pump for supplying the boiler with water is worked by a stud on the piston crosshead.

The governor \( g \), attached at the side of the column, is worked by a bevel wheel, upon the crank shaft, and the pipe for supplying steam \( f f \) enters the valve chest, having a stop valve worked by a handle \( h \) placed at the side of the column.

In most of the engines hitherto described, the motion of the engine has been transmitted direct from the periphery of the fly-wheel to the gearing of the mill. This plan I introduced nearly twenty-five years ago, and applied both to water wheels and to steam engines; in the former case, the gearing is usually internal, as shown in the Plates I., II., III., and IV., and in steam engines it is usually external, as shown in Plates V. and VII. But this rule is by no means absolute, as in part of the Deanston water wheels external spur gearing was employed: and in the columnar engine figured above, I have shown an internal geared fly-wheel. On the introduction of this method of obtaining direct the necessary speed in the first motion shaft, by gearing the periphery of the fly-wheel, I met with opposition on all sides, and it was not till a wheel of thirty-six tons' weight had been constructed for a pair of engines of 240 horses-power, that the more sceptical were convinced that the regularity of motion was not impaired, and that the train of geared wheels had been abandoned, with a material saving of power, and economy of prime cost. This system of connecting the prime-mover with the machinery of the mill greatly simplifies the motion, by attaining the required velocity at once, without the aid of speed gearing necessary where the motion
is taken from the fly-wheel shaft. This system has now become universal in stationary steam engines.

The duty of engines, or amount of work done for a given quantity of coal consumed, has gradually improved as the engine itself has been modified. Smeaton’s table of the effect of fifteen atmospheric engines at work at Newcastle in 1769 give a mean of 5,590,000 lbs. raised one foot per bushel of coals per hour. This is equivalent to an expenditure of 29·76 lbs. of coal per horse-power per hour. In Smeaton’s own engine, erected at Long Benton, an improved duty of 9,450,000 lbs. raised one foot per bushel of coal was obtained, equivalent to an expenditure of 17·6 lbs. per horse-power per hour. In Watt’s engines the expenditure of fuel was further reduced to so large an extent that the payment for them was made proportional to their economy, one-third of the annual saving of fuel obtained by their use being paid during the term of the patent. In the earliest of Watt’s engines without expansion the expenditure appears to have been about 8½ lbs. to 9 lbs. per horse-power per hour. At the present time, in condensing engines working expansively, a duty as high as 2·6 lbs. of coal per horse-power per hour has been obtained, or 11⅓ times the amount of work for the same consumption of fuel as in the early atmospheric engines.

The following tables have been carefully compiled by Mr. H. Harman, late Chief Inspector of the Association for the Prevention of Boiler Explosions in the districts of Lancashire and Yorkshire, from the extensive returns furnished to that association. They show most significantly the progressive economy arising from the use of high-pressure steam, and from a long expansion.
<table>
<thead>
<tr>
<th>Description of Engine</th>
<th>15 lbs. and under</th>
<th>16 lbs. to 30 lbs.</th>
<th>31 lbs. to 45 lbs.</th>
<th>46 lbs. to 60 lbs.</th>
<th>Above 60 lbs.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>No. of Engines</td>
<td>Indicated Horse-power per hour</td>
<td>Indicated Horse-power per hour</td>
<td>Indicated Horse-power per hour</td>
<td>Indicated Horse-power per hour</td>
</tr>
<tr>
<td>Condensing...</td>
<td>20</td>
<td>969</td>
<td>10-6</td>
<td>198</td>
<td>24,674</td>
</tr>
<tr>
<td>Non-condensing...</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Working compound...</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Steam cut off before $\frac{1}{2}$ stroke...</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Condensing...</td>
<td>13</td>
<td>671</td>
<td>10-3</td>
<td>105</td>
<td>10,840</td>
</tr>
<tr>
<td>Do. $\frac{1}{2}$ to $\frac{3}{4}$ stroke...</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Do. later than $\frac{3}{4}$ stroke...</td>
<td>6</td>
<td>245</td>
<td>10-6</td>
<td>16</td>
<td>1,577</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Maximum consumption of coal per hour</th>
<th>Minimum consumption of coal per hour</th>
</tr>
</thead>
<tbody>
<tr>
<td>17-0 2-6</td>
<td>23-0 5-5</td>
</tr>
<tr>
<td>11-0 3-0</td>
<td></td>
</tr>
<tr>
<td>Description of Engine</td>
<td>15 lbs. and under</td>
</tr>
<tr>
<td>-----------------------</td>
<td>-------------------</td>
</tr>
<tr>
<td></td>
<td>No. of Engines</td>
</tr>
<tr>
<td>Condensing</td>
<td>4</td>
</tr>
<tr>
<td>Non-condensing</td>
<td>-</td>
</tr>
<tr>
<td>Working compound</td>
<td>-</td>
</tr>
<tr>
<td>Steam cut off before 1/2 stroke</td>
<td>1</td>
</tr>
<tr>
<td>Steam cut off between 1/2 and 3/4 stroke</td>
<td>1</td>
</tr>
<tr>
<td>Steam cut off later than 3/4 stroke</td>
<td>2</td>
</tr>
</tbody>
</table>
In reference to the apparent superiority of the compound engines in the last table, Mr. Harman observes 'that, owing to increased friction, &c., engines which have been compounded invariably indicate more horses' power than before, the machinery remaining the same; hence arises an advantage, apparent and not real, in calculating the consumption of fuel. . . . .

Consideration has led me to conclude that the gross amount of power exhibited by compound diagrams as at present calculated is fallacious.'
CHAPTER VIII.

ON BOILERS.

Vessels for the generation of steam for supplying steam engines are of a great variety of forms, and are usually deno-
minated boilers. These vessels require great care and judgment
in their construction, in order that the fuel may be most
economically applied, the waste and nuisance of smoke avoided,
and the enormous force which steam is capable of exerting at
high temperatures safely restrained.

The boiler is, in fact, to the steam engine what the living
principle is to animated existence. Like the stomach, it re-
quires food to maintain the temperature, circulation, and con-
stant action, which constitute the energy of the steam engine
as a motive power. To keep up the temperature we have to
feed, stoke, and replenish the furnace with fuel, and we may
safely consider it a large digester, endowed with the functions of
producing that supply of force required in the maintenance of
the action of the steam engine.

The boiler has undergone great changes of
form and construction to adapt it to use. At
first it was hemispherical, fig. 165, as when em-
ployed by Newcomen, which shape was retained
for many years with certain modifications. Sub-
sequently it was altered by Watt to the form of
a parallelepipedon with a semi-cylindrical top,
as shown in fig. 166. This form of boiler was
extensively used by Watt in the early stages
of his steam engines, and continued to take
precedence of every other description of vessel
employed for the production of steam. It was
however, modified by the introduction of a
central flue, and a slight modification of its ex-
terior shape to enable it to withstand greater pressures. Fig. 167
represents the improved form of boiler, in which, in addition to the curvature introduced along the bottom, the sides were also constructed in that form, the better to resist the pressure of the steam, which at that time was increased from 7 lbs. to 10 lbs. on the square inch.

Simultaneously with these improvements Woolf and Hornblower introduced high pressure boilers of the cylindrical form, some with hemispherical ends, fig. 168, and others with flat ends having a cylindrical flue through the centre, fig. 169. Boilers of this sort were extensively used in Cornwall, where the pumping of the mines by steam engines on Woolf's plan required a pressure varying from 30 lbs. to 40 lbs. per square inch. The same description of boiler was adopted by Watt in his pumping engines, first erected in Cornwall, and worked expansively on the principle of cutting off the steam at an early point in the stroke.

It was in the Cornish districts that the first great improve-
VARIETIES OF BOILERS.

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ments in boilers took place. The high price of coal became an important item in the use of pumps for draining the mines, and every measure of economy was resorted to for a reduction of the cost. The result was the introduction of the cylindrical boiler, fig. 169, with a central flue, and a system of premiums to the superintendents for every bushel of coal saved in raising a given weight of water out of the mines. This system of premiums worked well in Cornwall, and I apprehend the steam engines of those districts are still worked with greater economy than in any other part of the kingdom. The Cornish miners pay more attention to their engines, are more careful of their boilers, and are stimulated to a more rigid economy than in any other part of the kingdom. They are never short of boiler space, and never force their fires or increase the power of their engines, without increasing the capacity of their boilers. These conditions give to the Cornish engines the advantages which are lost sight of in other districts, to such an extent, in some instances, as to increase the consumption beyond all reasonable bounds. Of late years great improvements have been effected in this respect, and further progress in the same direction will doubtless lead to similar results in the economical use of steam.

Exclusive of the Cornish principle of construction, boilers have been introduced of a cylindrical form, with a central ellip-

Fig. 170.

tical flue, and with the bottom cut away at one end to a distance of 8 feet, as shown in fig. 170, to admit a large furnace under
that part. It will be seen that this boiler, from the large concave arch at A, and the elliptical flue, inherits all the defects of the waggon form, fig. 167, and could not therefore be employed, without danger of explosion, at pressures above 12 lbs. per square inch. From its peculiar shape it took the name of the Whistlemouth, or Butterley boiler, and with its internal flue, through which the products of combustion pass, it presents a large heating surface, and was for several years considered an improvement upon Boulton and Watt's boiler. Like its predecessors it gave way to others better calculated to generate high pressure steam.

The next improvement was the Cornish boiler, with a furnace in a large cylindrical flue at one end, fig. 169, but this, from the large diameter of the flue, was liable to explode from collapse, and led to the strongest and most perfect boiler yet constructed for stationary purposes, namely, the double-flued boiler with two furnaces and alternate firing. This boiler, if made of the best material and properly constructed, will resist, with plates \( \frac{3}{8} \)ths of an inch thick, a pressure of upwards of 300 lbs. per square inch (that is, assuming the shell of the boiler to be 7 feet diameter), and as it is now almost universally adopted, we shall give a fuller account of its proportions.

Fig. 171 exhibits a longitudinal section, and fig. 172 a front view and a cross section of a double-flued stationary boiler, as I have been accustomed to construct it. It was originally
VARieties OF BOILERs.

Devised with a view to alternate firing in the two furnaces, in order to prevent the formation of smoke; it consists of an external cylindrical shell with flat ends, and has two similar cylindrical flues, \( a a \), passing through the water space of the boiler. The shell is six feet to seven feet in diameter, and twenty to thirty feet in length, and composed of \( \frac{1}{10} \) to \( \frac{1}{6} \) inch plates, riveted with lap joints, according to the pressure it is required to stand. The flues are usually two feet six inches or two feet nine inches in diameter, leaving a space of about six inches all round, for the circulation of the water. These flues are strengthened by ribs \( b b \), to prevent collapse, according to the principles developed in my researches on that subject.*

The boiler has flat ends, stayed by triangular gussets \( v, v \). The furnaces are within the flues, and the products of combustion, after passing through these, unite and pass beneath the boiler, towards the front, in the flues \( c c \), where they turn and pass back again on the other side to the chimney flue \( r \).

The ordinary fittings of these boilers consist of a stem dome \( d \), on which is placed a nozzle or stop valve, communicating with the large steam feed pipe \( s \), with which all the boilers communicate. Man-holes \( m, n \) are fitted to the boiler for cleaning and examination. The pipe \( r \) brings the feed water from the hot well of the engine in most cases, whence it passes

* Vide 'Useful Information for Engineers,' Second Series, pp. 1–45.
through a small stop valve down to the bottom of the boiler near the furnace end. Safety valves are shown at $f$, two having fixed weights, and a third being pressed down by a spring balance $g$. At the bottom of the boiler is a mud cock $i$, and there are usually a steam gauge for registering the pressure, and a glass water gauge $k$, for indicating the amount of water in the boiler.

Another form of boiler frequently employed for mills, is in part multitubular. There are two furnaces in two cylindrical flues, precisely similar to those in the preceding boiler, but immediately beyond the furnace; these flues unite into one chamber, in which the gases mix, and thence the gaseous products pass through about a hundred small tubes, three inches in diameter, and about eight feet long. They then circulate in brickwork flues beneath the boiler, and pass to the chimney as in the double-flued boiler. The mixing chamber, from its elliptical form, is weak, but to remedy this defect it is stayed by three vertical water tubes, riveted to the flat sides of the ellipse. Ten boilers of this description supply the steam for the four 100 horse power engines at Saltaire; their principal dimensions are as follows:—Shell 7 feet diameter, 24 feet long, and $\frac{1}{2}$ thickness of plates. Flues containing furnaces 9 feet long, and 2 feet 9 inches in diameter. Mixing chamber 8 feet long, small tubes 7 feet long, grates $2\frac{1}{2}$ feet by $6\frac{1}{2}$ feet.

The heating surface in one of these boilers is as follows:

<table>
<thead>
<tr>
<th>Area of furnace flues</th>
<th>. . . . 135 square feet</th>
</tr>
</thead>
<tbody>
<tr>
<td>&quot; mixing chamber . . .</td>
<td>. . . 102 &quot;</td>
</tr>
<tr>
<td>&quot; three vertical tubes</td>
<td>. . . 28 &quot;</td>
</tr>
<tr>
<td>&quot; small tubes . . . . .</td>
<td>. . . 550 &quot;</td>
</tr>
<tr>
<td>&quot; exterior flues . . .</td>
<td>. . . 285* &quot;</td>
</tr>
<tr>
<td>Total</td>
<td>1,100 &quot;</td>
</tr>
</tbody>
</table>

Area of firegrate, 33 $\frac{1}{2}$ square feet, being in the ratio of 1 to 32.

Messrs. J. and W. Galloway have patented a boiler in which a number of vertical, conical, water tubes, five or six inches in diameter at bottom, and twice as much at top, are introduced

* The area of the flues, 285 feet, under the exterior of the boiler is of little value, as the greater portion of the heat is absorbed by the time it has passed through the three-inch tubes.
into an elliptical flue passing through the boiler. The flame and heated gases circulate amongst these tubes and impinge against their sides. The dimensions of one of these boilers is as follows:—Length 24 feet; diameter 7 feet; greatest diameter of main flue, 5 feet 7 inches; the flue contains 21 vertical water tubes, acting as stays to prevent collapse, 11½ inches in diameter at top, and 6 inches at bottom. These tubes are welded and placed zig-zag fashion, so that a man may creep along each side of the flue to clean or examine it. The two furnaces are each 7½ feet long, 2½ feet diameter.

Another boiler, known as the French or elephant boiler, is sometimes used. It consists of three cylindrical tubes with hemispherical ends, one larger than the other two, and placed above them. The smaller boilers communicate with the upper one by conical water tubes. The furnace is under the lower tubes, and the gases, after passing the length of these, return underneath the larger boiler above, round which they circulate three times.

Messrs. Dunn and Co. manufacture what they term a retort boiler, in which the steam is generated in a number of retorts or cylindrical tubes, about 9 feet long by 18 inches in diameter, placed transversely to the furnace. These all communicate with a large steam chamber above. This boiler is chiefly intended for exportation, being light and convenient for carriage in new countries without roads, or the usual means of conveyance.

Computation of the Power of Boilers.—In our attempts to give any definite rules on this question, we must state that there is hardly any branch of practical science so exceedingly anomalous and unsatisfactory as that of boiler power. In fact, there is no definite rule for our guidance; on the contrary, the whole is a jumble of guesses, and for years I have laboured in vain to reduce our past experience to something like a system, or to some reliable and definite rules calculated to guide us to correct results. This however appears to be impossible, as we are in a constant state of transition with a long vista of speculations before us, which seem likely only to lead to the point from which we started. It is like the smoke question, where every man is his own doctor, and promises much, while
nothing is done. The only sound and definite principles of
construction we have arrived at pertain to the locomotive
boiler, where the area of heating surface, capacity of fire-box
and grate area necessary to generate, with the aid of the blast
pipe, the required quantity of steam, are well ascertained. But
in land and marine boilers we have not as yet come to an
agreement, and probably for this reason, that we have not the
energy of an artificial draught, which in the locomotive in-
creases or diminishes in proportion to the speed of the engine,
and the strength of the blast respectively. Now this is not the
case with the condensing engine, either on shore or afloat, and
notwithstanding that there are many efficient and well-propor-
tioned boilers doing their work well, we are nevertheless defi-
cient in the knowledge of which under any given circumstances
are the best construction and the most economical proportions.

We are still in want of an experimental investigation calcu-
lated to supply data on this subject. The trials hitherto made
have been too partial and under too variable circumstances to be
relied upon. As it is we must be content to take them as they
now exist, under the hope that time may elicit greater certainty
in the improved conditions now in progress. On some future
occasion it is possible we may return to the subject, as it is one
of deep importance in forwarding the manufacturing interests
of the country.

Horses Power of Boilers.—The horses power of boilers is
dependent in part on the capacity of the boiler itself, in part
on the heating surface, and in part on the area of grate and
the consumption of coal per hour. The common rule for
estimating the horse power is as follows:—Calculate the
‘effective section’ of the boiler by adding to the diameter of
the boiler the diameters of any internal flues and multiply-
ing by the length of the boiler, and divide the product by the
constant 5·5, 5·75, or 6, according to the practice of different
engineers.

For condensing engines I have usually allowed about twelve
square feet of ‘effective section’ for each nominal horse power
of the engine, although in practice many conditions necessitate
the alteration of this proportion to suit circumstances. Now, as
ingines are at present constructed, working at from two to three
times their nominal horses power, this is equivalent to an allowance of five square feet of 'effective section' per indicated horse power, and hence agrees approximately with the rule given above. But this empirical rule is not at all to be relied upon, as it gives erroneous results with boilers of different forms and proportions.

The true method of calculating the proper proportion of boiler for any given engine is, however, to estimate the actual amount of steam required, which can easily be done with the aid of the tables, already given, of the weight and density of steam. Then provide a boiler capable of evaporating that weight of water, according to the data obtained in experiments with boilers of the particular construction employed. Some data of this kind will be given below; it being borne in mind that more heat is required, and less water evaporated with a given weight of coal, the higher the pressure at which the steam is employed.

Area of Heating Surface.—The total area of metal exposed to the flame and hot gases is called the total heating surface of the boiler, and is usually expressed in terms of the grate-bar surface. This unit of comparison has, however, been rendered ambiguous by the employment of another unit called the efficient heating surface. The efficient heating surface is obtained by deducting from the total heating surface one-half the area of vertical portions, and one-half the area of horizontal cylindrical flues, on the supposition that the vertical heating surfaces and the under side of flues and tubes act less efficiently in absorbing heat than horizontal surfaces above the flame.

A common allowance of effective heating surface for stationary boilers has been 10 to 15 square feet per square foot of grate area, and one square foot of grate is required per nominal horse power of the engine. I have usually allowed 16 or 17 square feet of effective heating surface; and in Cornish boilers 25 square feet is allowed. In general practice it will, however, be found that such a proportion as 17 will better serve the interests of the employers of steam engines than the extreme limits of 1 in 10 or 1 in 25; at least this is the best proportion for cylindrical-flued boilers. The limits which define the amount of efficient heating surface are on the one hand the temperature of the gases escaping into
the chimney, which should be as low as possible, and on the other the temperature of the boiler bottom, on which soot is deposited. If the gases escape at a higher temperature than is necessary to create a sufficient draught, heat is wasted by dissipation in the atmosphere, in consequence of insufficient heating surface. On the other hand, if the boiler is unduly increased, so that part of the heating surface is coated with soot, and the absorption of heat prevented, not only is boiler space wasted, but heat is lost by radiation.

In the Saltaire boilers the proportions of the heating surface may be estimated as follows:

<table>
<thead>
<tr>
<th></th>
<th>Total heating surface in sq. ft.</th>
<th>Efficient heating surface in sq. ft.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Furnaces</td>
<td>135</td>
<td>68</td>
</tr>
<tr>
<td>Mixing chambers</td>
<td>102</td>
<td>51</td>
</tr>
<tr>
<td>Vertical tubes</td>
<td>28</td>
<td>14</td>
</tr>
<tr>
<td>Three-inch tubes</td>
<td>550</td>
<td>275</td>
</tr>
<tr>
<td>Exterior flues</td>
<td>285</td>
<td>192</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>1,100</strong></td>
<td><strong>600</strong></td>
</tr>
</tbody>
</table>

Area of firegrate, 33.5 square feet.

That is, 17 square feet of effective and 32 square feet of total heating surface per square foot of grate.

Again, in a double-flued tubular boiler, 30 feet long, 7 feet diameter, with two flues each 2 feet 8 inches in diameter, we have the following proportions:

<table>
<thead>
<tr>
<th></th>
<th>Total heating surface</th>
<th>Efficient heating surface</th>
</tr>
</thead>
<tbody>
<tr>
<td>Internal flues</td>
<td>894</td>
<td>262</td>
</tr>
<tr>
<td>Exterior flues</td>
<td>390</td>
<td>118</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>894</strong></td>
<td><strong>570</strong></td>
</tr>
</tbody>
</table>

Area of grates = 33 square feet.

Hence, there would be 27 square feet of total heating surface and 17 feet of effective heating surface, per square foot of grate area.

Boiler Capacity.—In my practice I have always advocated large boilers. I have said before that boilers of limited capacity, when overworked, must be forced, and this forcing is the gangrene which corrupts and festers the whole system of operations. Under such circumstances perfect combustion is out of the question, and every attempt at economy fails. Usually
with flued boilers I have allowed 15 to 20 cubic feet of boiler space per indicated horse power after deducting the flues. Mr. Armstrong contends for 27 cubic feet, of which one-half is steam, and the other half water room. I have allowed one-third for steam and two-thirds for water where the boiler is fitted with a dome. When the steam room is too small, the boiler primes, or water is carried over from the boiler with the steam.

Area of Grate-bar Surface.—The area of the grate depends upon the quantity and quality of the fuel to be burnt. In Cornish boilers, in which the combustion is slowest, only 6 to 10 lbs. of fuel are burnt per square foot of grate bar per hour; and in ordinary factory boilers about 14 to 16 lbs. is the average quantity. In marine boilers the combustion is still more rapid, and in locomotives it rises as high as 40 to 120 lbs. per square foot per hour.

The grate bars are ordinarily made to slope, to facilitate the pushing back of the fuel which has been partially coked on the dead plate. This slope varies from 1 in 5 to 1 in 25, being in cylindrical-flued boilers somewhat restricted by the form of the flue. The fire grate terminates in a brick bridge, over which the flame and products of combustion pass into the flues. These bridges distribute the flame over the boiler bottom, and cause an eddy which facilitates the mixture and combination of the gaseous products.

Mr. D. K. Clarke has very carefully investigated the relations of grate-bar surface, heating surface, and consumption of coal, and has arrived at the following relations:—1st. For a given area of grate the total hourly consumption of fuel should vary as the square of the total heating surface; that is to say, if the heating surface be doubled, the total consumption of fuel might be increased four times, whilst the same evaporative efficiency would be maintained. 2nd. For a given extent of heating surface, the total hourly consumption should vary inversely as the area of the grate. For instance, if the grate surface were increased to twice the area, the total hourly consumption of fuel should be reduced to one-half, in order to maintain the same efficiency. 3rd. For a given hourly consumption of fuel, the area of the fire grate will vary as the square of the heating surface in maintaining the
same efficiency. For example, if twice the heating surface be employed, the grate may be extended to four times. Conversely, if half the heating surface be removed, the grate must be reduced to one-fourth of its area. It is apparent from these relations, as Mr. Clarke has observed, that a superfluous size of grate is detrimental to the power of the boiler, unless at a sacrifice of fuel. On the contrary, an extension of heating surface adds a still greater proportion to the power of the boiler, whilst the efficiency of the fuel is maintained. The general formula embodying these relations is \( F = \frac{\pi R^2}{G} \), in which \( F \) is the quantity of fuel consumed per hour, \( \pi \) the area of heating surface, \( G \) the grate area, and \( c \) a constant varying for each kind of boiler.

Grates for burning wood require to be constructed on different principles from those for the consumption of coal. In this case, from the rapid ignition of the material, the furnace must be constructed capacious, whilst at the same time the area for the admission of air must be reduced. In Russia, where nearly the whole of the coal used in manufacture is imported from this country, it is usual to have the boilers constructed on the same principle as has already been described. It, however, sometimes happens, as in the case of the late war, that the supply of coal ceases, and the owners of mills are in this emergency under the necessity of burning wood, which even in Russia at the present time is more expensive than imported coal. When driven to its use, all that is done is to remove the coal grate and furnace bars, and substitute an iron gridiron, laid on the bottom of the internal flues, which increases the capacity of the furnace and decreases the grate area. The boiler is then as efficient with wood as it was before with coal. In other cases the wood is supplied by a hopper, in which it descends as it burns away at the bottom.

*Evaporative Power of Boilers.*—Good coal liberates in combustion sufficient heat to evaporate from 14 to 15½ lbs. of water, and good coke to evaporate about 13 lbs. of water per pound of the fuel. Wood evaporates only 6 to 7½ lbs. per pound of fuel.

The actual evaporation in engine boilers falls far short of this
theoretical result, owing to the heat carried off by the chimney, imperfect combustion, radiation, \&c.

In 1858 a report was published by Mr. Armstrong, Mr. Longridge, and Mr. Richardson, detailing the results of extensive experiments on the evaporative power of steam coals. These experiments were made with a multitubular boiler, with two furnaces and 135 tubes, 5\frac{1}{2} feet long and 3 inches in diameter. With this boiler they first determined a standard of evaporative power when the boiler was worked on the ordinary system, every care being taken to obtain the maximum of work out of the boiler, by keeping the fires clear and by frequent stoking. No air was admitted except through the firegrates. As the economic effect of the fuel increases when the ratio of the firegrate surface to the absorbing surface is diminished, they adopted two sizes of firegrates, and obtained in consequence two standards of reference. With the larger firegrate the amount of work done by the boiler per hour was greatest, but this was accomplished at a relative loss of economic value of the fuel, as compared with the smaller grate. The one gave the standard of maximum evaporative power of the boiler,—the other the standard of economic effect of the fuel. The grate areas were 28\frac{1}{4} and 19\frac{1}{4} square feet respectively. The heating surface of the boiler was 749 square feet. The results obtained are given in the following table:

<table>
<thead>
<tr>
<th>Economic value, or pounds of water evaporated from 212° by 1 lb. of coal</th>
<th>Firegrate 28\frac{1}{4} sq. ft.</th>
<th>Firegrate 19\frac{1}{4} sq. ft.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rate of combustion, or pounds of coal burned per hour per square foot of grate</td>
<td>9·41 11·15</td>
<td>10·06 12·58</td>
</tr>
<tr>
<td>Rate of evaporation per square foot of firegrate per hour, in cubic feet of water, from 60°</td>
<td>21·15 19·00</td>
<td>21·00 17·25</td>
</tr>
<tr>
<td>Total evaporation per hour in cubic feet of water from 60°</td>
<td>2·62 2·93</td>
<td>2·909 2·995</td>
</tr>
</tbody>
</table>

The columns marked A give the general results, much smoke being often evolved; those marked B, the mean of the best results obtained in the experiments when making no smoke. The coal employed in these experiments, viz. the Hartley’s, is very superior to that ordinarily employed in factory boilers.
By an apparatus constructed by Mr. Wright of Westminster, the same experimenters determined the absolute heating effect of this coal, and of some similar coal from Wales, to be as follows:

<table>
<thead>
<tr>
<th>Coal Type</th>
<th>Heating Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>Welsh coal</td>
<td>14.30 lbs. from 212°</td>
</tr>
<tr>
<td>Hartley coal</td>
<td>14.63</td>
</tr>
</tbody>
</table>

To give some idea of the practical economic effect of coal in stationary engine boilers, we may transcribe here some results obtained with care by Mr. John Graham, of Manchester, not as completely applying to ordinary practice, but as affording useful guidance when taken in conjunction with the preceding results on a better description of coal. The water was measured by a metre.

<table>
<thead>
<tr>
<th>Boiler Description</th>
<th>Pounds of Water Evaporated from 212° by 1 lb. of Coal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Boiler with two internal furnaces, known as ‘breeches boiler’</td>
<td>6.88</td>
</tr>
<tr>
<td>Waggon boiler</td>
<td>10.26</td>
</tr>
<tr>
<td>Cylindrical boiler with external furnace</td>
<td>7.54</td>
</tr>
<tr>
<td>Butterley boiler</td>
<td>9.72</td>
</tr>
</tbody>
</table>

Mr. Longridge has found 6 to 7\(\frac{1}{2}\) lbs. of water evaporated from 62° Fahrenheit, and converted into steam at 20 to 55 lbs. pressure, per pound of coal, by two fluid boilers.

Mr. Rankine’s formula for the efficiency of ordinary stationary boilers without a feed-water heater and with chimney draught is,

\[
\varepsilon_1 = \frac{\frac{14s}{E}}{s + \frac{1}{4}f} \ldots (1);
\]

where \(\varepsilon_1\) is the available evaporative power of one pound of fuel in a boiler furnace, \(\varepsilon\) the theoretical evaporative power, \(s\) area of heating surface, and \(f\) the number of pounds of fuel burnt per hour per square foot of grate. But the reader must be referred to his own work on the steam engine for a discussion of the constants to be employed under different circumstances.

**Strength of Boilers.**—To be of maximum strength, both the external shell and the internal flues should be as far as possible cylindrical. Where this is impossible and flat surfaces are necessary, careful staying by gussets or longitudinal stays is essential to safety. The cylindrical portions of boilers can be
very easily proportioned to the steam they have to bear by the formulae which will be given below. Certain restrictions are placed upon the proportions of boilers by the nature of the riveted joints. That these may be steam and water tight under pressure, and at the same time not unnecessarily weakened by rivets, it has been found best to use plates of about \( \frac{1}{8} \) or \( \frac{1}{6} \) inch thick, and plates of other dimensions are very seldom employed in the construction of boilers. Thick plates are inefficiently riveted, thin ones inefficiently caulked, and this restricts the available thickness for the plates within nearly the limits which have been stated. It is necessary, therefore, in proportioning boilers, having given the working pressure, to choose the diameter which is suitable for such a thickness of plates, lessening the diameter for high pressure boilers and increasing it for low pressure ones. Length does not affect the strength in vessels subject to internal pressure, and hence the diameter is the variable quantity over which we have most control in proportioning the external shell. But the flues, as will be shown, decrease in strength with their length, and this dimension is in that case more easily modified than the diameter.

The general equation expressing the resistance of thin hollow vessels to internal strain is, for spherical vessels,

\[ p = \frac{4 \cdot c \cdot t}{d} \text{(nearly)} \quad (2); \]

and for cylindrical vessels, bursting longitudinally,

\[ p = \frac{2 \cdot c \cdot t}{d} \quad (3). \]

This equation gives the bursting pressure in lbs. per square inch, when the thickness of the plates \( c \) in inches, the tenacity of the joints \( t \) in lbs. per square inch, and the diameter \( d \) in inches, are given.

Thus, for a boiler 7 feet or 84 inches diameter, \( \frac{3}{8} \) inch or \( 0.375 \) inch thick, and with joints having a tenacity of 34,000 lbs. per square inch, the bursting pressure

\[ p = \frac{2 \times 34000 \times 0.375}{84} = 303 \frac{1}{2} \text{ lbs.} \]

The value of \( t \) for various materials is given in the following table:—

\[ \text{PART I.} \]
Without joints:
- Wrought-iron plates: 50,000
- Steel plates: 100,000 to 130,000
- Copper, sheet: 30,000
- Glass: 4,200 to 6,000

With joints:
- Wrought-iron plates, double riveted: 35,700
- Wrought-iron plates, single riveted: 28,600
- Wrought-iron boiler plates, with single joints, crossed: 34,000

In the case of well-constructed wrought-iron stationary boilers, I have been accustomed to take $t = 34,000$, and in this case the bursting pressure of cylindrical vessels is, as was taken above,

$$p = \frac{68000c}{d} \ldots (4).$$

But with boilers the factor of safety is ordinarily taken at 6, or the working pressure is not allowed to exceed one-sixth of the bursting pressure, and in this case the maximum strain on the iron per square inch of section is 5,666 lbs. Putting $p$ for the safe working pressure,

$$p = \frac{11333c}{d} \ldots (5);$$

or in the case of the 7-foot boiler taken above,

$$p = \frac{11333 \times 3.75}{84} = 50.6 \text{ lbs.},$$

equivalent to one-sixth of 303\frac{1}{2}, the bursting pressure.

For half-inch plates we get from formula (5),

$$p = \frac{5666c}{d}, \text{ and } d = \frac{5666}{p};$$

for three-eighths inch plate we have similarly,

$$p = \frac{4250c}{d}, \text{ and } d = \frac{4250}{p};$$

and lastly for five-sixteenths inch plate,

$$p = \frac{3541c}{d}, \text{ and } d = \frac{3541}{p}.$$

That is, in words, to find the safe working pressure of a boiler, divide 5,666 for half-inch plates, 4,250 for three-eighths inch plates, and 3,541 for five-sixteenths inch plates, by the diameter.
in inches. Similarly, to find the safe diameter for a given working pressure, divide the same numbers by that working pressure in lbs. per square inch.

For flues subjected to an external pressure, I have deduced experimentally a formula the data of which are given in 'Useful Information for Engineers,' second series. Putting \( p \) for the collapsing pressure and \( p \) for the safe working pressure as before, \( c \) thickness of plates in inches, \( d \) diameter in inches, \( L \) length in feet,

\[
p = 806300 \frac{c^{2.19}}{Ld} \ldots (6);
\]

\[
p = \frac{p}{6} = 134400 \frac{c^{2.19}}{Ld} \ldots (7).
\]

For practical purposes we may substitute for the power 2.19 the square of the thickness. But it is better to employ a table of logarithms, when we get

\[
p = 1.5265 + 2.19 \log,(100c) - \log, Ld.
\]

Thus, for example, to find the collapsing pressure of a flue 10 feet long, 36 inches in diameter, and composed of half-inch plates, we have approximately,

\[
p = 806300 \times \frac{(\frac{1}{2})^2}{36 \times 10} = 560 \text{ lbs.};
\]

or, more accurately, by logarithms,

\[
\log, p = 1.5265 + 2.19 \log, 50 - \log, 360 = \log, 502 \text{ lbs.}
\]

The safe working pressure of this flue would be \( \frac{502}{6} = 74 \text{ lbs.} \)

This formula shows that with vessels subjected to external pressure the strength varies inversely as the length. That is, a flue 20 feet long will be only one-half the strength of one 10 feet long. This remarkable law enables us to proportion the strength of boiler flues with great ease. By introducing rigid angle or \( T \) iron ribs riveted round the exterior of the flues, we virtually decrease the length and increase the strength in the same proportion. Two or three such rings on the flues of boilers, constructed of plates equal in thickness to those of the shell, will usually render the resistance to collapse equal to the bursting pressure of any other part of the boiler.
Accessories of Boilers. The Feed Pump.—Boilers require replenishing with water in proportion to the waste caused by evaporation or its conversion into steam. For this purpose, in the early boilers, working at very low pressures, an open stand pipe was employed with a valve at top, for the admission of the water from a reservoir regulated by a float in the boiler. With the increase of pressure at which steam engines are now worked, this stand pipe has been abandoned and replaced by the feed pump, either attached to the engine or worked by a donkey engine attached to the boiler. The capacity of this pump must be such as to discharge into the boiler two or three times the quantity of water required by the engine in the shape of steam. The ample tables we have already given of the density of steam will enable this to be calculated with perfect ease. We have only to find the volume of steam required by the engine at each stroke (depending on the rate of expansion at which it works), and the pressure of the steam being known we have to seek its weight in the table of density, page 221, and provision must be made for the discharge of two or three times this quantity into the boiler at each stroke of the engine.

Back Pressure Valves.—To prevent accident in case of stoppage or fracture of the feed apparatus, there should always be placed on the feed pipe between the boiler and the regulating valve a self-acting valve to prevent the return of the water. Supposing the feed pipe accidentally broken, the water in the boiler would be forced back by the pressure of the steam, and expose the boiler to injury by overheating. In such a case the back pressure valve is of great service in preventing the escape of the water when acted on by the pressure of the steam.

Feed-water Heating Apparatus.—When the products of combustion escape into the chimney at an elevated temperature, the heat may be utilised by the employment of water-tubes through which the feed water is introduced on its way to the boiler. Of the arrangements adopted for this purpose the best is that of passing the feed water through a wrought-iron pipe or supplementary boiler, placed in the main flues immediately behind the boiler, where the water is heated to the boiling point after leaving the pump. A more complete apparatus is that of Mr. Green, of Wakefield, known as the 'Fuel Econo-
miser.' It consists of a series of upright tubes through which the feed water passes on its way to the boiler, and is heated above the boiling point, and steam in part generated. The formation of soot on the pipes was the source of the ill success of previous attempts in this direction. This difficulty Mr. Green has overcome by an apparatus of scrapers or cleaners, consisting of rings encircling the pipes, and maintained in constant but slow motion by chains and pulleys driven by a belt from the engine. With this apparatus it is found that when the waste gases escape at a temperature of 400° to 500°, the feed water can be heated to an average of 225°, the temperature of the gases after leaving the pipes being reduced to 250°. To produce this effect 10 square feet of heating surface are provided for each horse power.

Water Gauges.—Every boiler should be supplied with a glass tube, fixed in suitable stuffing boxes, and open at the top and bottom to the boiler to show the level of the water. Gauge cocks at various levels are sometimes employed as supplementary to the glass gauge: both are necessary.

Steam Gauges for indicating the pressure of the steam are also indispensable to the safe working of the boiler. For low pressures an open mercury column is employed on the principle of that used by Regnault in his experiments, and in some cases, to bring the indications within a small compass, the fall of the mercury in the cistern, rather than its rise in the smaller tube, is observed. To avoid the inconvenient length of the open mercury column, the air gauge has been used, in which the mercury in its rise condenses the air in a closed glass tube. This gauge, accurate and sensitive, has yet the fault that the indications decrease in length as the pressure increases, and there is also some difficulty in preserving the quantity of air in the gauge constant. Recently Mr. Allan has overcome these difficulties, by the use of a conical air chamber, so arranged that the indications of the gauge shall be uniform at all pressures, and the air can be renewed at any instant. In M. Bourdon's gauge a curved metallic tube, communicating at one end with the steam boiler, and at the other closed, is used. The curvature of this tube decreases with the increase of pressure in its anterior, and the closed end being free to move is connected with an arrow moving over a graduated
arc and marking the pressure. In Schaeffer and Budenberg’s
gauge the pressure acts on a flat corrugated plate of steel which
expands and raises a rack acting on a toothed wheel, and carry-
ing a similar arrow to indicate the amount of pressure. In
Smith’s gauge a flat spiral spring is used, against which the
pressure acts through the medium of a plate of india-rubber.
All these gauges should be fixed on the boiler with a siphon in
which water from the boiler may condense. In this way the
pressure in the boiler is transmitted through the column of
water, and at the same time the gauge is unaffected by the
temperature of the steam.

Safety Valves.—I usually place three safety valves on
boilers, as shown in fig. 173; two of these have fixed weights on
their levers, and the other is pressed down by a spring
balance, and serves to regu-
late the working pressure of
the boiler. The two larger
valves for a fifty-horse boiler
have each an area of 12
square inches. The third is
of only 5 square inches area.
These valves are fixed to a
common valve seating. The
bearing surfaces of the valves
are made either flat, conical,
or spherical. Flat valves have
a tendency to blow off at too
d low a pressure, from the steam getting between the bearing sur-
faces. These valves should always be open to the atmosphere
that they may be seen.

Man Holes are required to obtain access to the boiler for
purposes of examination and cleaning. In double-flued boilers
one must be placed beneath the flues as well as above them.
Mud Cocks are placed near the bottom of boilers for the dis-
charge of water and sediment.

Fusible Plugs are portions of metal fusing at a temperature
not greatly exceeding the maximum working temperature of the
steam, and fixed in that portion of the boiler most liable to be
overheated from deficiency of water. These plugs are of pure lead or of an alloy of bismuth, lead, and tin, according to the temperature they are required to melt at, and they are thought to prevent danger by relieving the pressure of the boiler, and putting out the fire before the plates are injured by overheating. These plugs, however, tend to lose their fusibility, and to become coated with a protecting coat of oxide or sediment, which prevents the communication of heat. They are not a very reliable provision.

**Plans for the Prevention of Smoke.**—Amongst the earliest of these we may class those which depend on mechanical means for the supply of the fuel.

Of this class is the earliest patent for smoke prevention taken out by James Watt in 1785. By this plan the fire is supplied from above downwards by a reservoir of fuel in contact with the burning mass, the combustion of which is supported by a strong lateral current of air passing direct through the fire to a flue on the other side, aided by a slight downward current beside or through the fuel, which last descends by its own gravity as it is consumed. For the purpose of intercepting and completing the combustion a clear fire is maintained at the entrance into the flues, so that the products of the first fire, being subjected to the intense heat of the second and mingled with atmospheric air, may be effectually consumed.

Apart from the external reservoir, we owe to Watt the dead plate very generally adopted in stationary boilers. The fresh fuel is thrown upon the dead plate, where it gradually cokes, the more volatile constituents distilling over and being consumed by the bright fire beyond. Then the coked fuel is pushed back on to the bars and a new supply introduced in front. This plan, where proper provision is made for the supply of the necessary quantity of air, obviates the production of smoke as effectually as many more complicated contrivances.

The succeeding patentees of the principle of mechanical feeding as a substitute for hand labour, have followed two different plans. Some have made the grate itself to carry forward the fuel, either by revolving horizontally or by rolling forward longitudinally, the grate-bars being connected together to form an endless chain, or by the oscillation of the alternate bars causing
the thrusting forward of the fuel by what has been called a peristaltic movement. Others have made the grate stationary, and have used fans revolving horizontally to distribute the fuel over the grate-bars. In all these cases the coal is supplied slowly and uniformly from a hopper. There is no doubt that the uniform distribution of the fuel over the whole surface of the grate-bars, so far as it is secured by these systems, must be to a large extent advantageous in the diminution of smoke and economy of fuel. At one time they were extensively used, but the complication and expense of the apparatus has led to their general abandonment and the return to hand-feeding.

Other plans for the prevention of smoke depend on a double furnace with alternate firing.

Double furnaces patented by Mr. Losh were in use as early as 1815, and in various modifications have been employed ever since. The principle of double furnaces within the same boiler was first introduced by myself; and the plan adopted has already been described as the double-flued boiler. The two flues enable the stoker to fire alternately, and so maintain a more uniform generation of steam than with a single flue, and the flame passing from one flue mingling with the gases from the other, assists in their combustion. I believe that this simple system of alternate firing, when conjoined with the requisites of the economical generation of steam, viz. plenty of capacity in the boiler, sufficient admission of air, and, what is quite as necessary, careful and attentive stoking, will effect the prevention of smoke without any costly apparatus, so far as that is possible with any given description of fuel. There is this further advantage in double furnaces, that the air required for combustion is necessarily variable. Now a double furnace tends to equalise the supply. The two furnaces fed alternately will not require a maximum or a minimum quantity at the same time, and as the two currents of gaseous products mingle, the surplus air of the one furnace will supply the deficiencies of the other. In this way the tendency is to compensate the supply and demand, and prevent waste from too large or too small a quantity in either furnace.

Others, in seeking the prevention of smoke, have introduced an additional supply of air over the fire.
Mr. C. Wye Williams was one of the earliest, as he has been the most pertinacious and consistent, advocate of the introduction of a large additional volume of air into the furnace, and we have to thank him for the labour he has expended in proving the necessity for air as one of the prime conditions of economy of fuel and success in the prevention of smoke. Mr. Wye Williams contends for a uniform admission of cold air to the furnace, relying upon frequent thin feeding to equalise the needs of the furnace. The peculiar principle of his plan is the mechanical division of the air by causing it to enter the furnace through what he terms a diffusion plate, or partition perforated with numerous small apertures. This is usually placed behind the bridge where the gases needing combustion pass into the flues. There is no doubt this is a convenient method for the introduction of air, and has in many instances effectually prevented the formation of smoke.

Mr. Syme Prideaux contends for a variable admission of air, greatest when the fuel is first thrown on, and decreasing to the ordinary supply through the grate-bars as the fire burns clear. For this purpose he constructs his furnace doors with metal Venetians, which open by a self-acting apparatus when the fuel is supplied. They then gradually close at a regulated speed, altogether independent of the care of the fireman. The air entering through the door is, by an arrangement of plates, warmed as it enters the furnace, and carries back the heat radiating from the door.

All these systems are more or less effective, but I am inclined to think that a judicious engineer, with a careful stoker or fireman, will effect all the objects to be attained with the means placed at his disposal, in a well constructed boiler of sufficient capacity, and with a simple furnace such as has been described in the foregoing chapter, as completely as can be done by any one of the numerous nostrums held forth as the only antidotes for smoke, and promising great economy of fuel.
CHAPTER IX.

ON WINDMILLS.

Atmospheric disturbances causing wind have from a high antiquity been employed as a motive power, and probably the earliest application of this force was the propulsion of ships by sails. Amongst the most primitive races, long before we made much progress, this power was applied in the navigation of small vessels; and the ancient Phœncians, Greeks, and Romans were all of them well acquainted with this mode of employing the force of the wind for purposes of human industry. It is to be regretted that we have no records of the time when it was applied as a motive power in mills; this event is lost in the oblivion of the past, and it was not till early in the thirteenth century that we find the Dutch and French employed in the construction of windmills adapted to the wants of an energetic and industrious population. These times were marked by a growing intelligence that encouraged and fostered inventive talent, and the Dutch millwrights and engineers were long celebrated for their skill and knowledge in every art that had for its object the improvement of the industrial resources of the people.

The following account of their ancient history as far as our knowledge extends, may not be uninteresting to the general reader.

'When were windmills introduced into England? The Romans had hand, and cattle, and water mills; but "it is very improbable, or much rather false," says Beckmann, "that they had windmills;" nor does there seem to be any sufficient ground for the common notion that Europe derived its windmills from the Saracens through the Crusaders.

'It is after or about the date of the Norman Conquest that we begin to hear mention of mills moved by wind in this quarter of the world. "They were first known in Spain, France,
and Germany," says one of the authorities quoted by Haydn, "in 1299." When were they first known in England? The "Boldon Book" of 1183 has frequent mention of mills—as, for example, when it speaks of our sister-borough at the other end of Tyne Bridge: "Gatesheued, cum burgo et molendinis, et piscariis et furnis, et cum tribus partibus terræ arabilis de eadem villa, reddit lx. marcas." ("Gateshead, with its borough and mills, and fisheries and bakehouses, and with three parts of the arable land of the said town, renders 60 marcs." But there is no direct description of the kind of mills which were in use. We are not left, however, without some clue. "William," we are told, "holds Oxenhall: to wit, one ploughland and two cultures of the territory of Darlington, which Osbert de Selby used to hold to farm, in exchange for two ploughlands of land at Ketton," &c. &c.: "debet etiam habere molendinum equorum." ("He ought also to have the horse mill.") And, again, "Guydo de Redwortha * * * operatur ad stagnum molendini, et vadit in legationibus Episcopi." ("Guy of Redworth works at the mill—dam, and goes on the bishop's errands.") So that there were horse and water-mills in the time of Bishop Pudsey; but the "Boldon Book" affords us no glimpse of a windmill, with its revolving wands, lending a picturesque air to the scenery of the bishopric. In the volume, however, before us, containing Hugh Pudsey's survey of the county palatine (edited for the Surtees Society by the Rev. William Greenwell), there is also a roll of receipts and expenditure of the 25th year of Bishop Bec (1307), wherein, among repeated mentions of mills, there is specified distinctly, not only a water, but a windmill:—"Respectio Molendinorum. — In refectione molendi de Heighinton, 71s. 8½d. In ref. molendi de North-auckland, 24s. In ref. moln' fullon' ibidem, 19s. 7d. In refn. moln' de Wolsingham, 100s. 2d. In refn. moln' de Cestr', 12s. 7½d. In ref. moln' de Gatesheued, 13s. 6d. In refn. moln' de Ryton', 10s. In uno novo molendino aquatico facto apud Brunhop', 119s. 10d. ** In refn. moln' de Norton' ad tascam, 31s. 8d. In solutione facta Roberto de Tevydale carpentario pro meremio colpando ad j. molendinum ventricicum faciendum apud Norton', 20s." Have we not here a Scotch carpenter (we may not call him a millwright) cutting wood to make a wind-
mill at Norton, and receiving twenty shillings for his job? It is evident, then, that one windmill, at least, came into existence in the bishopric so early as 1307; and we must not rashly draw any larger conclusions. We must not conclude that there was only one. The sites of some of the other mills mentioned in Bishop Bec's roll, it has been suggested to us, would seem to point to wind as the moving power. There is, for example, the mill at "Clivedon" (Cleadon). ("Firmæ Molendinarum.—De molin de Boldon', Clivedon', et Wyteburne, £8 16s.") And there can be little doubt that in other parts of England (and not improbably in our own) windmills had for a considerable time been enlivening our landscapes. Long before 1299 (the date assigned for their simultaneous introduction into France, Spain, and Germany), Don Quixote might have tilted with the four-armed giants of France and Britain. "Mabillon," says Beckmann, "mentions a diploma of 1105" (when the Crusades were in their early infancy), "in which a convent in France is allowed to erect water and wind mills (molenaina ad ventum);" and "in the year 1143, there was in Northamptonshire an abbey (Pipewell), situated in a wood which, in the course of 180 years, was entirely destroyed"; "one cause of its destruction being said to be, "that in the whole neighbourhood there was no house, wind or water mill built, for which timber was not taken from the wood. (Dugdale, Mon. i. p. 816.) The letter of donation, which appears also to be of the twelfth century, may be found in the same collection (ii. p. 459). In it occurs the expression molendinum ventricum. In a charter also, in vol. iii. p. 107, we read of molendinum ventorium. (See Dugdale's Monasticon, ed. nov. vol. v. p. 431, 442.)"

From this it appears that we did not get our windmills from the Saracens; and the probability is that we had them on this side of Europe before they came into use on the other. It was not till 1332 that Bartolomeo Verde proposed to the Venetians to erect a mill to go by wind; and a site was only granted to him on condition of its surrender if his experiment should fail. Windmills were probably scant at the close of the eleventh century, when the Crusades broke out; but in the twelfth they began to be more common, and "a dispute arose whether the tithes of them belonged to the clergy"—a question which Pope
Celestine III. very naturally, and not unreasonably, determined in favour of the Church.

An ingenious writer in the *Practical Mechanics' Magazine* states that 'About seventy years ago, a master mariner, residing at Dunbar, in Haddingtonshire, devised a novel windmill on the horizontal construction. It consisted essentially of an upright shaft, which carried four arms, at the extremities of which were four masts, rigged with trysails, and the sheets were adjusted so that the sails might take their proper positions, according as they were acted on by a beam wind, "booming out," or coming up in the "wind's eye." A mill so constructed would not possess the important element of durability, as the violent jerks imparted to the sheets would very soon snap them. Several mills on the horizontal construction were in use at the town of Eli, in the litigious kingdom of Fife, at the end of the last century, and were employed in grinding indigo; but they have long since been removed.

'In the twelfth century, when windmills began to be more common, a dispute arose whether the tithes of them belonged to the clergy, and Pope Celestine III. very considerately decided the question in favour of the Church.

'About three or four centuries ago, the avaricious landholders, favoured by the meanness and injustice of Government and the weakness of the people, extended their regality or kingship not only over all streams, but also over the very air, and mills which it impelled, so that small proprietors, before erecting a windmill upon their own property, had first to obtain permission from the superior of the province before doing so.

'The early mills were immovable, and could only work when the wind was in one quarter; they were afterwards placed, not on the ground, but on a float which could be moved round in such a manner that the mill should catch every wind. This method gave rise, perhaps, to the invention of movable mills.

'To turn the mill to the wind, two methods have been invented, and are in common use: in the one the whole structure is arranged so as to turn on a post below; and in the other the roof alone, together with the axle and the wings, is movable. Mills of the former kind are called German mills, those of the latter, Dutch mills. They were both moved round either by a
wheel and pinion within, or by a long lever without, which acted as a stay to the structure, and which was sometimes connected at its extremity to a cart wheel, in order to facilitate its movement horizontally.

During the period of the Crimean war, the writer had an opportunity of examining several of the windmills in European Turkey, and also in the Crimea.

Around the town of Eupatoria, in the Crimea, there appeared to be nearly 200 windmills, chiefly employed in grinding corn; and all which were in a workable state were of the vertical construction, and only one horizontal mill, which seemed to have been out of use for at least a quarter of a century. The tower of this mill was built of brickwork, about 20 ft. diameter at the base, and about 17 ft. at the top, and 20 ft. high; the revolving wings, which consisted of six sets of arms, appeared to be about 20 ft. diameter and about 6 ft. broad, fitted with vertical shutters which were movable on pivots passing through the arms, the shutters being each about 12 in. wide by 5 or 6 ft. high, and the pivots were fixed at about one-third of the breadth from the edge of the shutter, in order that the wind might open and shut them at the proper time, during the revolution of the wings. About one-third of the circumference of the wings was surrounded by a segmental screen to shelter the arms and shutters while moving up against the wind, and the screen seemed to have been hauled round with ropes, in order to suit the direction of the wind.

The writer also examined one of the most recently erected mills on the vertical construction, which had the words "Moulin Français" inscribed upon the door, by way of recommendation. The tower of this mill was also of brickwork, and appeared to be 18 ft. diameter at the base, and about 15 ft. at the top, and about 22 ft. high; the four wings were about 35 ft. diameter, and of a rectangular shape, about 15 ft. long and 5 ft. broad; the surface exposed to the wind was increased or diminished by the application of canvas sails, whose spread could be raised by reefing or twisting up the extreme end of the sails when the mill was in a state of rest. The main axle, which was octagonal in form, was constructed of oak, about 15 in. diameter at the neck, and about 10 in. at the rear end. The front of the axle, which re-
ceived the arms, was square, and the two pairs of arms did not intersect the axle in the same plane, the one pair being in advance of the other; all the arms butted against the axle, and were united to it by side pieces, which were securely bolted to the arms and through the axle, which rendered mortising unnecessary, and preserved the strength of the shaft. The bearing in which the neck of the axle revolved seemed to be formed of some hard wood, probably lignum vitae, and was lubricated with soft soap and plumbago. The rear end of the shaft was fitted with an iron gudgeon, about 3 in. diameter, secured by iron hoops and wedges. About the middle of its length, this axle carried a face wheel about 4 ft. diameter, which was constructed entirely of timber; its arms were mortised through the axle, and secured by iron hoops round the rim, which formed the bearing surface for the friction strap or brake for arresting the speed of the mill. The teeth of this wheel, which were about $3\frac{1}{2}$ or 4 inches broad and $4\frac{1}{2}$ pitch, geared into a "trundle," or pinion, about 14 or 15 in. diameter, fixed on the top of a long vertical wrought-iron shaft, about $2\frac{1}{2}$ in. square, which was coupled at its lower extremity to the rhynd on the top of the millstone spindle, the long shaft being steadied by a bearing near the centre of its length to prevent any jarring or vibration being communicated to the revolving millstones. When the writer visited the mill, the miller was engaged in laying on the revolving stones; he was thus enabled to see the working faces. The millstones were about $3\frac{1}{2}$ ft. in diameter, and were formed of a single stone, similar in appearance to the white siliceous burl obtained from the quarries near Rouen. The stones were not indented with roads and channels to assist in grinding and throwing out the flour, like our flour stones in Britain, but were simply roughened or cracked with the miller's pick. The neck of the millstone spindle was guided by a bushing of hard wood, with the fibre endways,—a mode of bushing employed for more than half a century in the flour mills of this country, and which, no doubt, gave the idea to Mr. Penn, of Greenwich, for his mode of bushing the screw shafts in our modern steamers, and which was better than gun metal in situations precluding the use of unguents.

* When the mill was set agoing, the wings, which were 35 ft.
diameter, performed 29 revolutions per minute, when loaded, and the extremity of the sails acquired a velocity of about 3,200 ft. per minute, or nearly 35 miles per hour, and which showed that the "Crim Tartars" knew the importance of letting off their prime-movers,—a subject not too well understood by some of our British millwrights as yet.'

It is more than probable that we are indebted to the Dutch for our improved knowledge of windmills and wind as a motive power, and it is within my own recollection that the whole of the eastern coasts of England and Scotland were studded with windmills; and that for a considerable distance into the interior of the country. Half a century ago, nearly the whole of the grinding, stamping, sawing, and draining was done by wind in the flat countries, and no one could enter any of the towns in Northumberland, Lincolnshire, Yorkshire, or Norfolk, but must have remarked the numerous windmills spreading their sails to catch the breeze. Such was the state of our windmills sixty years since, and nearly the whole of our machinery depended on wind, or on water where the necessary fall could be secured. These sources of power have nearly been abandoned in this country, having been replaced by the all-pervading power of steam. This being the case, wind as a motive power may be considered as a thing of the past, and a short notice will therefore suffice.

Windmills may be arranged in two classes, namely, the horizontal and the vertical, the sails in the one revolving on a vertical axis, in the other upon a horizontal axis, depressed or raised at a certain angle to the horizon. The first of these has been very little used; the latter kept its ground against all competitors until it was supplanted by its more energetic opponent in the shape of steam.

Much has been done and a great deal of labour has been expended in endeavouring to improve the horizontal mill, but without success. In fact, the horizontal windmill requires so large a surface exposed to the plane of motion, while moving in a medium of the same density by which it is impelled, that it suffers great retardation, and from the principle of the construction and the position of the vanes, only one or two can be in action at the same time. Now this is not the case with the vertical
windmills, as all the sails, four or five in number, act simultaneously, and generally attain a speed greater than the velocity of the wind.

One of the earliest windmills employed in Scotland was erected in 1720, near Dunbar, in Haddingtonshire, and was employed in making pearl barley, and, like a large portion of the barley mills in Holland (of which it was a copy), turned out an unremunerative speculation. With a moderate wind the wings had not power enough to drive the barley mill, and when blowing fresh, they often became unmanageable when the mill was being emptied of barley, and sometimes set the brake wheel on fire. A very simple plan of correcting the variable resistance would be to have two barley mills, and work them alternately; while the one was finishing the barley the other could be receiving its supply of corn, which would render the resisting load nearly uniform, and thus control the speed of the wings.

About the year 1750, Mr. Andrew Meikle, of Houston Mill, in Haddingtonshire, effected several important improvements upon windmills, and was the first to devise a really useful automatic appliance for moving the sails so as to catch every wind. This he accomplished by means of a supplementary set of revolving vanes, about 10 ft. diameter, situated in the rear, and at right angles to the cardinal sails; by reducing the motion of the new set of vanes about 5,000 times, through the intervention of wheel-work, and a worm, operating upon a dead worm ring bolted to the mason-work of the tower, he caused the cap of the tower, along with the axle and the cardinal wings, to veer round to the wind, and these smaller vanes were termed the ‘fan-tail.’ The next improvement which Mr. Meikle attempted was an appliance for reefing the sails when the mill was in motion. His first attempts were not attended with success; but in 1780, he devised a most ingenious adaptation of the centrifugal governor, viz., a sliding frame on the front of the wings which operate upon rollers placed transversely with the arms, and wound up or reefed the narrow canvas sails when the wings attained too great a velocity, and the unfurling of the sails or increasing their spread was accomplished by a weight which actuated a rod passing through the centre of the main axle, and operated centripetally on the sliding frames, and then
unwound the canvass when the motion of the wings was too much retarded. This was the first successful automatic reefing apparatus applied to windmills, and when the wind was not squally, imparted to the vanes a precision of motion little inferior to some of our modern steam engines, and by varying the weights for unfolding the sails the power of the mill could be increased or diminished with facility.

In the year 1788, about two years after Mr. Meikle invented the thrashing machine, he applied his improved windmill for thrashing corn; and in order to illustrate Mr. Meikle's ingenuity in erecting windmills for farm purposes, it was his practice always to erect the thrashing mill previous to the wings of the windmill, and as the thrashing drum revolved upwards of twenty times faster than the main axle, the gearing of the thrashing mill formed a convenient crane for elevating the wings after being attached one by one to the axle at the lower part of this circuit. Mr. Meikle was described by those who knew him as possessing much shrewdness and originality in his profession; and, with the exception of the late Mr. Smeaton, and the elder Rennie, who was Mr. Meikle's pupil, was one of the ablest millwrights of his day, and died poor and unrecompensed for his many useful inventions.

In the year 1758, the late Mr. John Smeaton instituted a series of experiments with a model windmill about 2 ft. diameter, in order to ascertain the best shape and angle for the sails of windmills. In the experiments referred to, the air was in a state of rest, and a progressive motion was communicated to the mill by means of a determinate weight acting by means of a cord coiled round an axis with a horizontal arm, at the extremity of which were four small movable sails; thus the sails met with a constant and equable blast of air, and as they moved round, a cord with a weight affixed was wound about their axes, and they showed what construction of sails and 'angle of weather' produced the best effect. From these experiments, Mr. Smeaton concluded that the angle of weather, with the plane of motion, should, at the extremity of the sails, be 7 deg., and at the middle 18 deg., and at the centre 18 deg., to produce the best effect. But it is an ascertained fact that the angles of weather, instead of being a constant quantity, should
be varied according to the velocity with which the sails are intended to move; when the extremities of the sails are intended to move at 35 miles per hour, the angle of weather should be less than when a speed of only 20 miles an hour is contemplated.

When the sails are planes, and when the extremities move at 30 miles per hour, it has been ascertained that the best angle of weather, with the plane of motion, is 16 deg. A plane, although the best form for the sails of a ship when operated on by a beam wind, and when every part of the sail recedes from the wind with the same velocity, does not apply in the case of revolving sails, where the velocity varies, according to the distance from the centre of motion, and the sails accordingly should be considerably twisted to obtain the same angular velocity, and in order that the moving wind might operate with a uniform purpose over the whole surface of the sails, and the cylinder of wind recede from the sails with a uniform flow. When revolving sails have the form of a plane, the useful area is virtually diminished; and it is a fact worth recording, that the sails of the windmills employed in Holland have considerably more twist than those in Britain.

With reference to the number of sails it is most advantageous to employ, there appears to be a diversity of opinion among millwrights. Four, however, is the most common number employed in Holland, Germany, and France, and also in the South of England. About twenty years ago, some experiments, on a large scale, were made by a millwright residing near Hull, on a mill which had four sails, which were carried away during a gale. When the mill was re-erected, five sails were substituted, the collective area of which was identical with that of the four sails formerly employed. It was found that the five wings or sails produced a better effect than the four previously employed. This improvement was attributed to the wind escaping more freely from the sails, which produced a more steady action, and less reaction or relaxing of their effect or power while passing the tower. The next experiment had eight radiating or tapering sails, which promised good results; but having encountered a hurricane shortly after its erection, all the eight sails were carried away. Perhaps the principal
objection to mills having more than five sails, is their increased first cost, and also the increase of trouble attending their management; so that, all things considered, five sails are found to be the most suitable number in practice; and when a mill with this number of sails is in a state of rest, three of the sails are brought below, and two upwards, in order to lessen the effect of the wind upon the structure.

The conical pendulum, or centrifugal governor, originally devised by Huygens about the middle of the seventeenth century, to regulate the movement of clocks, was applied by Hooper in 1789 to control the motion of flour mills, impelled by wind. In a windmill, when the velocity is increased by the irregular action of the wind, the grain is sometimes forced rapidly through the mill without being sufficiently ground, and by means of the centrifugal force of one or more balls, which fly out as soon as the velocity is augmented, and by operating on a combination of levers in connection with the bridge of the stone, to increase the power, and to diminish the travel, causes the revolving millstone to descend, and bring it in nearer proximity with the bedstone, thus increases the resisting load on the mill; and this appliance is in some parts of England termed a 'lift tenter.' In the early part of the present century, William Cubitt (afterwards Sir William Cubitt), then a millwright, residing at Ipswich, devised a mode of reefing the sails of windmills, by introducing movable shutters on the wings of the mill, which shutters were closed by a governor, like that of the steam engine, operating upon a rod passing through the centre of the main axle. These shutters were suspended on pivots fixed about one-third of their breadth from one side, and when the wind was blowing too strong it opened the shutters and allowed a portion of the wind to pass through them, and so also checked the velocity of the mill. Perhaps an improvement upon Mr. Cubitt's plan might be effected by springs instead of weights to close the shutters, and arranged so that the centrifugal action of the shutter would open them. It is believed that a reefing apparatus so constructed would operate with greater uniformity, and be as sensitive as a properly balanced steam engine governor.

The largest windmills in Britain are to be found at the town
of Great Yarmouth, in the county of Norfolk. The wings of some of these mills describe a circuit of 100 ft. diameter, and with a moderate breeze drive six pairs of millstones 4 ft. 6 in. in diameter, grinding collectively 30 bushels of flour per hour. The main shaft is generally constructed of oak, about 3 ft. in diameter, its main bearing being lined with strips of iron 1½ in. broad, and ½ in. thick, sunk longitudinally into it, and fastened with screws and spring hoops, so as to form the main journal of the shaft, which revolves in a bearing bush or brass. The ‘stock pieces’ to which the arms are fixed are mortised through the axle. This first motion shaft carries the usual face wheel, which is made of cast iron, about 12 ft. in diameter (the rim of which forms the bearing surface for the brake), and gears into a man pinion or ‘wallower’ about 4 ft. in diameter, fixed on the top of the upright shaft. This shaft carries at its lower end a spur wheel, about 14 ft. in diameter, which drives the spindles of six pairs of millstones which are posited around it, each pair being fitted with a ‘lift tenter.’

In order to maintain the efficiency of windmills, it is of much importance that the wood and iron work should be of the best description; the main axle should be of wrought iron, having a cast-iron flange of large diameter keyed on its front, and furnished with recesses for receiving the arms of the wings. The brake wheel should be strongly constructed, and covered with hard wood, and of ample breadth, as well as that of the friction strap, which should be strongly secured to the framing at the top of the tower; and it would be an improvement to have a small force pump worked from the top of the upright shaft to discharge water upon the brake wheel, when the mill requires to be arrested in a gale of wind.

The vertical windmill consists of a tower, near the top of which is an axle carrying four vanes or sails set in a plane inclined about ten degrees to the vertical. The vanes are also inclined to the plane in which they revolve, their inclination varying from the axis to the extremity of the arms. They are made light and filled with thin plates of wood, or are covered with canvas. Thus the wind, blowing perpendicularly to the plane of revolution of the arms, impinges obliquely upon the broad sails, and a rotatory movement is generated, which,
transmitted by bevel gearing, works the millstones, stampers, or other machinery contained in the mill.

The mill-sails require to be placed perpendicularly to the direction of the wind, and for this purpose, in the older mills, the whole upper part of the tower containing the machinery is turned round by manual labour. In more modern constructions, however, a dome or cap carrying the sails is fixed on the summit of the tower, and is turned by a self-acting fly with four or more oblique vanes, similar to a smoke-jack, which, acted upon by the changing currents of wind, gives motion to the cap of the

tower, carrying round with it the wind axis and sails, keeping them perpendicular to the direction of the wind. Such a mill is shown in fig. 174, where \( \text{D} \) is the cap moving on rollers, \( \text{s} \) the shaft carrying the sails \( \text{s} \text{s} \), and the bevel wheel \( \text{a} \text{ a} \), gearing into another bevel wheel \( \text{b} \), on the millstone shaft. The wind acting on the fan \( \text{f} \), communicates motion to the bevel wheel and spur pinion \( \text{e} \), which, acting on a spur wheel or rack fixed on the summit of the tower, causes the revolution of the cap. The sails of the fan are constructed so that, when they lie in
the plane of the wind, they are not affected; but as the wind shifts, it strikes them obliquely, and causes the revolution of the cap till they are again in the plane of the wind.

Of experiments upon windmills by far the most important are those of Smeaton, communicated to the Royal Society in 1759. The inclination of the sail to the plane of revolution he found should vary in the following ratio, where the radius is supposed to be divided into six equal parts, and the angle of the sail given at each point:

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<th>Angle with the plane of motion</th>
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<tr>
<td>0</td>
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<tr>
<td>1</td>
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<td>5</td>
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<td>6</td>
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<td>— centre</td>
</tr>
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<td>18°</td>
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<tr>
<td>19</td>
</tr>
<tr>
<td>18 middle</td>
</tr>
<tr>
<td>16</td>
</tr>
<tr>
<td>12 1/2</td>
</tr>
<tr>
<td>7 extremity</td>
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</table>

This inclination of the sail to the plane of revolution is known as its weather. Sails before Smeaton's time were simple parallelograms; he found, however, that advantage was gained by adding a triangular sail to the leading edge of the radius or whip $a a$, so placed that the sail was broadest at its periphery. The extreme breadth of the sail $c b$ was then made equal to one-third of the radius or whip, and of this $\frac{1}{3}$, or $\frac{1}{6}$ of the radius, was the breadth of the ordinary sail $a b$, and the remaining $\frac{2}{3}$, or $\frac{1}{3}$ of the radius, was the breadth of the triangular leading sail $a c$, as shown in fig. 175. The ordinary length of the whip of the sail is 30 feet.

Regulation of the Speed of Windmills.—This is best effected in the case of windmills with cloth sails, by a plan of Mr. Bywater, in which a series of racks and pinions cause the cloth to roll or unroll according to the strength of the wind.

Another plan, suggested by Mr. (now Sir William) Cubitt at the beginning of this century, is shown at fig. 176, applied to sails which have movable boards or thin plates.
instead of sail-cloth. $a$ is the whip; $b$ the axis on which the sails are carried, and which is hollow to receive the rod $c\,c$. At the extremity of this is a rack $c\,d$, gearing in a pinion $e$, which is connected with a pulley over which is hung a weight, so as to press the rod $c\,c$ outwards with a constant force. $g\,g\,g$ are the boards which form the surface of the sail, and which are connected together so as to open or shut like the bars of a Venetian blind. On the last board of each sail is a toothed segment, in which works a rack $f\,f$, connected by levers with the rod $c\,c$, as shown. By this arrangement the force of the wind, as it varies, opens or shuts the boards of the sail, so as to keep the total pressure on the sails equivalent to the force exerted by the balance-weight hung over the pulley $e$. 
APPENDIX.

EXPERIMENTS ON MR. THOMSON'S VORTEX WHEEL AT BALLYSILLAN, TO DETERMINE ITS EFFICIENCY.

Abstract of Data and Calculations according to which the Vortex was designed—Total Height of Fall = 24 feet. Standard quantity of Water = 420 cubic feet per Minute. Calculated Speed, 292.5 Revolutions per Minute.

Radius of Friction Brake, 4 ft. 2 ins. Circumference, 26.18 feet. In the Table the quantity of Water passing over the Wheel is calculated by means of very refined data arrived at by MM. Poncelet and Lacroix, and submitted to the Academy of Sciences in 1829.

<table>
<thead>
<tr>
<th>No. of Experiment</th>
<th>Total weight on Chain Foot lb.</th>
<th>Duration of each Experiment min. sec.</th>
<th>Total Height of Fall ft.</th>
<th>Height of Friction Break ft.</th>
<th>Total Height of Fall over Wheel ft.</th>
<th>No. of revolutions of Shafts per Minute</th>
<th>No. of Cubic Feet of Water per Min.</th>
<th>No. of Cubic Feet of Water per Min. after being deducted to weight the break</th>
<th>Work given out at Horse Power get Wheel</th>
<th>Work due to the Wheel, Horse Power, Foot lbs. per Minute</th>
<th>Efficiency of Horse Power get Wheel</th>
<th>Remarks entered at the time of the Experiments, relating to the supposed accuracy of the Experiments</th>
</tr>
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<tbody>
<tr>
<td>1</td>
<td>46-31</td>
<td>5 34</td>
<td>1,800</td>
<td>323-3</td>
<td>23-73</td>
<td>718</td>
<td>355-8</td>
<td>354-4</td>
<td>392,000</td>
<td>11-88</td>
<td>523,900</td>
<td>Satisfactorily accurate</td>
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<td>2</td>
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<td>1,800</td>
<td>319-5</td>
<td>23-71</td>
<td>718</td>
<td>355-8</td>
<td>354-4</td>
<td>387,400</td>
<td>11-73</td>
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Remarks on the above Experiments.—It is to be observed that as the Experiments happened to be made in dry weather, the stream in none of them supplied the standard supply of water for which the wheel was particularly adapted. Even with the diminished quantity of water, the efficiencies experimentally found were very high. Also, from information received after the time of the Experiments, it happened that during the Experiments the joint rings of the Vortex were not screwed properly close to the rings of the wheel, and that on their being afterwards screwed close, the power of the wheel was sensibly increased. It is therefore probable that still higher efficiencies are attainable than those shown in the above Experiments.
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